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Miniature radiocarbon measurements (< 150 µg C) from sediments of Lake Żabińskie, Poland: effect of precision and dating density on age–depth models

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Abstract. The recent development of the MIni CArbon DAting System (MICADAS) allows researchers to obtain radiocarbon (14C) ages from a variety of samples with miniature amounts of carbon ($< 150 \mu g C$) by using a gas ion source input that bypasses the graphitization step used for conventional ¹⁴C dating with accelerator mass spectrometry (AMS). The ability to measure smaller samples, at reduced cost compared with graphitized samples, allows for greater dating density of sediments with low macrofossil concentrations. In this study, we use a section of varved sediments from Lake Żabińskie, NE Poland, as a case study to assess the usefulness of miniature samples from terrestrial plant macrofossils for dating lake sediments. Radiocarbon samples analyzed using gas-source techniques were measured from the same depths as larger graphitized samples to compare the reliability and precision of the two techniques directly. We find that the analytical precision of gas-source measurements decreases as sample mass decreases but is comparable with graphitized samples of a similar size (approximately $150 \,\mu g$ C). For samples larger than $40 \,\mu g$ C and younger than 6000 BP, the uncalibrated 1σ age uncertainty is consistently less than 150 years ($\pm 0.010 \text{ F}^{14}\text{C}$). The reliability of ${}^{14}\text{C}$ ages from both techniques is assessed via comparison with a best-age estimate for the sediment sequence, which is the result of an OxCal V sequence that integrates varve counts

with ¹⁴C ages. No bias is evident in the ages produced by either gas-source input or graphitization. None of the ¹⁴C ages in our dataset are clear outliers; the 95 % confidence intervals of all 48 calibrated ¹⁴C ages overlap with the median best-age estimate. The effects of sample mass (which defines the expected analytical age uncertainty) and dating density on age-depth models are evaluated via simulated sets of ¹⁴C ages that are used as inputs for OxCal P-sequence age-depth models. Nine different sampling scenarios were simulated in which the mass of ¹⁴C samples and the number of samples were manipulated. The simulated age-depth models suggest that the lower analytical precision associated with miniature samples can be compensated for by increased dating density. The data presented in this paper can improve sampling strategies and can inform expectations of age uncertainty from miniature radiocarbon samples as well as age-depth model outcomes for lacustrine sediments.

1 Introduction

Radiocarbon (14 C) dating is the most widely used technique to date sedimentary sequences that are less than 50 000 years old. The robustness of age–depth models can be limited by the availability of suitable material for dating; this is particularly a problem for studies on sediments from alpine, polar, or arid regions where terrestrial biomass is scarce. Most accelerator mass spectrometry (AMS) labs recommend that samples contain 1 mg or more of carbon for reliable ¹⁴C age estimations. It is well established that terrestrial plant macrofossils are the preferred material type for dating lake sediments because bulk sediments or aquatic macrofossils may have an aquatic source of carbon, which can bias ¹⁴C ages (Groot et al., 2014; MacDonald et al., 1991; Tornqvist et al., 1992; Barnekow et al., 1998; Grimm et al., 2009). Furthermore, a high density of ¹⁴C ages (i.e., one age per 500 years) is recommended to reduce the overall chronologic uncertainty of age-depth models (Blaauw et al., 2018). Researchers working on sediments with low abundances of terrestrial plant macrofossils face difficult choices about whether to date suboptimal materials (e.g., bulk sediment or aquatic macrofossils), pool material from wide sample intervals, or rely on few ages for their chronologies. The problem of insufficient material can affect age estimates at all scales from an entire sedimentary sequence to a specific event layer which a researcher wishes to determine the age of as precisely as possible.

Recent advances have reduced the required sample mass for AMS ¹⁴C analysis, opening new opportunities for researchers (Delqué-Količ et al., 2013; Freeman et al., 2016; Santos et al., 2007; Shah Walter et al., 2015). The recently developed MIni CArbon DAting System (MICADAS) has the capability to analyze samples with miniature masses via the input of samples in a gaseous form, thus omitting sample graphitization (Ruff et al., 2007, 2010a, 2010b; Synal et al., 2007; Szidat et al., 2014; Wacker et al., 2010a, b, 2013). Samples containing as little as a few micrograms of C can be dated using the gas-source input of the MICADAS. The analysis of such small samples provides several potential benefits for dating lake sediments: (1) the possibility to date sediments that were previously not dateable using ${}^{14}C$ due to insufficient material, (2) the ability to date sedimentary profiles with a greater sampling density and lower costs per sample, and (3) the ability to be more selective when selecting material to be analyzed for ¹⁴C. The disadvantage of miniature samples is increased analytical uncertainty, which is a consequence of lower counts of carbon isotopes and the greater impact of contamination on the measurement results. The goal of this study is to assess the potential benefits and limits of applying miniature ¹⁴C measurements to dating lake sediments. We aim to answer the following questions in this study: (1) How reliable and how precise are gas-source ${}^{14}C$ ages compared with graphitized ages? (2) What is the variability of ¹⁴C ages obtained from a single stratigraphic level? (3) How do analytical precision and dating density affect the accuracy and precision of age-depth models for lake sediments?

In this study, we use the sediments of Lake Żabińskie, Poland, as a case study to investigate the application of gas-source ¹⁴C measurements to lake sediments. We focus on a continuously varved segment of the core, which spans roughly 2.1 to 6.8 ka. We report the results of 48 radiocarbon measurements (17 using graphitization and 31 using the gassource input) in order to compare the precision and reliability of gas-source ¹⁴C ages with graphitized samples. The core was sampled such that up to five ages were obtained from 14 distinct stratigraphic depths. A floating varve chronology was integrated with the ¹⁴C ages to produce a best-age estimate using the OxCal V-sequence routine (Bronk Ramsey, 2008). This best-age estimate is used as a benchmark for the ¹⁴C results. The results of our ¹⁴C measurements were used to constrain a statistical model designed to simulate sets of ¹⁴C ages in order to test nine different hypothetical sampling scenarios in which we manipulate the number of ages and the mass of C per sample, which determines the analytical uncertainty of the simulated ages. By comparing the results of the simulated age-depth model outputs from these simulated ¹⁴C ages with the best-age estimate from which the simulated ages were derived, we can improve our understanding of how the number of ages and their analytical precision influence the accuracy and precision of radiocarbon-based age-depth models.

2 Materials and methods

2.1 Core material and radiocarbon samples

Cores were obtained from Lake Żabińskie (coring site: 54.1318° N, 21.9836° E, 44 m water depth) in 2012 using an UWITEC piston corer (90 mm diameter). Lake Żabińskie is a small (41.6 ha), relatively deep (44.4 m) kettle-hole lake located at an altitude of 120 m a.s.l. The catchment is 24.8 km² and includes two other smaller lakes: Lake Purwin and Lake Łękuk. Average temperatures range from 17 °C in summer to -2 °C in winter. Annual precipitation is 610 mm, with the annual peak in summer (JJA). The geology of the catchment is primarily glacial till, sandy moraines, and glacial fluvial sands and gravels (Szumański, 2000). Modern land cover in the catchment is a mixture of cultivated fields and primarily oak-lime-hornbeam and pine forests (Wacnik et al., 2016). The high relative depth (6.1%; calculated according to Wetzel et al., 1991) of Lake Zabińskie leads to strong seasonal stratification, bottom-water anoxia, and the preservation of varves in the sediments (Bonk et al., 2015a, b; Tylmann et al., 2016; Żarczyński et al., 2018). Varve-based chronologies and ¹⁴C measurements have been published for the most recent 2000 years of the Lake Żabińskie sedimentary sequence (Bonk et al., 2015a; Żarczyński et al., 2018). These studies show major changes to varve structure and a 3-fold increase in sedimentation rates in response to increased cultivation and deforestation, beginning around 1610 CE. Prior to this time, land cover in the region was relatively stable, with forest or woodland cover dominating the landscape from the early Holocene until the 17th century CE (Wacnik, 2009; Żarczyński et al., 2019).

A composite sediment profile was constructed from overlapping, 2 m long cores by correlating distinctive stratigraphic features. The composite sequence spans 19.4 m. Published downcore varve counts stop above a $\sim 90 \,\mathrm{cm}$ thick slump or deformed unit. This slump event is dated to 1962-2071 cal BP (present: 1950 CE) based on an extension of the varve count published in Zarczyński et al. (2018). This study focuses on a section of core (7.3-13.1 m depth in our composite sequence) directly below this slump unit; this section was selected because it features continuous well-preserved varves throughout the section. Samples of 1 to 2 cm thick slices of sediment were taken from the core (sample locations and core images are found in Supplement - File S1), then sieved with a 100 µm sieve. Macrofossil remains were identified and photographed (File S2), and only identifiable terrestrial plant material was selected for ¹⁴C measurements. Suitable macrofossils from a single stratigraphic level were divided into subsamples for analysis, with the goal of producing one graphitized ¹⁴C age and 2-4 gas-source ages from each depth. When convenient, we grouped samples by the type of material (leaves, periderm, needles, seeds, or woody scales), though 11 samples are a mixture of material types. In most cases, subsamples within a stratigraphic level are assumed to be independent, meaning they may have different true ages. However, there are some subsamples that were taken from single macrofossil fragments (six subsamples taken from two fragments sampled from two different depths); thus these samples have the same true age. It is also possible that subsamples from a single depth may be from the same original material without our knowledge (i.e., a macrofossil could break into several pieces while sieving, and these pieces could be analyzed as separate subsamples).

