Technical note: Accelerator mass spectrometry of $^{10}$Be and $^{26}$Al at low nuclide concentrations

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Received: 15 October 2021 – Discussion started: 5 November 2021
Revised: 20 April 2022 – Accepted: 11 May 2022 – Published: 7 June 2022

Abstract. Accelerator mass spectrometry (AMS) is currently the standard technique to measure cosmogenic $^{10}$Be and $^{26}$Al concentrations, but the challenge with measuring low nuclide concentrations is to combine high AMS measurement efficiency with low backgrounds. The current standard measurement setup at ANSTO uses the $3^+$ charge state with Ar stripper gas at 6 MV for Be and 4 MV for Al, achieving ion transmission through the accelerator for $^{10}$Be$^{3^+}$ and $^{26}$Al$^{3^+}$ of around 35% and 40%, respectively. Traditionally, $^{26}$Al measurement uncertainties are larger than those for $^{10}$Be. Here, however, we show that $^{26}$Al can be measured to similar precision as $^{10}$Be even for samples with $^{26}$Al/$^{27}$Al ratios in the range of $10^{-15}$, provided that measurement times are sufficiently long. For example, we can achieve uncertainties of 5% for $^{26}$Al/$^{27}$Al ratios around $1 \times 10^{-14}$, typical for samples of late Holocene age or samples with long burial histories. We also provide empirical functions between the isotope ratio and achievable measurement precision, which allow predictive capabilities for future projects and serve as a benchmark for inter-laboratory comparisons. For the smallest signals, not only is understanding the source of $^{10}$Be or $^{26}$Al background events required to select the most appropriate blank correction method but also the impact of the data reduction algorithms on the obtained nuclide concentration becomes pronounced. Here we discuss approaches to background correction and recommend quality assurance practices that guide the most appropriate background correction method. Our sensitivity analysis demonstrates a 30% difference between different background correction methods for samples with $^{26}$Al/$^{27}$Al ratios below $10^{-14}$. Finally, we show that when the measured signal is small and the number of rare isotope counts is also low, differing $^{26}$Al or $^{10}$Be concentrations may be obtained from the same data if alternative data reduction algorithms are used. Differences in the resulting isotope concentration can be 50% or more if only very few ($\lesssim 10$) counts were recorded or about 30% if single measurement is shorter than 10 min. Our study presents a comprehensive method for analysis of cosmogenic $^{10}$Be and $^{26}$Al samples down to isotope concentrations of a few thousand atoms per gram of sample, which opens the door to new and more varied applications of cosmogenic nuclide analysis.

1 Introduction

Cosmogenic nuclides are now routinely applied in the Earth sciences (Schaefer et al., 2022). Over the past three decades, the technique has revolutionised the field of quantitative geomorphology (e.g. Granger and Schaller, 2014; Dixon and Riebe, 2014) and has made important contributions to the reconstruction of glacier chronologies and past climate changes (e.g. Ivy-Ochs and Briner, 2014; Balco, 2019). While cosmogenic $^{10}$Be has been the workhorse for Earth
science applications, $^{26}\text{Al}$ – as part of the $^{26}\text{Al}/^{10}\text{Be}$ nuclide pair – has also been widely applied in studies of burial dating (e.g., Granger, 2006; Balco and Rovey, 2008) and in settings where material has experienced a complex exposure history. The latter includes landforms repeatedly covered by ice (Knudsen and Egholm, 2018, and references therein) and the sediment of large river basins (Fülöp et al., 2020; Wittmann et al., 2020).

Accelerator mass spectrometry (AMS) is currently the standard technique to measure cosmogenic $^{10}\text{Be}$ and $^{26}\text{Al}$ concentrations, and while the majority of routine samples yield $^{10}\text{Be}/^{9}\text{Be}$ or $^{26}\text{Al}/^{27}\text{Al}$ ratios $\sim 10^{-13}$ or above, more recent applications often push the limits of the technique. Examples of such applications, routinely yielding isotope ratios on order of $10^{-14}$–$10^{-15}$, include dating of young glacial deposits (Schaefer et al., 2009), using onshore and offshore bedrock and sediment cores to reconstruct the glaciation histories of polar regions (Bierman et al., 2016; Schaefer et al., 2016; Shakun et al., 2018) or to reconstruct palaeo-erosion rate records (Lenard et al., 2020; Mariotti et al., 2021; Mandel et al., 2021; see also Codilean and Sadler, 2021), estimating coastal cliff retreat rates (Hurst et al., 2016; Swirad et al., 2020) or denudation rates in rapidly uplifting terrain (Derrieux et al., 2014; Siame et al., 2011), dating of old ice (Auer et al., 2009), and search for supernova signatures (Feige et al., 2018). Furthermore, recent refinements to burial dating models (Knudsen et al., 2020) will likely translate into an increase in isochron burial dating applications in the near future. These applications will require accurate and precise determination of $^{26}\text{Al}/^{27}\text{Al}$ ratios that are often close to background values.