Sample material was treated with an acid-baseacid (ABA) method at $40 \,^{\circ}$ C, using $0.5 \,\text{mol}\,\text{L}^{-1}$ HCl, 0.1 mol L^{-1} NaOH, and 0.5 mol L^{-1} HCl for 3, 2, and 3 h, respectively. After drying at room temperature, samples were weighed, and those less than 300 µg were input to the gas ion source via combustion in an Elementar Vario EL Cube elemental analyzer (Salazar et al., 2015). Larger samples were graphitized following combustion using automated graphitization equipment (AGE) (Szidat et al., 2014). Radiocarbon data was processed using the software BATS (Wacker et al., 2010a). Additional corrections were applied to the data to account for cross contamination (carryover), and constant contamination (blanks) (Gottschalk et al., 2018; Salazar et al., 2015). The parameters for these corrections were calculated based on standard materials (the primary NIST standard oxalic acid II (SRM 4990C) and sodium acetate (Sigma-Aldrich, no. 71180) as ¹⁴C-free material) run with the sample batches. We applied a constant contamination correction of $1.5 \pm 0.2 \,\mu g \,C$ with $0.72 \pm 0.11 \,F^{14}C$ and a cross contamination correction of $(1.2\% \pm 0.3\%)$ from the previously run sample. Measurement uncertainties were fully propagated for each correction. In total, 48 ages were obtained from 14 distinct stratigraphic levels (17 graphitized and 31 gas-source measurements).

2.2 Varve count

Varves in Lake Żabińskie are biogenic, with calcite-rich pale laminae deposited in spring and summer and darker laminae containing organic detritus and fine clastic material deposited in winter (Żarczyński et al., 2018). We defined the boundary of each varve year by the onset of calcite precipitation (i.e., the upper boundary of dark laminae and lower boundary of light-colored laminae). Varves were counted using CooRecorder software (Larsson, 2003) on core images obtained from a Specim PFD-CL-65-V10E linescan camera (Butz et al., 2015). Three people performed independent varve counts, and these three counts were synthesized and uncertainties calculated according to the methodology recommended by Żarczyński et al. (2018) yielding a master varve count with asymmetric uncertainties.

Because of the slump deposit above our section of interest, the varve chronology is "floating" and must be constrained by the ¹⁴C ages. Several different approaches were used to compare the varve count with the ¹⁴C ages, all of which rely on some assumptions. One method is to tie the varve count to the radiocarbon-based age at a chosen depth in the core. We tested this method using the median calibrated age of the uppermost dated level as the tie point. Such an approach assumes that the radiocarbon-based age at the tie point is correct. An additional drawback is that the choice of tie point is arbitrary and can change the resulting varve count ages. Alternatively, we used least-squares minimization to fit the varve count to all radiocarbon ages (Hajdas et al., 1995) by minimizing the offset between the varve count and the combined calibrated radiocarbon age at each dated level. However, we focus on a third, more sophisticated method, which is the OxCal 4.3 V sequence (Bronk Ramsey, 2008, 2009; Bronk Ramsey and Lee, 2013). This technique integrates all available chronological information including varve counting and ¹⁴C ages into a single model to determine a best-age estimate for the sequence (see section below for more details). The advantages of this approach are that all ages are considered equally likely to be correct (or incorrect), and the error estimate of the V sequence is relatively consistent along the profile, whereas the error associated with the varve count is small at the top of the section but increases downcore. Additionally, this technique allows for the possibility that the master varve count is incorrect (within the expected uncertainty of the count).

2.3 Age-depth modeling

Age–depth modeling was performed using OxCal 4.3 (Bronk Ramsey, 2008, 2009; Bronk Ramsey and Lee, 2013), which integrates the IntCal13 calibration curve (Reimer et al., 2013) for 14 C ages with statistical models that can be used to con-

struct age-depth sequences. As an initial test to compare the reliability of gas-source ages and graphitized ages, and their effect on age-depth models, we produced three P-sequence models: one using all obtained ¹⁴C ages, one using only graphitized ages, and one using only gas-source ages. For all OxCal models in this study, ages measured from the same depth were combined (using the function *R_combine*) into a single ¹⁴C age with uncertainty before calibration and integration into the age-depth sequence. This choice was verified by the chi-squared statistic calculated by OxCal to test the agreement of ages sampled from a single depth. For every combination of ages except one, we find that the chisquared test is passed at the 0.05 significance level. We justify the use of the combine function even for the grouping that failed to pass the chi-squared test (samples from 811 cm depth) because all ages in this group overlap, and there is no significant difference when models are run with the ages separated at this depth (less than 5 years difference for median age and confidence interval, CI). The OxCal P sequence uses a Bayesian approach in which sediment deposition is modeled as a Poisson (random) process. A parameter (k)determines the extent to which sedimentation rates are allowed to vary. For all P-sequence models in this study, we used a uniformly distributed prior for k such that $k_0 = 1$, and $\log_{10}(k/k_0) \sim U(-2, 2)$; this allows k to vary between 0.01 and 100. Sediment deposition sequences are constrained by likelihood functions produced by the calibration of radiocarbon ages. Thousands of iterations of sediment deposition sequences are produced using Markov Chain Monte Carlo (MCMC) sampling (Bronk Ramsey, 2008). These iterations can then be summarized into median age estimates, with confidence intervals.

The varve counts and all ¹⁴C ages were incorporated into an OxCal V sequence in an approach similar to that used by Rey et al. (2019). The V sequence differs from the P sequence in that it does not model sediment deposition. Instead, the V sequence uses "Gaps" (the amount of time between two points in a sequence) to constrain the uncertainty of radiocarbon ages. The gap can be determined from independent chronological information such as varve counts or tree ring counts. We input the number of varves in 10 cm intervals to the V sequence as an age gap with associated uncertainty. The OxCal V sequence assumes normally distributed uncertainties for each gap, whereas our varve count method produces asymmetric uncertainty estimates. We used the mean of the positive and negative uncertainties as inputs to the V sequence. However, OxCal sets the minimum uncertainty of each gap equal to 5 years, which in most cases is larger than the mean uncertainty in our varve count over a 10 cm interval. By including the varve counts as an additional constraint, the V sequence produces a more precise age-depth relation than the P sequence, which only considers the radiocarbon ages.

2.4 Age-depth model simulation

In order to test the effects of analytical uncertainty and dating density (number of ages per time interval) on age-depth models, we designed an experiment in which nine different sampling scenarios were simulated for the Lake Zabińskie sedimentary sequence to determine the expected precision and accuracy of resulting age-depth models. Three different sampling densities were simulated for the 5.8 m long section: 5, 10, and 20 ages (equivalent to approximately 1, 2, and 4 ages per millennium, respectively). For each of these sampling densities three different sample-size scenarios were simulated: 35, 90, and 500 µg C. These scenarios were designed to represent different sampling circumstances such as high or low abundances of suitable material for ¹⁴C analysis and different budgets for ¹⁴C analysis. Radiocarbon ages were simulated using a technique similar to Trachsel and Telford (2017). In brief, we distributed the simulated samples evenly by depth across the 5.8 m long section and then used the median output of the OxCal V sequence as the assumed true age for a given depth. This calibrated assumed true age was back-converted to ¹⁴C years using IntCal13 (Reimer et al., 2013). A random error term was added to the ¹⁴C age to simulate the analytical uncertainty. The error term was drawn from a normal distribution with mean zero and standard deviation equivalent to the age uncertainty determined from the relationship between sample mass and age uncertainty found in the results of our ¹⁴C measurements (Fig. 1a). The same expected analytical uncertainty was used for the age uncertainty for each simulated age. For a sample with 35 µg C, we expect a measurement uncertainty of ± 148 years (or $\pm 0.0114 \,\mathrm{F}^{14}$ C), which is representative of the average age of all samples in this study (approximately 4000¹⁴C BP). In reality, older samples would have greater age uncertainty, while younger samples would have less uncertainty. However, the effect of these differences on the performance of simulated age-depth models would be minimal as roughly half the ages would be more precise and half would be less precise. These simulated ¹⁴C ages were input into an Ox-Cal P sequence using the same uniform distribution for the k parameter as described in the previous section. This experiment was repeated 30 times for each scenario to assess the variability of possible age-model outcomes. We quantify the accuracy of the age-depth models as the deviation of the median modeled age from the best-age estimate at a given depth. We define precision as the width of the age-depth model CI.

3 Results

3.1 Radiocarbon measurements

In total, 48 radiocarbon measurements on terrestrial plant macrofossils were obtained from the section of interest yielding values from 0.475 to $0.777 \,\mathrm{F^{14}C}$ (2030 to 5990 ¹⁴C BP; Table 1). Thirty-one ages were measured using the gas-



Figure 1. (a) Age uncertainty of AMS radiocarbon ages (without calibration) versus the mass of carbon in the sample. Note that these samples date to approximately 2000–6000 BP; older ages will have greater age uncertainties. Note the logarithmic scale on the *x* axis. The black line represents the best-fit power model for our dataset. (b) Same as (a), except uncertainties are plotted as measurement uncertainty in $F^{14}C$ units. This measure of uncertainty is not directly influenced by the age of the sample.

source input; these samples contained between 11 and 168 µg C. Seventeen samples containing between 115 and 691 µg C were measured using graphitization. Analytical uncertainties for the 14 C measurements range from ± 0.0027 to $\pm 0.0306 \,\mathrm{F}^{14}\mathrm{C}$ (± 41 to ± 328 years) with higher values associated with the smallest sample masses. The uncertainties for gas-source measurements and graphitized measurements are comparable for samples that contain a similar amount of carbon (Fig. 1). Samples containing less than 40 µg C (roughly equivalent to 80 µg of dry plant material) produce uncertainties greater than ± 150 years (1 σ). We use a power-model fit with least-squares regression, to estimate the typical age uncertainty for a given sample mass ($r^2 = 0.90$, p < 0.001, Fig. 1). The resulting power model is nearly identical to what would be expected based on the assumed Poisson distribution of the counting statistics where the uncertainty follows the relationship $N^{-0.5}$ (N: the number of measured ¹⁴C atoms).