The above applications are not only pushing the limits of the technique but also require increased sample numbers. The answer to both challenges at some level is to optimise and improve the AMS measurement efficiency. In this study, we quantify the measurement losses that limit the achievable measurement sensitivity for $^{10}\text{Be}$ and $^{26}\text{Al}$ analyses at ANSTO’s AMS facilities, discuss approaches to background correction for low ratio $^{10}\text{Be}$ and $^{26}\text{Al}$ measurements, and discuss approaches to calculating nuclide concentrations from small numbers of rare isotope counts. Although the data presented here are specific to the setup at ANSTO, the conclusions drawn from these data are more widely applicable.

2 Accelerator mass spectrometry of $^{10}\text{Be}$ and $^{26}\text{Al}$ at ANSTO

The principle behind an AMS measurement, including that of $^{10}\text{Be}$ and $^{26}\text{Al}$, is as follows (e.g., Finkel and Suter, 1993; Fifield, 1999; Synal, 2013): negative ions are extracted from the sample via Cs sputtering (e.g. Middleton, 1983; Southon and Santos, 2007) and after electrostatic and magnetic analysis ions with selected mass to charge ratio are injected into an accelerator. In the accelerator terminal the ions undergo collisions with gas molecules (or a solid foil may also be used) that result in molecule breakup and the injected ions leaving the terminal with a range of charge states. A second electrostatic and magnetic analysis, after the accelerator, is used to select the mass to charge ratio for the final ion detection. Recent important technical improvements in the AMS method are summarised by Synal (2013). In the context of $^{10}\text{Be}$ and $^{26}\text{Al}$, these improvements include:

i. molecular breakup at 1+ charge state (Lee et al., 1984; Suter et al., 1997; Synal et al., 2000);

ii. development of He gas strippers (Lachner et al., 2014; Müller et al., 2015);

iii. development of ion detection methods to suppress $^{10}\text{B}$ interference at low energies (Grajcar et al., 2004, 2007; Müller et al., 2008, 2010);

iv. development of the gas-filled magnet method to enable magnesium suppression for $^{26}\text{Al}$ measurements using AlO$^{-}$ ions (Paul et al., 1989; Arazi et al., 2004; Fifield et al., 2007; Miltenberger et al., 2017).

As a result of the above technical improvements, it is now possible to measure $^{10}\text{Be}$ and $^{26}\text{Al}$ with accelerators that range from a few hundred kV to 10 MV or larger. In general all these varying measurement methods can achieve backgrounds that are sufficient for the majority of routine samples with $^{10}\text{Be}/^{9}\text{Be}$ or $^{26}\text{Al}/^{27}\text{Al}$ ratios $\sim 10^{-13}$ or above, and have led to increased accessibility with a growing number of AMS facilities that are capable of measuring cosmogenic nuclides. However, a challenge is posed by samples with low nuclide concentrations because the losses during the measurement will directly affect the sensitivity and achievable statistical precision.

AMS measurement efficiency is characterised by losses in: (i) ion source, (ii) ion transport, (iii) charge state yields, and (iv) ion detection. Understanding, quantifying, and subsequently minimising these losses will improve the measurement sensitivity and increase the achievable statistical precision for $^{10}\text{Be}$ and $^{26}\text{Al}$ analysis. Typically the largest losses arise from the inefficient negative ionisation in the ion source, with lesser but still significant losses in the transmission of the ions through the accelerator and ion detection.