When comparing measurements taken from within a single sediment slice we find good agreement for all ¹⁴C ages, regardless of whether the samples were analyzed with the gas-source input or via a graphitized target (Fig. 2), and no clear bias based on the type of macrofossil that was dated (Fig. 3). One method to test whether the scatter of ages is consistent with the expectations of the analytical uncertainty is a reduced chi-squared statistical test, also known as mean square weighted deviation (MSWD) in geochronological studies (Reiners et al., 2017). If the spread of ages is exactly what would be expected from the analytical uncertainty, the value of this statistic is 1. Lower values represent less scatter than expected, and larger values represent more

scatter than expected. Of the 11 sampled depths with three or more ages, only one (811 cm, MSWD = 3.07) returned an MSWD that exceeds a 95 % significance threshold for acceptable MSWD values that are consistent with the assumption that the age scatter is purely the result of analytical uncertainty.

3.2 Varve count and age-depth modeling

In total, 4644 (+155/-176) varves were counted in the section of interest, with a mean varve thickness of $1.26 \pm$ 0.58 mm (Fig. 4). Full varve count results are available at https://doi.org/10.7892/boris.134606. Sedimentation rates averaged over 10 cm intervals range from 0.91 to 2.78 mm yr^{-1} . All chronological data (¹⁴C ages and varve counts) were integrated to generate a best-age estimate for the section of interest using an OxCal V sequence (output of the Oxcal V sequence is available at https://doi.org/10.7892/boris.134606). This produced a wellconstrained age-depth model with a 95% CI width that ranges from 69 to 114 years (mean 86 years). OxCal uses an agreement index to assess how well the posterior distributions produced by the model (modeled ages at the depth of ¹⁴C ages) agree with the prior distributions (calibrated ¹⁴C ages). The overall agreement index for our OxCal V sequence is 66.8%, which is greater than the acceptable index of 60 %. Three of the fourteen dated levels in the V sequence had agreement indices less than the acceptable value of 60 % (A = 22.8 %, 48.5 %, and 52.6 % for sample depths of 1283.0, 1176.1, and 732.5 cm, respectively); nonetheless



Figure 2. (a) Comparison of age–depth model outputs from OxCal (Bronk Ramsey, 2008, 2009; Bronk Ramsey and Lee, 2013; Reimer et al., 2013). From left to right: OxCal V sequence using all ¹⁴C ages as well as varve counts as inputs; OxCal P sequence using all ¹⁴C ages; OxCal P sequence using only gas-source ¹⁴C ages; OxCal P sequence using only graphitized ¹⁴C ages. The median age of the V sequence is considered the best-age estimate and is repeated in all four panels as a red line. Gray lines represent the upper and lower limits of the 95 % confidence interval of each model. Black lines represent the median ages of the P sequences. (b) Radiocarbon calibrated age probability density functions for each measured age, grouped by composite depth. The best-age estimates from the OxCal V sequence are plotted as red lines for comparison. The = symbol adjacent to some probability density functions indicates that these ages (within a single depth) came from the same specimen and have the same true age.

Table 1. Results of the 48 14 C analyses obtained for this study. Uncertainties of 14 C ages refer to 68% probabilities (1 σ), whereas ranges of calibrated and modeled ages represent 95% probabilities.

Material	<i>Pinus sylvestris</i> seed fragments (seed wing, and fragments of seed)	Terrestrial seed fragment Periderm (coniferous) Woody scale Ahuus seed fragments Dicotyledonous leaf fragment ³ Dicotyledonous leaf fragment ³ Dicotyledonous leaf fragment ³ Dicotyledonous leaf fragments Nicotyledonous leaf fragments wordy scales	<i>Pinus sylvestris</i> needle Woody scale <i>Pinus sylvestris</i> needle Peridern (deciduous)	Periderm, dicotyledonous leaf fragments, woody scales	Dicotyledonous leaf fragment Dicotyledonous leaf fragment Dicotyledonous leaf fragments, periderm fragments Periderm Dicotyledonous leaf fragments Dicotyledonous leaf fragments Dicotyledonous leaf fragment ³ Dicotyledonous leaf fragment ³	Betula seed fragments, terrestrial woody material, woody scale, periderm fragments Leaf fragments Wood fragment, Periderm fragments Periderm, woody scales Betula alba seed Periderm fragments Periderm fragments Periderm fragments
Modeled age from OxCal V sequence (Cal BP) ²	2106–2218	2106–2218 2106–2218 2106–2218 2297–2402 2611–2703 2611–2703 2611–2703 2611–2703	2850–2929 2850–2929 2850–2929 2850–2929	3113–3187	3113–3187 3113–3187 3113–3187 3113–3187 3391–3462 3391–3462 3391–3462 3391–3462 3391–3462 3391–3462 3391–3462 3845–3915 3845–3915 3845–3915 3845–3915	4084–4155 4084–4155 4084–4155 4540–4616 4540–4616 4540–4616 4960–5042 4960–5042
Calibrated age (Cal BP) ¹	1823–2293	1867–2361 1416–2968 1636–3325 1998–2702 2159–2715 2183–2725 2437–3447 2490–2754	2760–3076 2774–3143 2790–3174 2807–3229	2764–3984	2761–3215 2876–3374 2866–3358 2979–3340 3078–3700 3375–3696 3375–3696 3375–3696 3375–34086 3717–4084 3724–4086 3724–4086	3829-4417 3731-4832 3725-4836 4296-4837 4299-4832 4421-4813 4655-5318 4860-5434
¹⁴ C age (BP)	2028 ± 72	2149 ± 112 2190 ± 322 2386 ± 328 2273 ± 117 2358 ± 84 2379 ± 82 2379 ± 82 2379 ± 82 2379 ± 82 2379 ± 82	2799 ± 67 2820 ± 72 2857 ± 73 2885 ± 72	3158 ± 252	2845 ± 96 2968 ± 99 2944 ± 97 2980 ± 56 3197 ± 119 3296 ± 74 3145 ± 51 3542 ± 45 3592 ± 62 3593 ± 62 3503 ± 59 3603 ± 59 3616 ± 62 3631 ± 75	$\begin{array}{c} 3724\pm107\\ 3856\pm194\\ 3856\pm203\\ 4062\pm97\\ 4042\pm105\\ 4042\pm105\\ 4045\pm52\\ 4387\pm108\\ 4475\pm90\end{array}$
Graphite/ gas	Gas	Gas Gas Gas Gas Gas Gas Gas Gramhite	Graphite Graphite Graphite Graphite	Gas	Gas Gas Gas Graphite Graphite Graphite Graphite Graphite	Gas Gas Gas Gas Gas Gas Gas Gas
Carbon mass (µg)	168	34 11 11 36 87 87 21 21 553	131 120 115 120	21	54 50 52 37 37 37 37 328 328 691 179 691 179 124	42 23 23 26 46 49 49 135
Centered composite depth (cm)	732.5	732.5 732.5 762 811 811 811 811	861 861 861 861	902.5	902.5 902.5 902.5 941.5 941.5 941.5 941.5 941.5 1001.4 1001.4 1001.4 1001.4	1031.2 1031.7 1031.7 1031.7 1081.7 1081.7 1125.2 1125.2
Bottom core depth (cm)	<i>LL</i>	77 77 37 86 86 86	21 21 21 21 21 21 21 21 21 21 21 21 21 2	62.5	62.5 62.5 62.5 62.5 62.5 101.5 45 45 45 45	26 26 76 76 119.5 119.5
Top core depth (cm)	75	75 75 36 85 85 85 85	50 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	61.5	6.15 6.15 6.16 6.16 7.10 7.00 44 44 44 44	24 25 25 75 75 75 75 118.5 118.5
Core ID	ZAB-12-4-3-2	ZAB-12-4:3-2 ZAB-12-4:3-2 ZAB-12-4:3-2 ZAB-12-4:3-2 ZAB-12-3:4-2 ZAB-12-3:4-2 ZAB-12-3:4-2 ZAB-12-3:4-2 ZAB-12-3:4-2 ZAB-12-3:4-2	ZAB-12-4-4-2 ZAB-12-4-4-2 ZAB-12-4-4-2 ZAB-12-4-4-2 ZAB-12-4-4-2	ZAB-12-4-4-2	ZAB-12-4-4-2 ZAB-12-4-4-2 ZAB-12-4-4-2 ZAB-12-4+4-2 ZAB-12-4+4-2 ZAB-12-4+4-2 ZAB-12-3-5-2 ZAB-12-3-5-2 ZAB-12-3-5-2 ZAB-12-3-5-2 ZAB-12-3-5-2 ZAB-12-3-5-2 ZAB-12-3-5-2	ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1 ZAB-12-4-5-1
Lab ID	BE-9791.1.1	BE-9793.1.1 BE-9792.1.1 BE-9794.1.1 BE-9503.1.1 BE-9502.1.2 BE-9502.1.1 BE-9502.1.1 BE-9501.1.1 BE-9501.1.1 BE-9501.1.1	BE-9497.1.1 BE-9498.1.1 BE-9496.1.1 BE-9499.1.1	BE-9495.1.1	BE-9494.1.1 BE-9494.1.2 BE-9494.1.3 BE-9491.1.1 BE-9491.1.1 BE-9490.1.2 BE-9489.1.1 BE-9489.1.1 BE-9489.1.2 BE-9489.1.3 BE-9489.1.3 BE-9489.1.3	BE-9795.1.1 BE-9487.1.1 BE-9488.1.1 BE-9488.1.1 BE-9486.1.1 BE-9484.1.1 BE-9483.1.2 BE-9483.1.1

Top	Bottom	Centered					Modeled age	
core	core	composite	Carbon		^{14}C	Calibrated	from OxCal	
depth	depth	depth	mass	Graphite/	age	age	V sequence	
(cm)	(cm)	(cm)	(µg)	gas	(BP)	(Cal BP) ¹	(Cal BP) ²	Material
54	55.5	1176.1	95	Gas	4850 ± 104	5321–5887	5500-5591	Woody seed fragments, leaf fragments, woody scales
54	55.5	1176.1	22	Gas	5246 ± 232	5485-6536	5500-5591	Periderm fragments
79	80	1200.8	35	Gas	5081 ± 228	5320-6315	5745-5832	Periderm fragments
79	80	1200.8	42	Gas	5063 ± 127	5586-6178	5745-5832	Periderm, woody scale
79	80	1200.8	111	Graphite	5197 ± 86	5745-6190	5745-5832	Periderm fragments and woody scales
5	6	1242.5	49	Gas	5601 ± 125	6032-6718	6175-6267	Periderm and woody scale
S	6	1242.5	72	Gas	5294 ± 107	5768-6300	6175-6267	Periderm
S	6	1242.5	45	Gas	5410 ± 127	5920-6439	6175-6267	Periderm fragments
S	6	1242.5	504	Graphite	5402 ± 43	6020-6294	6175-6267	Pinus periderm fragments
45.5	46.5	1283	34	Gas	5988 ± 162	6479-7250	6531-6643	Dicotyledonous leaf fragments
45.5	46.5	1283	55	Gas	5787 ± 119	6317-6880	6531-6643	Dicotyledonous leaf fragments
45.5	46.5	1283	74	Gas	5868 ± 107	6415-6949	6531-6643	Dicotyledonous leaf fragments
45.5	46.5	1283	38	Gas	5936 ± 150	6436-7165	6531–6643	Dicotyledonous leaf fragments
45.5	46.5	1283	143	Graphite	5916 ± 78	6547–6946	6531-6643	Dicotyledonous leaf fragments, periderm fragment
h the IntCall n a single fra	3 calibration agment prior 1	curve (Bronk R: to analysis; thus	amsey, 2009; samples with	Reimer et al., 2 hin the same de	2013). The range 1 pth with this symb	reported here reprisol have the same	esents the 95 % con true age.	fidence interval. ² Range represents 95 % confidence interval.
	Top core depth (cm) 54 54 79 79 79 79 79 79 79 79 79 79 79 79 5 5 5 5	Top Bottom core core depth depth (cm) (cm) 54 55.5 79 80 79 80 79 80 55 6 5 6 5 6 5 6 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 45.5 46.5 5 46.5 6 5 6 5	Top Bottom Centered core core composite depth depth depth (cm) (cm) (cm) 54 55.5 1176.1 79 80 1200.8 79 80 1200.8 79 80 1200.8 55 6 1242.5 5 6 1242.5 5 6 1242.5 5 6 1242.5 5 6 1242.5 5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 45.5 46.5 1283 hthe IntCall3 calibration curve (Bronk Ramalysis; thus	Top Bottom Centered core core composite Carbon depth depth depth mass (cm) (cm) (µg) 54 55.5 1176.1 95 54 55.5 1176.1 22 79 80 1200.8 35 79 80 1200.8 35 6 1242.5 49 5 6 1242.5 49 55 6 1242.5 72 5 6 1242.5 49 5 6 1242.5 72 5 6 1242.5 45 5 45.5 46.5 1283 34 4 45.5 46.5 1283 55 55 504 55 55 56 1242.5 504 55 55 56 1243.3 34 34 34 35 34 35 34 35 34 34 35 34 35 34	TopBottomCenteredcorecorecompositeCarbondepthdepthmassGraphite/(cm)(cm)(cm)(μ g)gas5455.51176.195Gas79801200.835Gas79801200.842Gas5561242.549Gas561242.572Gas561242.545Gas561242.5504Graphite61242.545Gas7946.512833461242.5504Graphite61242.545Gas61242.545Gas61242.545Gas746.5128334Gas45.546.5128374Gas45.546.51283143Graphite45.546.51283143Graphite45.546.51283143Graphiteh the IntCall 3 calibration curve (Bronk Ramsey, 2009; Reimer et al. ζ 1283143	Top Bottom Centered ^{14}C core core composite Carbon ^{14}C depth depth mass Graphite/ age (cm) (cm) (ug) gas (BP) 54 55.5 1176.1 95 Gas 4850 ± 104 79 80 1200.8 35 Gas 5081 ± 228 79 80 1200.8 42 Gas 5081 ± 228 79 80 1200.8 411 Graphite 5197 ± 86 5 6 1242.5 49 Gas 5061 ± 125 5 6 1242.5 49 Gas 5294 ± 107 5 6 1242.5 504 Graphite 5197 ± 86 6 1242.5 45 Gas 5294 ± 107 5 6 1242.5 504 Graphite 5197 ± 86 6 1242.5 504 Gas 5294 ± 107 128 540.5	Top Bottom Centered ^{14}C Calibrated core core cormposite Carbon ^{14}C Calibrated depth depth mass Graphite/ age age 54 55.5 1176.1 95 Gas 4850 \pm 104 5321–5887 79 80 1200.8 35 Gas 5081 \pm 222 5485–6536 79 80 1200.8 35 Gas 5081 \pm 228 5320–6315 79 80 1200.8 311 Graphite 5197 \pm 86 5745–6190 5 6 1242.5 49 Gas 5061 \pm 122 6032–6718 5 6 1242.5 72 Gas 5204 \pm 107 5768–6300 5 6 1242.5 504 Graphite 5197 \pm 86 5745–6190 5 6 1242.5 504 Graphite 501 \pm 127 5920–6439 6 1242.5 504 Graphite 5402	$ \begin{array}{llllllllllllllllllllllllllllllllllll$



Table 1. Continued



Figure 3. Offsets between median calibrated ${}^{14}C$ ages and the bestage estimate from the OxCal V sequence. Data are grouped by material type. Higher values indicate that the sample age is older than the best-age estimate.

we find the model fit acceptable as all 48 ¹⁴C ages overlap with the median output of the V sequence. We use the V sequence as a best-age estimate for subsequent data comparisons and analyses. Alternative methods of linking the floating varve count with ¹⁴C ages confirm that the ¹⁴C ages are consistent with the varve count results (Fig. 4). When the varve count is tied to the combined radiocarbon ages at the uppermost dated level (732.5 cm), we find that all other radiocarbon ages overlap with the varve count when considering the uncertainty of the varve count. If least-squares minimization is used to minimize the offset between all radiocarbon ages and the varve count, we again find that all radiocarbon ages overlap with the master varve count (without considering varve count uncertainty). The result from the least-squares minimization technique is highly similar to the OxCal V-sequence output.

To test the reliability of gas-source ages versus graphitized ages we created three OxCal P sequences using (1) all ¹⁴C ages, (2) only graphitized ages, and (3) only gas-source ages. The results of all three of these age–depth models agree well with the best-age estimate of the V sequence, although with larger 95 % CIs (Fig. 2). The agreement index was greater than the acceptable value of 60 for all three models overall and for each dated depth within all three models. The P sequence using all ¹⁴C ages spans 4838 ± 235 years, which is slightly greater than, but overlapping with, the total number of varves counted (the V-sequence estimates 4681 ± 79 years in the section). There is no clear bias observed in the age–depth models produced using either the gas-source or graphi-

Graphite µg C

200 400

600

à

0 10

50

 \bigcirc

Gas

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Figure 4. All radiocarbon ages and their 95 % calibrated uncertainties plotted with the varve count results. The gray bands show the varve count tied to the combined calibrated age of the uppermost 14 C ages (at 732.5 cm) with dark gray representing the uncertainty calculated from the three replicated varve counts and light gray representing the uncertainty of the tie point. Dashed green is the varve count fit to the 14 C ages using least-squares minimization of the offset between the varve age and the combined 14 C ages at each sampled depth.

tized samples. The P-sequence outputs clearly show that a very precise age can narrowly constrain the age-model uncertainty at the depth of that sample; however, if dating density is low, the uncertainty related to interpolation between ages becomes large. Despite the lower precision of the gassource ages, the model based on only gas-source ages actually has a lower mean CI width than the model with graphitized ages (mean 95% CI width: 373 years for the gassource model, 438 years for the graphitized model). However, a direct comparison between the gas-source-only and the graphitized-only age models is confounded by differences in the number and spacing of samples. Specifically, there are no graphitized ages between the top of the section (724 cm) and 811 cm and between 1082 and 1200 cm, which

results in a wide CI in these sections. On the other hand, uncertainty is reduced compared to the gas-source model in the depths adjacent to the graphitized ages due to higher precision such that 40% of the section (in terms of depth) has lower age uncertainty in the graphitized model.

3.3 Age-depth model simulations

Nine different sampling scenarios (described in Sect. 2.3) were simulated to test the effects of dating density and analytical precision on age-depth model confidence intervals. For each of the nine scenarios, sets of ¹⁴C ages were simulated 30 times to create an ensemble of age-depth models for each scenario. One set of these simulated age-depth models is shown in Fig. 5, and an animation of the full set of simulated models is available online (File S3). The age-depth models were evaluated for their precision (mean width of the 95 % CI) and accuracy (the mean absolute deviation from the best-age estimate; summarized in Fig. 6 and Table 2). As expected, we find that increased dating density and increased sample masses improve both the accuracy and precision of the age-depth models. It is notable that increasing the number of ages can compensate for the greater uncertainty associated with smaller sample sizes. For instance, the mean CI of age-depth models based on ten 90 µg C samples is narrower than age-depth models with five 500 µg C samples (Table 2). However, the effect of analytical precision is greater on the mean absolute deviation from the best-age estimate. Increased dating density does tend to reduce the deviation from the best-age estimate (especially if the ages are imprecise), but the three scenarios that use 500 µg samples perform better than all other scenarios, in terms of deviation from the best-age estimate, regardless of the sampling density. Additionally, increased dating density does not improve the deviation from the best-age estimate for the 500 µg sample scenarios. This result may be due to the relatively constant sedimentation rates in our sedimentary sequence, which reduces errors caused by interpolation in scenarios with low dating density. Another prominent pattern in the simulations is the large spread of performance for models with relatively few and imprecise ages (Fig. 6). Increasing the number of samples and, especially, the mass of samples has a large impact on the agreement among the different iterations of each scenario.