2.1 Measurement of $^{10}\text{Be}$

Unfortunately beryllium does not form negative ions as readily as carbon, for example, and the achieved ionisation efficiencies for beryllium are much lower. Standard practice is to use molecular BeO$^{-}$ ions for $^{10}\text{Be}$ measurement as they are more prolific than elemental negative beryllium ions (Middleton, 1989). Nevertheless, the highest reported ionisation efficiencies using BeO$^{-}$ are $\sim 3\%$ (Middleton, 1989; Rood et al., 2010; Wilcken et al., 2019), whereas for C$^{-}$ values between 10% and 30% have been reported (Fallon et al., 2007;
Hlavenka et al., 2017; Yokoyama et al., 2010). The poor negative ion yield for Be and Al (see Sect. 2.2) is sometimes taken to be an inherent limitation of the technique, rather than a challenge to be addressed.

There is significant scope for improvement in the performance and operation of negative ion Cs-sputter sources in terms of their stability, consistency, sample consumption, and efficiency. However, this is challenging as some design considerations are somewhat contradictory, e.g. to ensure expedient sample consumption the sputtering rate of the material needs to be high which in turn makes it difficult to keep the source insulators clean. The lack of a well-understood theoretical model for the negative ionisation process further adds to the engineering challenges. Modifications to the source design that improve longevity, stability, optimise the sample consumption, and improve negative ionisation probability are equally important. Practical methods to optimise sample consumption and negative ionisation include: (i) optimising the shape of the sample holder, (ii) changing the position that the sample is loaded in relative to the sample holder, (iii) using different binding materials and amounts relative to the amount of sample material, (iv) optimising the position of the sample within the ion source, and (v) finding the optimal operating conditions for each ion source. Inconveniently, different ion source designs require their own optimisations, and different isotopes are likely to behave differently with the same ion source. For example, the optimal recess depth where the sample is loaded within the sample holder is different between C\textsuperscript{−}, BeO\textsuperscript{−}, and Al\textsuperscript{−} ions (Yokoyama et al., 2010; Auer et al., 2007; Hunt et al., 2006, 2007).

The nature of tandem acceleration is that only a certain fraction of the negative ions that are injected into the accelerator go into the positive charge state that is selected for analysis. This is the second most significant loss in the AMS measurement. Table 1 shows the transmission of the \(^{10}\)Be ions when injected as \(^{9}\)Be\textsuperscript{16}O\textsuperscript{−} for 1+, 2+, and 3+ charge states with Ar and He stripper gases at accelerator voltages that yield maximum transmission for the given charge state and stripper gas. Selecting the most prominent charge state is an advantage but impacts the ion detection as will be discussed below.

The accelerator terminal voltage that is required to reach maximum transmission under equilibrium charge state distributions for both Ar and He are displayed in Table 1, collating measurements on ANSTO’s 1 MV VEGA (Wilcken et al., 2015) and 6 MV SIRIUS (Wilcken et al., 2017) accelerators using BeO\textsuperscript{−} ions. In our case, charge states 1+, 2+, and 3+ are all a viable option given that we have 1 and 6 MV accelerators that can be used for the \(^{10}\)Be measurement. Table 1 shows that charge state losses can be minimised if 1+ or 2+ ions are selected for analysis with maximum transmission being \(\sim 60\%\) with Ar and/or He stripper gases. For 1+, the maximum yield is achieved around 0.5–1 MV (Ar and He), whereas 2+ transmission peaks occur around 3.5–5 MV with Ar but later around 5–6 MV with He. We cannot reach the charge state peak for 3+ either with Ar or He with the maximum 6 MV acceleration voltage, where the measured transmissions are \(\sim 35\%\) and \(\sim 18\%\), respectively.

Currently, our standard measurement setup uses the 3+ charge state with Ar stripper gas at 6 MV accelerator voltage. This is combined with the conventional passive absorber cell method where the interfering \(^{10}\)B ions are stopped within the absorber cell in front of the ion detector whilst \(^{10}\)Be ions pass through (Klein et al., 1982; Raisbeck et al., 1984). The method offers an effective suppression of \(^{10}\)B (see Sect. 3.1) without compromising the measurement efficiency. The measured unnormalised \(^{10}\)Be/\(^{9}\)Be ratio of a standard material is typically between 80\% and 90\% of the reference value, which is the result of transmission differences between \(^{9}\)Be and \(^{10}\)Be and losses during ion detection. Whilst measurements of \(^{10}\)Be/\(^{9}\)Be ratios at the level 10\(^{-16}\) or below are possible (Wilcken et al., 2019), typically the blank samples are in the range from 3 \times 10\(^{-16}\) to 3 \times 10\(^{-15}\). These blank levels do not include any additional boron correction and depend on the carrier used and the sample preparation laboratory where the samples were prepared.