An additional measure of age-model quality is the Chron Score rating system (Sundqvist et al., 2014), which does not assess age-depth model fit; rather it assesses the quality of inputs used to generate an age-depth model. Thus the Chron Score provides an assessment of the nine sampling scenarios that is independent of the choice of age-depth modeling software or parameter selection during age-depth model construction. The Chron Score is calculated from three criteria used to assess the reliability of core chronologies: (1) delineation of downcore trend (D), (2) quality of dated materials (Q), and (3) precision of calibrated ages (P). These met-



Figure 5. Results of age–model simulations to test the effects of sampling density and sample mass on age–model results. Each panel shows the output of an OxCal P sequence using simulated ¹⁴C ages as inputs compared with the best-age estimate from the V sequence (shown in red). Simulated ¹⁴C ages are based on the decalibrated best-age estimate of a given depth and the expected uncertainty associated with the mass C in the simulated ¹⁴C age, which defines not only the age uncertainty but also a random error term added to each simulated age. Plots show one ensemble member out of 30 simulations. An animation of all 30 simulations can be found in File S3.

rics are combined using a reproducible formula to provide a Chron Score (G) in which higher values represent more reliable chronologies:

$$G = -w_D D + w_Q Q + w_P P. (1)$$

We used the default weighting parameters (w_D , w_Q , and $w_P = 0.001$, 1 and 200) for each component of the Chron Score formula as described in Sundqvist et al. (2014). The quality (Q) parameter depends on two factors – the proportion of ages which are not rejected or reversed (i.e., an older age stratigraphically above a younger age) and a qualitative classification scheme for material types. We modified the threshold for determining if an age is considered a reversal such that if a ¹⁴C age is older than a stratigraphically higher age by more than the age uncertainty (1σ), the age is considered to be stratigraphically reversed. This is different from the default setting, which is 100 years. For the material type classification (m), the simulated age models were assigned the value 4, which is the value assigned to chronologies based on terrestrial macrofossils. For more details on the Chron Score calculation, see Sundqvist et al. (2014). The mean Chron Scores for the simulated age models (Table 2) show that doubling dating density substantially improves the Chron Score, but the effect is greater when moving from 5 to 10 ages than from 10 to 20 ages. The effect of increased precision on the Chron Score is also substantial; it is essentially defined by the Chron Score formula, in which precision is assessed as $P = s^{-1}$, where s is the mean 95 % range of all calibrated ¹⁴C ages. The effect of precision on the Chron Score is also determined by the weighting factors mentioned above. **Table 2.** Table summarizing the effect of dating density (number of ages) and analytical precision (sample mass) on the accuracy, precision, and reliability of OxCal P-sequence models generated from simulated ¹⁴C ages. Each of the nine scenarios was simulated 30 times; presented values are the mean of the 30-member ensemble. Precision is assessed by the mean width of the age–depth model 95 % confidence interval. Accuracy is measured by the mean absolute deviation from the OxCal V-sequence best-age estimate, which is the reference from which ¹⁴C ages were simulated. Chron Score is a metric designed to assessing the reliability of age–depth models, where higher numbers represent greater reliability (Sundqvist et al., 2014).

Sample	Expected Expected		Number of ages in model			
mass	uncertainty	uncertainty $(\mathbf{F}^{14}\mathbf{C})$	5 ages	10 ages	20 ages	
(µg)	(yı)	(I ⁺ C)	(1.07 pci kyi)	(2.14 pci kyi)	(4.27 pci kyi)	
			N	Mean 95 % CI width	h (yr)	
35	±148	± 0.011	633	527	433	
90	±92	± 0.007	577	430	335	
500	±39	± 0.003	524	325	219	
			Mean absolute	deviation from Ox	Cal V sequence (yr)	
35	±148	± 0.011	144	99	78	
90	±92	± 0.007	98	64	65	
500	±39	± 0.003	42	40	49	
			Chron Score			
35	±148	± 0.011	2.46	3.14	3.48	
90	±92	± 0.007	2.87	3.64	4.09	
500	±39	± 0.003	3.92	4.74	5.18	

* Expected age uncertainty for an approximately 4000-year-old sample used to inform age-depth model simulations.

4 Discussion

4.1 Radiocarbon measurements

The results of our ¹⁴C measurements from repeated sampling of single stratigraphic levels provide useful information for other researchers working with miniature ¹⁴C analyses or any ¹⁴C samples from lake sediments. We show that there is an exponential relationship between sample mass and the resulting analytical uncertainty (Fig. 1). We use the relationship shown in Fig. 1a to define the age uncertainty of our simulated ages; however it is important to note that this relationship is only valid for samples with a similar age to the samples in this study (approx. 2000-7000 cal BP). Older samples will yield greater age uncertainty for the same mass of C due to fewer ¹⁴C isotopes (Gottschalk et al., 2018). The measurement uncertainty in F¹⁴C units is not affected by age (Fig. 1b). The exact parameters of these relationships will also depend on laboratory conditions; however, the general shape of the relationship is valid. These data can inform researchers about the expected range of uncertainty for ¹⁴C ages from samples of a given size. We find that samples larger than 40 µg C yield ages that are precise enough to be useful for dating Holocene lake sediments in most applications, and even smaller samples can provide useful ages if no other material is available.

It is well documented that ¹⁴C ages can be susceptible to sources of error that are not included within the analytical un-

certainty of the measurements. Such errors can be due to lab contamination, sample material which is subject to reservoir effects (i.e., bulk sediments or aquatic organic matter; Groot et al., 2014; MacDonald et al., 1991; Tornqvist et al., 1992), or depositional lags (terrestrial organic material, which is older than the sediments surrounding it; Bonk et al., 2015a; Howarth et al., 2013; Krawiec et al., 2013). Errors related to reservoir effects can be avoided by selecting only terrestrial plant material for dating (Oswald et al., 2005). Floating or shoreline vegetation should also be avoided as these plants may uptake CO₂ released by lake degassing (Hatté and Jull, 2015). Dating fragile material such as leaves (as opposed to wood) may reduce the chances of dating reworked material with a depositional lag, but generally this source of error is challenging to predict and depends on the characteristics of each lake's depositional system. To identify ages affected by depositional lags, it is necessary to compare with other age information. Consequently, the identification of outlying ages is facilitated by increased dating density.

In our dataset, multiple ¹⁴C measurements were performed on material taken from a single layer, which enables outlier detection. We find that the scatter of ¹⁴C ages obtained from the same depths is generally consistent with what would be expected based on the analytical uncertainties of the ages. There are no clear outliers in the data; every single ¹⁴C age has a calibrated 95 % CI that overlaps with the median of our best-age estimate OxCal V sequence (and this result is con-



Figure 6. (a) Boxplots showing the distribution of the mean 95 % confidence interval widths produced by simulated age–depth models. Results are grouped by dating density along the *x* axis, and by sample mass (smaller mass equals greater uncertainty) using different colors. Each boxplot represents the distribution of results produced for 30 unique sets of simulated ¹⁴C samples. Data points that are greater (less) than the 75th (25th) percentile plus (minus) 1.5 times the interquartile range are plotted as single points beyond the extent of the whiskers. (b) Same as (a), but showing the mean absolute deviation from the best-age estimate (median output of OxCal V sequence).

firmed by alternative methods of linking the varve count to 14 C ages). This agreement between the varve count and the 14 C ages is evidence that no age in this dataset is incongruent with the other available chronological information (other 14 C ages and varve counts). This notion is further demonstrated by the fact that 10 of 11 sampled levels from which we obtained three or more ages returned an MSWD within the 95 % confidence threshold for testing age scatter (see Sect. 3.1; Reiners et al., 2017). This test is typically used for repeated measurements on the same sample material; however, in our study, many of the measurements from within a single sediment slice are from material that has different true ages. The MSWD test indicates that the variability in ages among samples from within a single sediment slice can reasonably be expected given the analytical uncertainty. However, in this

study, no more than five samples were measured per depth, and thus the range of acceptable values for the MSWD is relatively wide due to the small number of degrees of freedom. Additionally, the analytical uncertainties are relatively large for the gas-source samples, allowing for wide scatter in the data without exceeding the MSWD critical value. Despite these caveats, the consistency between the variability among ages from one level and the analytical uncertainties allows us to make two important conclusions. (1) The analytical precision estimates are reasonable, even for miniature gas-source samples. (2) When material is carefully selected and taxonomically identified for dating, the sources of error that are not considered in the analytical uncertainty (e.g., contamination or depositional lags) are relatively minor in our case study. However, this second conclusion is highly dependent on the sediment transport and depositional processes, which are site specific. Depositional lags still likely have some impact on our chronology. Six ¹⁴C ages from plant material collected from the Lake Żabińskie catchment in 2015 yielded a range of ages from 1978 to 2014 CE (Bonk et al., 2015a) suggesting that the assumption that ¹⁴C ages represent the age of the sediments surrounding macrofossils is often invalid. The scale of these age offsets is likely on the scale of a few decades for Lake Żabińskie sediments, which is inconsequential for many radiocarbon-based chronologies but is the same order of magnitude as the uncertainty of our best-age estimate from the OxCal V sequence and should be considered when reporting or interpreting radiocarbon-based age determinations with very high precision.