The above measurement setup is preferred over low energy 1+ measurements (Wilcken et al., 2015) because the total measurement efficiency is higher; that is, even though the transmission to 1+ charge state at 1 MV through the accelerator is 60\%, which is nearly double what is achieved to 3+ at 6 MV, the losses in the ion detection to suppress \(^{10}\)B interference in our case mean that the total efficiency is currently a factor of \(\sim 3\) lower when using the 1+ instead of the 3+ method.

Recently it has been demonstrated that the high transmission of 55\% to 2+ at 3 MV can be used for \(^{10}\)Be measurements and backgrounds below 7 \times 10\(^{-16}\) without significant losses in the ion detection efficiency (Steier et al., 2019). In our case we have ion optical losses when running the accelerator around 3–4 MV and reach only around 45\% transmission with Ar, as opposed to 55\% reported by Steier et al. (2019). Alternatively using He stripping the 2+ peak occurs later around 5–6 MV and we observe close to 60\% transmission. However, our stripper design is currently not able to contain He to a sufficient thickness to suppress the molecular interferences and using it for \(^{10}\)Be measurements is not practical. Furthermore, we have not assessed how the suppression of \(^{10}\)B or other interferences compares with our current standard method, and hence will not discuss this approach further.

### 2.2 Measurement of \(^{26}\)Al

Similar to, but worse than, \(^{10}\)Be, low ionisation efficiency is the major challenge for \(^{26}\)Al measurements. For \(^{26}\)Al, one is faced with two options as the measurements can be done by either using Al\textsuperscript{−} or AlO\textsuperscript{−} beams. A distinct advantage of using Al\textsuperscript{−} is that \(^{26}\)Mg does not form stable negative ions and the measurement of \(^{26}\)Al becomes free from isobaric inter-
Table 1. Beam transmission for $^9$Be ions injected as $^9$Be$^{16}$O$^-$ for 1+, 2+, and 3+ charge states at selected accelerator terminal voltages (TV) for Ar and He stripper gases using ANSTO’s VEGA and SIRIUS accelerators.

<table>
<thead>
<tr>
<th>Ion</th>
<th>Ar Transmission (%)</th>
<th>Ar TV (MV)</th>
<th>He Transmission (%)</th>
<th>He TV (MV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^9$Be$^{1+}$</td>
<td>60</td>
<td>0.5–1</td>
<td>60</td>
<td>0.5–1 VEGA</td>
</tr>
<tr>
<td>$^9$Be$^{2+}$</td>
<td>45</td>
<td>3.5–5</td>
<td>58</td>
<td>5–6 SIRIUS</td>
</tr>
<tr>
<td>$^9$Be$^{3+}$</td>
<td>35</td>
<td>6</td>
<td>18</td>
<td>6 SIRIUS</td>
</tr>
</tbody>
</table>

Figures. Unfortunately, the highest reported ionisation efficiencies for Al$^-$ are around 0.2% (Middleton, 1989; Auer et al., 2007; Wilcken et al., 2017). In contrast, the molecular AlO$^-$ beam is typically on the order of 10–20 times higher than Al$^-$, but ion detection of $^{26}$Al requires suppression of the interfering $^{26}$Mg ions that are injected into the accelerator as $^{26}$MgO$^-$.

We use Al$^-$ for the measurement of $^{26}$Al and therefore the challenge almost entirely becomes optimising the ion source performance. Beyond the low ionisation efficiency of Al$^-$, there is the well-known characteristic of ion source output decreasing during the course of a run. An example of this is provided in Fig. 1, which shows traces of $^{27}$Al$^-$ currents as a function of time from cathodes analysed during two separate runs. Traces in grey to black lines show a drastic reduction in output when we returned to them after a break-off ~ 60 h that had been spent on measuring other samples that were part of the same run. When returned to these samples the output dropped to 200–300 nA despite being in the order of 800–1000 nA before the break. In contrast, the second set of samples (shown in shades of blue) analysed during a separate run shows no sign of the output deteriorating during the course of the run. Whilst earlier work by Middleton (1983) showed that higher sputtering voltages yield an increase in Al$^-$ output, we observed that this might be sometimes overshadowed by deterioration in the source output, as with 4.5 kV sputtering voltages (blue profiles) in Fig. 1 the samples performed much more consistently as a function of time than with 6.5 kV sputtering voltages (grey profiles). However, whilst we are confident that the difference in longevity of the source is not simply a matter of quality in target preparation and/or packing, as the feature existed across multiple samples from different sources, we are not suggesting that the increased longevity is solely due to lower sputtering voltage. We cannot control all the parameters, such as the amount of Cs in the source between experiments, and therefore we cannot isolate the cause for the observed improvement in longevity.