The lack of outliers in our dataset is an apparent contrast with the findings of Bonk et al. (2015)a, who report that 17 of 32 radiocarbon samples taken from the uppermost 1000 years of the Lake Żabińskie core were outliers. The outlying ages were older than expected based on the varve chronology, and this offset was attributed to reworking of terrestrial plant material. The identification of outliers did not take into account uncertainties of the radiocarbon calibration curve and varve counts, which could explain some of the differences between the ¹⁴C and the varve ages. Still, 8 of 32 ages reported by Bonk et al. (2015a) have calibrated 2σ age ranges that do not overlap with varve count age (including the varve count uncertainty). The higher outlier frequency in the Bonk et al. (2015a) data might be explained by their generally more precise ages and the fact that their varve count is truly independent of the ¹⁴C ages.

Additionally, our dataset allows us to compare the results of ¹⁴C ages obtained from different types of macrofossil materials, which we grouped into the following categories: leaves (including associated twigs), needles, seeds, periderm, woody scales, and samples containing mixed material types (Fig. 3). When comparing the calibrated median age of each sample to the median of our best-age estimate, we find that the difference between the age offsets of the different material types is not significant at the $\alpha = 0.05$ level (ANOVA, F = 2.127, p = 0.08). This is likely due to our selective screening of sample material, which only includes terrestrial plant material while avoiding aquatic insect remains or possible aquatic plant material, as well as the relatively small number of samples within each material type. There does appear to be a tendency for seeds to produce younger ages, and two of the three woody scale samples yielded ages that are approximately 300 years older than the best-age estimate. This could be due to the superior durability of woody materials compared with other macrofossil materials, which enables wood to be stored on the landscape prior to being deposited in the lake sediments. A larger number of samples would allow for more robust conclusions about the likelihood of certain material types to produce biased ages.

4.2 The OxCal V-sequence best-age estimate

In this study we have tested multiple approaches to assigning absolute ages from ¹⁴C ages to a floating varve count (Fig. 4). Using a single tie point relies on a potentially arbitrary selection of tie-point location and yields large uncertainty intervals when considering both the varve count uncertainty and the uncertainty of calibrated ages. Using least-squares minimization of the offset between all radiocarbon ages and the varve count has the advantage of using all the ¹⁴C ages rather than one tie point; however this approach does not consider varve count uncertainties and does not directly yield an estimate of uncertainty derived from the radiocarbon age uncertainties. The OxCal V sequence is unique in that all age information is integrated into a statistical framework including the probability functions of ¹⁴C ages and the uncertainty associated with the varve count as well. In contrast to the other two approaches, the V sequence can change the total number of years in the sequence compared to the original varve count. However, the addition of 37 years in the V sequence is well within the uncertainty of the varve count (+155/-176). The V-sequence approach is expected to provide more precise and more reliable age estimates than either varve counting or radiocarbon-based age models alone. The resulting age-depth relation has a relatively narrow CI (mean 95 % CI is 86 year). Extremely precise age estimates were also produced using this method for Moossee, Switzerland by Rey et al. (2019). A combination of varve counts and ¹⁴C ages from the Moossee sediments generated a V-sequence output with a mean 95 % CI of 38 years. The higher precision in the Moossee study compared to our V-sequence output is primarily attributed to the higher dating density in Moossee with 27 radiocarbon ages over \sim 3000 years (3.9–7.1 ka) versus our study, which used 48 ages but from only 14 unique depths, over ~ 4700 years. This comparison shows that repeated measurements from the same depth are less useful than analyses from additional depths. This approach to integrating varve counts and ¹⁴C ages could potentially be improved by a better integration of varve count uncertainties into the OxCal program. Currently the uncertainties on age gaps in OxCal are assumed to be normally distributed and cannot be less than 5 years. Nevertheless, the result of the OxCal V sequence is an age–depth model that is much more precise than those constructed only using ¹⁴C ages and provides a useful reference to compare with the ¹⁴C ages. It is important to note that the best-age estimate is not independent of the ¹⁴C ages; it is directly informed by the ¹⁴C ages.

4.3 Age-depth model simulations

The simulated age-depth modeling experiment allows us to assess the effects of dating density and sample mass (expected precision) on the outputs of age-depth models constructed for the section of interest in the Lake Żabińskie sediment core. Models based on relatively few but very precise ages, are tightly constrained at the sample depths, but the CI widens further away from these depths (Fig. 5, File S3). In contrast, models based on a greater sampling density produce confidence intervals with relatively constant width. If models are built using a high density of imprecise ages, the CI of the model output can actually be narrower than the CI of the individual ages. Bayesian age-depth models in particular can take advantage of the stratigraphic order of samples to constrain age-depth models to be more precise than the individual ages that make up the model (Blaauw et al., 2018); however, this is only achievable when dating density is high enough. The results from this experiment suggest that, in the case of the Lake Żabińskie sequence, doubling the number of ages can approximately compensate for an increased analytical uncertainty of 50 years.

The choice of OxCal to produce age-depth models from these hypothetical sampling scenarios may have some influence on the results; however we expect that the key findings are replicable for any Bayesian age-depth model routine (i.e., Bacon or Bchron; Blaauw and Christen, 2011; Haslett and Parnell, 2008). To demonstrate this, we used Bacon (Blaauw and Christen, 2011, 2018) to generate age-depth models for one iteration of the simulated sampling scenarios and compared the results to those generated by OxCal. We find that the Bacon-generated models are highly similar to the OxCal models, and the patterns observed in terms of model precision and accuracy are reasonably similar to those obtained from Oxcal models. The Bacon results can be found in File S4.

The Chron Score results provide a succinct summary of the reliability of the chronologies produced in the different simulated sampling scenarios and is independent of model selection. The Chron Score becomes more sensitive to changes in precision as precision increases, so the difference in the Chron Scores between the 500 and 90 µg scenarios (1 σ uncertainty of ±39 and 92 years, respectively) is greater than the difference between the 90 and 35 µg scenarios (1 σ uncertainty of ±92 and 148 years, respectively). Increased dating density consistently improves the Chron Score results, with a stronger impact seen when shifting from 5 to 10 ages compared to shifting from 10 to 20 ages. The improvement of the Chron Score due to increased dating density is generally consistent for each of the different sample mass scenarios. This differs from the age-depth model statistics where increased dating density has a greater impact on precision in the larger sample mass scenarios (more precise ages). The opposite effect is seen in the mean absolute deviation results, where mean absolute deviation is reduced substantially as dating density increases for the smaller sample scenarios and not at all for the 500 µg scenario. For all measures of chronologic performance, we find a greater improvement when increasing the number of ages from 5 to 10 ages compared to increasing from 10 to 20 ages, suggesting there are some diminishing returns from increased dating density. This result is in accordance with the results of Blaauw et al. (2018). While the Chron Score results are dependent on the parameters chosen for the calculation, they intuitively make sense. Because Chron Score results use only the simulated ¹⁴C ages as input and are unaffected by the age modeling routine, the patterns exhibited in the scores may be more applicable to a variety of sedimentary records.

In real-world applications, there are additional advantages from increasing dating density. Many lacustrine sequences have greater variability in sedimentation rates than the sequence modeled here. More fluctuations in sedimentation rate require a greater number of ages to delineate the changes in sedimentation. Additionally, outlying ages and age scatter beyond analytical uncertainty are not considered in this modeling experiment. In most cases, detecting outlying ages becomes easier as dating density increases. Because this experiment is only applied to a single sedimentary sequence, the results may not be directly applicable for other sedimentary records with different depositional conditions. In the future, this type of age model simulation could be applied to a range of sedimentary sequences with a variety of depositional conditions.

4.4 Recommendations for radiocarbon sampling strategy

Radiocarbon sampling strategies will always be highly dependent on project-specific considerations such as how the chronology will affect the scientific goals of the project, budget and labor constraints, the nature of the sedimentary record in question, and the availability of suitable materials. A goal of this study is to provide data that can inform sampling strategies for building robust chronologies, particularly in cases where suitable material may be limited. Firstly, an iterative approach to ¹⁴C measurements is preferred. An initial batch of measurements should target a low dating density of perhaps one date per 2000 years. Subsequent samples should aim to fill in gaps where age uncertainty remains highest (Blaauw et al., 2018) or where preliminary age-depth trends appear to be non-linear. In accordance with many previous studies (e.g., Howarth et al., 2013; Oswald et al., 2005), we advocate for careful selection of material identified as terrestrial in origin. If the mass of such material is limited, the MICADAS gas source is useful for dating miniature samples, and we are convinced that miniature samples of terrestrial material are preferable to dating questionable material or bulk sediments. Samples as small as a few micrograms of C can be measured using the MICADAS, though samples larger than 40 µg C are recommended for more precise results (mid to late Holocene samples containing 40 µg C are expected to have an analytical uncertainty of \sim 138 years). Dating small amounts of material from single depths is also preferable to pooling material from depth segments that may represent long time intervals. A general rule of thumb is to avoid taking samples with depth intervals representing more time than the expected uncertainty of a ¹⁴C age. To improve the accuracy of age-depth models, a higher priority should be placed on achieving a sufficiently high dating density (ideally greater than one age per 500 years; Blaauw et al., 2018) using narrow sample-depth intervals. In most cases, this goal should be prioritized over the goal of gathering larger sample masses in order to reduce analytical uncertainties. The results of this study and others (e.g., Blaauw et al., 2018; Trachsel and Telford, 2017) clearly indicate that increased sampling density improves the accuracy, precision, and reliability of age-depth models.