The difference in the source stability, as shown in Fig. 1, highlights the reason why it is often difficult to achieve the theoretical efficiency from real samples. Another practical issue that hinders the measurement of $^{26}$Al is that samples typically vary in outputs when compared with standard reference materials. To quantify the latter, Fig. 2 shows histograms of sample outputs relative to the primary standard KN-4-2 (Nishiizumi, 2004) from three different sample preparation laboratories: ANSTO, University of Wollongong (UOW), and CosmIC Laboratories at Imperial College London (IMPERIAL).

Aluminium purification procedures at ANSTO and UOW follow Child et al. (2000), whereas those at CosmIC Laboratories mostly follow Corbett et al. (2016). On average, samples prepared at ANSTO and UOW give outputs that are 60% and 50% of the primary standard, respectively. In contrast, samples prepared at CosmIC Laboratories at Imperial College London give on average 90% of the current of the standards but show the largest spread. Al$_2$O$_3$ is mixed with Ag at 1 : 2 ratio by weight and loaded into Cu cathodes independently at each laboratory. Whilst there are differences.
in how long the samples were measured, we make the first-order approximation that a set of samples from each laboratory would be subject to a similar spread. This allows us to quantify that the small differences in trace elemental composition between samples, or differences in the process of loading the samples, may yield a factor of two differences in outputs.

As in the case of $^{10}\text{Be}$, the second largest contributor to the $^{26}\text{Al}$ measurement inefficiency is the charge state yield. The transmission of $^{26}\text{Al}$ to 1+, 2+, and 3+ charge states with Ar and He stripper gases at accelerator voltages that yield maximum transmission for the given charge state and stripper gas are shown in Table 2. Using Ar stripper gas, maximum transmissions to 1+, 2+, and 3+ charge states are 40%, 48%, and 40% at 0.5, 1, and 4 MV accelerator voltages, respectively. Using He stripping, the maximum measured transmissions to 1+, 2+, and 3+ are 21%, 57%, and 39% at 0.5, 0.5, and 4 MV, respectively.

Our standard measurement setup uses 3+ charge state at 4 MV accelerator voltage with Ar stripper gas (Wilcken et al., 2019). The measured unnormalised $^{26}\text{Al} / ^{27}\text{Al}$ ratio of a standard material is typically around 90% of the reference value, which is due to a combination of transmission differences between $^{26}\text{Al}$ and $^{27}\text{Al}$, and losses in the ion detection. The above method does not utilise the maximum transmission that is achievable with 2+, but the benefit of clean spectra that is free of interferences has, to date, outweighed the losses in transmission. Equal ion optical transmission of about 40% can be achieved with 1+ charge state, but this decreases to about ~30% by the time all the molecular interferences are sufficiently suppressed (Wilcken et al., 2015), and therefore offers no gain over the 3+ method.

The maximum transmission to 2+ is about 60% at 0.5 MV when using He stripper gas. Given the extremely low ionisation efficiency, the possibility to improve the measurement precision with 1.5 times higher count rates, when compared with our standard 3+ method, is significant. However, the challenges with $^{26}\text{Al}^{2+}$ measurement are the interfering $^{13}\text{C}^{2+}$ ions and how to separate these with low ion energies. Whilst the latter has been demonstrated elsewhere (e.g. Müller et al., 2015), we have not assessed the robustness of the method with our accelerator setup and samples from varying lithological settings.

### 2.3 Benchmarks

A simple approach to estimate the overall measurement efficiency is to look at the achieved precision from a suite of $^{10}\text{Be}$ and $^{26}\text{Al}$ samples as shown in Fig. 3. These are minimum efficiency values because the samples are not fully consumed, and consumed to variable degrees. At isotope ratios below $10^{-13}$ the achievable precision becomes dominated by the counting statistics and from there on precision decreases for lower isotope ratios. At higher nuclide concentrations we typically limit the statistical precision to about 2% in measurement sequencing to allocate more time for low ratio samples and to ensure the measurement proceeds expeditiously. Reproducibility of standard reference materials is about 1% for both $^{10}\text{Be}$ and $^{26}\text{Al}$ as has been demonstrated at different AMS laboratories: ANSTO (Wilcken et al., 2017), SUERC (Xu et al., 2015), and LLNL-CAMS (Rood et al., 2013).

Figure 3 demonstrates that it is possible to measure $^{26}\text{Al}$ and $^{10}\text{Be}$ to similar precision even for samples with isotope ratios at ~$10^{-15}$. This is possible for samples with $^{26}\text{Al} / ^{10}\text{Be}$ ratios close to the surface production ratio of 6.75 in quartz (Balco et al., 2008), where the roughly factor of 10 lower ionisation efficiency for $^{10}\text{Be}^{-}$ compared with $^{26}\text{Al}^{-}$ is, for typical chemistry procedures and stable Al concentrations in quartz, in part compensated by a $^{26}\text{Al} / ^{27}\text{Al}$ ratio two to three times higher than the $^{10}\text{Be} / ^{9}\text{Be}$ ratio for the same sample. However, currently the long measurement times required to achieve similar precision as for $^{10}\text{Be}$ (see Fig. 1) reserve
the capability only for a few selected projects, and for most samples the $^{26}$Al measurement precision is lower than for $^{10}$Be, as shown in Fig. 3.

A distinct feature of the $^{26}$Al samples shown in Fig. 3 is that the measurement precision is more variable than for $^{10}$Be and it is possible to see nearly a factor of 10 differences in measurement precision for samples with similar $^{26}$Al/$^{27}$Al ratios. This is a direct consequence of either the variable output from samples as shown earlier in Fig. 2, or of the idiosyncratic behaviour of the ion source during the run as shown in Fig. 1. In contrast, $^{10}$Be behaves much more consistently which is reflected in the tight grouping of the data.

To allow a simple means to estimate achievable precision for future projects, functions have been fitted to the measured $^{10}$Be/$^9$Be and $^{26}$Al/$^{27}$Al data and are given in Fig. 3. The fitted functions were forced to result in measurement precision of about 2% when ratios approach $1 \times 10^{-12}$. This is our routine measurement precision and whilst higher precision is possible for high-ratio samples, it is not pertinent here. The functions given in Fig. 3 are applicable to standard size samples with BeO and Al$_2$O$_3$ masses around 0.6 and 4 mg, respectively.

### 3 Background correction

With small signals, the importance of background correction is clear, and ultimately comes down to the question of when a signal is above background (e.g. Currie, 1968). In AMS, one must employ Poisson statistics which is typically done as Gaussian approximation; however, at a very low number of counts, such approximation does not apply anymore (Currie, 1972; Schmidt et al., 1984; Feldman and Cousins, 1998).

How differing measurement times between sample and blank will impact the lowest minimum detectable quantity has been discussed in Mathews and Gerts (2008), Potter and Strzelczyk (2008, 2011), and Alvarez (2013). However, before any such statistical analysis is undertaken, we argue that it is possible to isolate the most likely source of background by fully characterising the AMS instrument in question with a suite of quality assurance samples. This information, in turn, will be our primary guide for selecting the most appropriate background correction method.

#### 3.1 Background corrections for $^{10}$Be

The measured $^{10}$Be/$^9$Be ratio for an unknown sample and process blank can be approximated as:

$$ R_{10,s} \approx \frac{N_{10,q} + N_{10,c} + N_{10,sp} + N_{10,AMS}}{N_{9,c}^{s}} $$

$$ R_{10,b} \approx \frac{N_{10,c}^{b} + N_{10,sp} + N_{10,AMS}^{b}}{N_{9,c}^{b}} $$