Multiple measurements from within a single stratigraphic depth, as we have done in this study, can be useful in sediments where age scatter (possibly from reworked material) is expected. In such cases, multiple measurements from a single depth could allow for the identification of certain types of material that should be avoided. If age scatter is not expected, single measures of pooled macrofossils are more cost-effective than repeat measurements from a single depth.

Although increased dating density does incur greater cost, gas-source ages have lower costs compared to graphitized ages allowing for greater dating density at a similar cost. Injecting CO₂ into the AMS rather than generating graphite and packing a target substantially reduces the effort to analyze a sample following pre-treatment and additionally reduces some chance of contamination during graphitization. These advantages are partly offset by additional operator attention required during gas-source measurements. How these differences translate to per-sample costs depends on the pricing structures implemented in each lab. Cost estimates from two MICADAS labs at the University of Bern and Northern Arizona University range between approximately 15 % and 33 % lower costs for gas-source measurements compared to graphitized samples. The use of smaller samples can also reduce the labor time required to isolate suitable material from the sediment; however, handling and cleaning miniature samples can add additional challenges, which increases labor time.

5 Conclusions

AMS 14 C analysis of Holocene terrestrial plant macrofossils using the MICADAS gas-ion source produces unbiased ages with similar precision compared to graphitized samples that contain a similar mass of carbon (approximately 120–160 µg C).

The precision of a ¹⁴C age can be approximately estimated based on the amount of carbon within a sample. Holocene samples containing greater than 40 μ g C produce ¹⁴C measurements with analytical uncertainty expected to be less than $\pm 0.01 \, F^{14}$ C (150 years for samples than are approximately 4000 years old). Uncertainty increases exponentially as samples get smaller, so 10 μ g C samples are expected to have an uncertainty of $\pm 0.021 \, F^{14}$ C (277 years).

The variability among ages obtained from 1 or 2 cm thick samples in the Lake Żabińskie sediment core is compatible with the variability expected due to analytical uncertainty alone.

We find no clear evidence in our dataset for age bias based on the type of macrofossil material dated, which we limited to terrestrial plant material.

Judging from the output of age–depth models, the lower precision of miniature gas-source ages can be compensated for by increasing sampling density. Based on sets of simulated ¹⁴C ages that mimic the ¹⁴C ages of our study core, together with age–depth models generated using OxCal, doubling dating density roughly compensates for a decrease in analytical precision of 50 years.

The effect of ¹⁴C age precision is among several factors that influence chronological precision. The thickness of the depth interval used to obtain samples, the ability to select identifiable terrestrial materials or to analyze more than one type of material, the reliability of detecting age outliers, and the amount of variability in sedimentation rate all determine the accuracy and precision of an age–depth model, which are both improved by increasing the number of ages.

This study can inform sampling strategies and provide expectations about radiocarbon-based age-depth model outcomes.

Data availability. The key datasets associated with this paper (varve count results and the best-age estimate OxCal V-sequence output) are available at the Bern Open Repository and Information System: https://doi.org/10.7892/boris.134606 (Zander et al., 2019).

Supplement. Supplementary File S1: Core images and location of ¹⁴C ages. Supplementary File S2: Microscope images of macrofossils used for ¹⁴C dating. Supplementary File S3: Animation of OxCal P-sequence age–depth models for all 30 iterations of simulated sampling scenarios (animated version of Fig. 4). Supplementary File S4: Comparison of Bacon and OxCal simulated age–depth models. The supplement related to this article is available online at: https://doi.org/10.5194/gchron-2-63-2020-supplement.

Author contributions. PDZ prepared samples, designed and performed the age modeling experiment, analyzed results, and prepared the paper with contributions from all authors. MG, DSK, SS, and PDZ designed the strategy and goals of the study. MZ, AIP-G, and PDZ performed varve counting. PB-K identified and selected suitable macrofossils. SS oversaw ¹⁴C analyses. DSK assisted with laboratory work.

Competing interests. The authors declare that they have no conflict of interest.

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References

- Barnekow, L., Possnert, G., and Sandgren, P.: AMS ¹⁴C chronologies of Holocene lake sediments in the Abisko area, northern Sweden a comparison between dated bulk sediment and macrofossil samples, GFF, 120, 59–67, https://doi.org/10.1080/11035899801201059, 1998.
- Blaauw, M. and Christen, J. A.: Flexible paleoclimate age-depth models using an autoregressive gamma process, Bayesian Anal., 6, 457–474, https://doi.org/10.1214/11-BA618, 2011.
- Blaauw, M. and Christen, J. A.: rbacon: Age-Depth Modelling using Bayesian Statistics, R package version 2.3.4, available at: https: //CRAN.R-project.org/package=rbacon (last access: 23 March 2020), 1–14, 2018.
- Blaauw, M., Christen, J. A., Bennett, K. D., and Reimer, P. J.: Double the dates and go for Bayes Impacts of model choice, dating density and quality on chronologies, Quaternary Sci. Rev., 188, 58–66, https://doi.org/10.1016/j.quascirev.2018.03.032, 2018.
- Bonk, A., Tylmann, W., Goslar, T., Wacnik, A., and Grosjean, M.: Comparing varve counting and ¹⁴C-Ams chronologies in the sediments of Lake Żabińskie, Northeastern Poland: Implications for accurate ¹⁴C dating of lake sediments, Geochronometria, 42, 157–171, https://doi.org/10.1515/geochr-2015-0019, 2015a.
- Bonk, A., Tylmann, W., Amann, B., Enters, D., and Grosjean, M.: Modern limnology and varve-formation processes in lake Żabińskie, northeastern Poland: Comprehensive process studies as a key to understand the sediment record, J. Limnol., 74, 358– 370, https://doi.org/10.4081/jlimnol.2014.1117, 2015b.
- Bronk Ramsey, C.: Deposition models for chronological records, Quaternary Sci. Rev., 27, 42–60, https://doi.org/10.1016/j.quascirev.2007.01.019, 2008.

- Bronk Ramsey, C.: Bayesian Analysis of Radiocarbon Dates, Radiocarbon, 51, 337–360, https://doi.org/10.1017/s0033822200033865, 2009.
- Bronk Ramsey, C. and Lee, S.: Recent and Planned Developments of the Program OxCal, Radiocarbon, 55, 720–730, https://doi.org/10.1017/s0033822200057878, 2013.
- Butz, C., Grosjean, M., Fischer, D., Wunderle, S., Tylmann, W., and Rein, B.: Hyperspectral imaging spectroscopy: a promising method for the biogeochemical analysis of lake sediments, J. Appl. Remote Sens., 9, 096031, https://doi.org/10.1117/1.jrs.9.096031, 2015.
- Delqué-Količ, E., Comby-Zerbino, C., Ferkane, S., Moreau, C., Dumoulin, J. P., Caffy, I., Souprayen, C., Quilès, A., Bavay, D., Hain, S., and Setti, V.: Preparing and measuring ultra-small radiocarbon samples with the ARTEMIS AMS facility in Saclay, France, Nucl. Instruments Methods Phys. Res. Sect. B, 294, 189– 193, 2013.
- Freeman, E., Skinner, L. C., Reimer, R., Scrivner, A., and Fallon, S.: Graphitization of small carbonate samples for paleoceanographic research at the godwin radiocarbon laboratory, University of Cambridge, Radiocarbon, 58, 89–97, https://doi.org/10.1017/RDC.2015.8, 2016.
- Gottschalk, J., Szidat, S., Michel, E., Mazaud, A., Salazar, G., Battaglia, M., Lippold, J., and Jaccard, S. L.: Radiocarbon Measurements of Small-Size Foraminiferal Samples with the Mini Carbon Dating System (MICADAS) at the University of Bern: Implications for Paleoclimate Reconstructions, Radiocarbon, 60, 469–491, https://doi.org/10.1017/RDC.2018.3, 2018.
- Grimm, E. C., Maher, L. J., and Nelson, D. M.: The magnitude of error in conventional bulk-sediment radiocarbon dates from central North America, Quaternary Res., 72, 301–308, https://doi.org/10.1016/j.yqres.2009.05.006, 2009.
- Groot, M. H. M., van der Plicht, J., Hooghiemstra, H., Lourens, L. J., and Rowe, H. D.: Age modelling for Pleistocene lake sediments: A comparison of methods from the Andean Fúquene Basin (Colombia) case study, Quat. Geochronol., 22, 144–154, https://doi.org/10.1016/j.quageo.2014.01.002, 2014.
- Hajdas, I., Bonani, G., and Goslar, T.: Radiocarbon dating the Holocene in the Gosciaz Lake float-Radiocarbon, 37. 71-74, ing varve chronology, https://doi.org/10.1017/S0033822200014806, 1995.
- Haslett, J. and Parnell, A.: A simple monotone process with application to radiocarbon-dated depth chronologies, J. Roy. Stat. Soc. Ser. C, 57, 399–418, https://doi.org/10.1111/j.1467-9876.2008.00623.x, 2008.
- Hatté, C. and Jull, A. J. T.: ¹⁴C in Plant Macrofossils, in: Encyclopedia of Scientific Dating Methods, edited by: Rink, J. W. and Thompson, J. W., 1–79, Springer Science and Business Media, Dordrecht, 2015.
- Howarth, J. D., Fitzsimons, S. J., Jacobsen, G. E., Vandergoes, M. J., and Norris, R. J.: Identifying a reliable target fraction for radiocarbon dating sedimentary records from lakes, Quat. Geochronol., 17, 68–80, https://doi.org/10.1016/j.quageo.2013.02.001, 2013.
- Krawiec, A. C. L., Kaufman, D. S., and Vaillencourt, D. A.: Age models and tephrostratigraphy from two lakes on Adak Island, Alaska, Quat. Geochronol., 18, 41–53, https://doi.org/10.1016/j.quageo.2013.07.002, 2013.