where sub- and superscripts $s$, $q$, $c$, $sp$, and $b$ refer to sample, dissolved quartz, carrier, sample process, and blank, respectively, and $R_{10,s}$ and $R_{10,b}$ are the measured $^{10}$Be/$^9$Be ratios in a sample and process blank, respectively. The number of $^{10}$Be atoms from the dissolved quartz is $N_{10,q}$. To account for potentially different amounts of carrier between samples and blanks these are labelled as $N_{10,c}^{s}$ and $N_{10,c}^{b}$, respectively. Similarly, the $^{10}$Be atoms that might enter the sample or blank during the sample processing are labelled
as $N_{10,sp}^s$ and $N_{10,sp}^b$, respectively. Any $^{10}$Be events that are recorded due to the AMS measurement itself are accounted with $N_{10,AMS}$ and again can be different between sample and blank. $N_{10,AMS}$ encapsulates sample cross talk in the ion source as well as potential interference caused by high $^{10}$B rates. Equations (1) and (2) are based on the assumption that the amount of $^9$Be coming from the dissolved quartz, sample processing, or AMS make negligible contributions as compared with the carrier itself. If these assumptions are not valid, one needs to expand Eqs. (1) and (2) to include the relevant terms, but here we focus on the given approximations as they are valid under regular routine methods. $^{10}$Be/$^9$Be ratios in the sample ($R_{10,s}$) and blank ($R_{10,b}$) are measured and the amounts of carrier added ($N_{9,c}^s$ and $N_{9,c}^b$) are known.

To be able to solve the number of $^{10}$Be atoms from the dissolved quartz from Eqs. (1) and (2), one needs to either make assumptions about, or have external information on, the origin of the background $^{10}$Be events. The first common assumption is that the number of $^{10}$Be atoms that might enter a sample and a blank during sample processing is approximately equal, i.e. $N_{10,sp}^s \approx N_{10,sp}^b$. This is a reasonable assumption in most circumstances as the sample preparation steps for unknown samples and blanks are closely mimicked.

The apparent $^{10}$Be counts observed due to the AMS instrument response ($N_{10,AMS}$) can be treated as equal between samples and blanks ($N_{10,AMS}^s \approx N_{10,AMS}^b$) under the following circumstances: samples and blanks are measured close in time for a similar duration when small source memory contribution can be approximated to be equal, and B rates are below a certain threshold above which the background $^{10}$Be/$^9$Be ratio starts to increase due to increasing interference rate. In Fig. 4, we plot a set of background test samples with artificially elevated boron concentrations (grey circles) along with a representative collection of unknown samples (red circles) in order to illustrate the impact of increasing B rates on measurement background. The $^{10}$B test samples were prepared by adding diluted 1000 ppm B standard solution to crucibles with $^{10}$Be carrier mixture, the solution being subsequently dried down and calcined. As shown in Fig. 4, samples located to the left of the inflection point in $^{10}$B test samples, where the measured $^{10}$Be/$^9$Be ratio starts to increase as a function of increasing interference rate, do not need a separate B correction. In this case, for example, all the unknown samples do not need a correction for B.

A further contribution of $^{10}$Be atoms in the blank is from the $^9$Be carrier itself. This may be quantified by preparing an AMS sample directly from the carrier by conversion of the carrier solution to BeO with minimal handling and measuring it early in the run to avoid source memory build-up. The measurable $^{10}$Be/$^9$Be ratio in the carrier can be written as $R_{10,c} = N_{10,c}/N_{9,c}$.

Now, we may solve the number of $^{10}$Be atoms in the quartz sample by rewriting Eqs. (1) and (2):

$$N_{10,q} = \left[ R_{10,s} - R_{10,c} \right] \times N_{9,c}^s - \left[ R_{10,b} - R_{10,c} \right] \times N_{9,c}^b. \quad (3)$$

The above is the general solution for background correction and requires one to measure both a process blank and a direct carrier blank. An obvious way to simplify the blank correction is to keep the carrier mass equal between a sample and a blank when $N_{9,c}^s$ and $N_{9,c}^b$ become equal. As a consequence the $R_{10,c}$ terms cancel out in Eq. (3) and we obtain:

$$N_{10,q} = \left[ R_{10,s} - R_{10,b} \right] \times N_{9,c}^s. \quad (4)$$

Equation (4) is also reached if the dominant source of $^{10}$Be in the blank samples is the carrier itself, when $R_{10,b}$ approaches $R_{10,c}$ and the second term in Eq. (3) becomes very small. Note also that Eq. (4) is identical to the common background correction method where the number of atoms in the blank are scaled with the masses of the carrier solutions between samples and blank:

$$N_{10,q} = R_{10,s} \times N_{9,c}^s - m_{9,s} \times R_{10,b} \times N_{9,c}^b$$

$$= \left[ R_{10,s} - R_{10,b} \right] \times N_{9,c}^s, \quad (5)$$

where $m_{9,s}$ and $m_{9,b}$ are the masses of carrier solutions added to sample and blank, respectively.