- Larsson, L.: COORECORDER v2. 3.13: Image Co-ordinate Recording Program, Cybis Elektronik & Data AB, Saltsjöbaden, Sweden, 2003.
- MacDonald, G. M., Beukens, R. P., and Kieser, W. E.: Radiocarbon Dating of Limnic Sediments: A Comparative Analysis and Discussion, Ecology, 72, 1150–1155, https://doi.org/10.2307/1940612, 1991.
- Oswald, W. W., Anderson, P. M., Brown, T. A., Brubaker, L. B., Feng, S. H., Lozhkin, A. V., Tinner, W., and Kaltenrieder, P.: Effects of sample mass and macrofossil type on radiocarbon dating of arctic and boreal lake sediments, Holocene, 15, 758–767, https://doi.org/10.1191/0959683605hl849rr, 2005.
- Reimer, P. J., Bard, E., Bayliss, A., Beck, J. W., Blackwell, P. G., Ramsey, C. B., Buck, C. E., Cheng, H., Edwards, R. L., Friedrich, M., Grootes, P. M., Guilderson, T. P., Haflidason, H., Hajdas, I., Hatté, C., Heaton, T. J., Hoffmann, D. L., Hogg, A. G., Hughen, K. A., Kaiser, K. F., Kromer, B., Manning, S. W., Niu, M., Reimer, R. W., Richards, D. A., Scott, E. M., Southon, J. R., Staff, R. A., Turney, C. S. M., and van der Plicht, J.: IntCal13 and Marine13 Radiocarbon Age Calibration Curves 0–50,000 Years cal BP, Radiocarbon, 55, 1869–1887, https://doi.org/10.2458/azu_js_rc.55.16947, 2013.
- Reiners, P. W., Carlson, R. W., Renne, P. R., Cooper, K. M., Granger, D. E., McLean, N. M., and Schoene, B.: Geochronology and thermochronology, Wiley Blackwell, Hoboken, NJ, USA, p. 480, 2017.
- Rey, F., Gobet, E., Szidat, S., Lotter, A. F., Gilli, A., Hafner, A., and Tinner, W.: Radiocarbon wiggle matching on laminated sediments delivers high-precision chronologies, Radiocarbon, 61, 265–285, https://doi.org/10.1017/RDC.2018.47, 2019.
- Ruff, M., Wacker, L., Gäggeler, H. W., Suter, M., Synal, H. A., and Szidat, S.: A gas ion source for radiocarbon measurements at 200 kv, Radiocarbon, 49, 307–314, https://doi.org/10.1017/S0033822200042235, 2007.
- Ruff, M., Szidat, S., Gäggeler, H. W., Suter, M., Synal, H. A., and Wacker, L.: Gaseous radiocarbon measurements of small samples, Nucl. Instruments Methods Phys. Res. Sect. B, 268, 790– 794, https://doi.org/10.1016/j.nimb.2009.10.032, 2010a.
- Ruff, M., Fahrni, S., Gäggeler, H. W., Hajdas, I., Suter, M., Synal, H. A., Szidat, S., and Wacker, L.: On-line radiocarbon measurements of small samples using elemental analyzer and MICADAS gas ion source, Radiocarbon, 52, 1645–1656, https://doi.org/10.1017/S003382220005637X, 2010b.
- Salazar, G., Zhang, Y. L., Agrios, K., and Szidat, S.: Development of a method for fast and automatic radiocarbon measurement of aerosol samples by online coupling of an elemental analyzer with a MICADAS AMS, Nucl. Instruments Methods Phys. Res. Sect. B, 361, 163–167, https://doi.org/10.1016/j.nimb.2015.03.051, 2015.
- Santos, G. M., Southon, J. R., Griffin, S., Beaupre, S. R., and Druffel, E. R. M.: Ultra small-mass AMS ¹⁴C sample preparation and analyses at KCCAMS/UCI Facility, Nucl. Instruments Methods Phys. Res. Sect. B, 259, 293–302, https://doi.org/10.1016/j.nimb.2007.01.172, 2007.
- Shah Walter, S. R., Gagnon, A. R., Roberts, M. L., Mc-Nichol, A. P., Gaylord, M. C. L., and Klein, E.: Ultra-Small Graphitization Reactors for Ultra-Microscale ¹⁴C Analysis at the National Ocean Sciences Accelerator Mass Spec-

trometry (NOSAMS) Facility, Radiocarbon, 57, 109–122, https://doi.org/10.2458/azu_rc.57.18118, 2015.

- Sundqvist, H. S., Kaufman, D. S., McKay, N. P., Balascio, N. L., Briner, J. P., Cwynar, L. C., Sejrup, H. P., Seppä, H., Subetto, D. A., Andrews, J. T., Axford, Y., Bakke, J., Birks, H. J. B., Brooks, S. J., de Vernal, A., Jennings, A. E., Ljungqvist, F. C., Rühland, K. M., Saenger, C., Smol, J. P., and Viau, A. E.: Arctic Holocene proxy climate database – new approaches to assessing geochronological accuracy and encoding climate variables, Clim. Past, 10, 1605–1631, https://doi.org/10.5194/cp-10-1605-2014, 2014.
- Synal, H. A., Stocker, M., and Suter, M.: MICADAS: A new compact radiocarbon AMS system, Nucl. Instruments Methods Phys. Res. Sect. B, 259, 7–13, https://doi.org/10.1016/j.nimb.2007.01.138, 2007.
- Szidat, S., Salazar, G. A., Vogel, E., Battaglia, M., Wacker, L., Synal, H.-A., and Türler, A.: ¹⁴C analysis and sample preparation at the new Bern Laboratory for the Analysis of Radiocarbon with AMS (LARA), Radiocarbon, 56, 561–566, https://doi.org/10.2458/56.17457, 2014.
- Szumański, A.: Objaśnienia do Szczegółowej Mapy Geologicznej Polski, Arkusz Giżycko, (Explanation to the Detailed Geological Map of Poland, Sheet Gizycko (104)), Polish Geological Institute, Warsaw, Poland, 2000.
- Tornqvist, T. E., De Jong, A. F. M., Oosterbaan, W. A., and Van Der Borg, K.: Accurate dating of organic deposits by AMS ¹⁴C measurement of macrofossils, Radiocarbon, 34, 566–577, https://doi.org/10.1017/S0033822200063840, 1992.
- Trachsel, M. and Telford, R. J.: All age-depth models are wrong, but are getting better, Holocene, 27, 860–869, https://doi.org/10.1177/0959683616675939, 2017.
- Tylmann, W., Bonk, A., Goslar, T., Wulf, S., and Grosjean, M.: Calibrating ²¹⁰Pb dating results with varve chronology and independent chronostratigraphic markers: Problems and implications, Quat. Geochronol., 32, 1–10, https://doi.org/10.1016/j.quageo.2015.11.004, 2016.
- Wacker, L., Christl, M., and Synal, H. A.: Bats: A new tool for AMS data reduction, Nucl. Instruments Methods Phys. Res. Sect. B, 268, 976–979, https://doi.org/10.1016/j.nimb.2009.10.078, 2010a.

- Wacker, L., Bonani, G., Friedrich, M., Hajdas, I., Kromer, B., Němec, M., Ruff, M., Suter, M., Synal, H. A., and Vockenhuber, C.: MICADAS: Routine and highprecision radiocarbon dating, Radiocarbon, 52, 252–262, https://doi.org/10.1017/S0033822200045288, 2010b.
- Wacker, L., Fahrni, S. M., Hajdas, I., Molnar, M., Synal, H. A., Szidat, S., and Zhang, Y. L.: A versatile gas interface for routine radiocarbon analysis with a gas ion source, Nucl. Instruments Methods Phys. Res. Sect. B, 294, 315–319, 2013.
- Wacnik, A.: From foraging to farming in the Great Mazurian Lake District: Palynological studies on Lake Miłkowskie sediments, northeast Poland, Veg. Hist. Archaeobot., 18, 187–203, https://doi.org/10.1007/s00334-008-0196-0, 2009.
- Wacnik, A., Tylmann, W., Bonk, A., Goslar, T., Enters, D., Meyer-Jacob, C., and Grosjean, M.: Determining the responses of vegetation to natural processes and human impacts in north-eastern Poland during the last millennium: combined pollen, geochemical and historical data, Veg. Hist. Archaeobot., 25, 479–498, https://doi.org/10.1007/s00334-016-0565-z, 2016.
- Wetzel, R. G., Likens, G. E., Wetzel, R. G., and Likens, G. E.: Lake Basin Characteristics and Morphometry, in: Limnological Analyses, 1–14, Springer, New York, 1991.
- Zander, P. D., Szidat, S., Grosjean, M., Kaufmann, D. S., Boltshauser-Kaltenrieder, P., Żarczyński, M., and Poraj-Górska, A.: Data tables – Lake Zabinskie Geochronology, BORIS, https://doi.org/10.7892/boris.134606, 2019.
- Żarczyński, M., Tylmann, W., and Goslar, T.: Multiple varve chronologies for the last 2000 years from the sediments of Lake Żabińskie (northeastern Poland) Comparison of strategies for varve counting and uncertainty estimations, Quat. Geochronol., 47, 107–119, https://doi.org/10.1016/j.quageo.2018.06.001, 2018.
- Żarczyński, M., Wacnik, A., and Tylmann, W.: Tracing lake mixing and oxygenation regime using the Fe/Mn ratio in varved sediments: 2000 year-long record of human-induced changes from Lake Żabińskie (NE Poland), Sci. Total Environ., 657, 585–596, https://doi.org/10.1016/j.scitotenv.2018.12.078, 2019.