In contrast, if the sample preparation process dominates the $^{10}$Be background, $R_{10,s}$ and $R_{10,b}$ become much larger than $R_{10,c}$ and Eq. (3) may be rewritten as:

$$N_{10,q} \approx R_{10,s} \times N_{9,c}^s - R_{10,b} \times N_{9,c}^b. \quad (6)$$

Here it is noteworthy that when the sample preparation process itself is the dominant source of $^{10}$Be background atoms, the correction does not scale with the mass of the carrier in the sample as shown in Eq. (6). However, the simple practice of keeping the carrier masses equal between samples and blanks makes the blank correction very simple and one does not need to choose between Eqs. (4) and (6) as
they become identical. There may be situations when keeping carrier masses between samples and blanks equal is not desired, however, as the carrier mass is proportional with the longevity of the sample during measurement and carrier masses may be chosen such that predicted $^{10}\text{Be} / ^{9}\text{Be}$ ratios are within a range that does not compromise the measurement.

### 3.2 Background corrections for $^{26}\text{Al}$

Similar to $^{10}\text{Be}$, the measured $^{26}\text{Al} / ^{27}\text{Al}$ ratio for an unknown sample $R_{26,s}$ and process blank $R_{26,b}$, respectively, can be written as:

$$R_{26,s} = \frac{N_{26,q} + N_{26,c} + N_{26,sp} + N_{26,AMS}}{N_{27,q} + N_{27,c}},$$

$$R_{26,b} = \frac{N_{26,c} + N_{26,sp} + N_{26,AMS}}{N_{27,c}},$$

where $N_{26,q}$ is the number of $^{26}\text{Al}$ atoms from the dissolved quartz, and $N_{26,c}$ and $N_{26,sp}$ are the numbers of $^{26}\text{Al}$ atoms from the carrier, if any was used, in the sample and blank, respectively. Additional $^{26}\text{Al}$ atoms that might enter the sample during sample processing are $N_{26,sp}$, and the impact of AMS measurement to the recorded $^{26}\text{Al}$ events is $N_{26,AMS}$. The latter encapsulates cross talk in the ion source as well as any events that might have erroneously been recorded as $^{26}\text{Al}$. As in the case of $^{10}\text{Be}$, contamination during processing or measurement ($N_{26,sp}$ and $N_{26,AMS}$) can be assumed to be equal between sample and blank as long as they are processed and measured in a similar way and there are no clear ion source memory effects or interferences that might be different between the two. The latter is quite a safe assumption when using $\text{Al}^+$ beams and the $3^+$ charge state for the measurement because the $^{26}\text{Al}$ events are so clearly separated from any possible interferences. Equations (7) and (8) assume that possible $^{27}\text{Al}$ contamination is negligible.

If the carrier $^{26}\text{Al} / ^{27}\text{Al}$ ratio ($R_{26,c} = N_{26,c} / N_{27,c}$) is known, we can solve the number of $^{26}\text{Al}$ atoms from the dissolved quartz from Eqs. (7) and (8):

$$N_{26,q} = R_{26,s} \times \left[ N_{27,q} + N_{27,c} \right] - R_{26,c} \times \left[ N_{27,c} - N_{27,c} \right] - R_{26,b} \times N_{27,c}.$$  

This general solution simplifies to a simple blank subtraction if the amounts of carrier added to the sample and blank are equal, in which case the second term drops out of Eq. (9). However, unlike in the case of $^{10}\text{Be}$, the presence of $^{27}\text{Al}$ from the dissolved quartz means that the amounts of carrier added to the sample and blank are often different, and more commonly no carrier is added at all to samples to bolster the $^{26}\text{Al} / ^{27}\text{Al}$ ratio. The above means that measurements of $R_{26,s}$, $R_{26,b}$, and $R_{26,c}$ are required in order to weigh the different sources of backgrounds appropriately.

Unfortunately, $^{26}\text{Al}$ count rates are so low that it is often difficult to obtain a sufficient number of counts to be able to tell different blank samples apart. However, a collection of multiple blank measurements over a longer measurement time period offers higher statistical precision and allows differentiation of various blank samples, as shown in Table 3.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$N$ (total counts)</th>
<th>$^{26}\text{Al}$ rate (counts s$^{-1}$)</th>
<th>$^{26}\text{Al}$ rate (counts s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ag</td>
<td>3</td>
<td>$2 \times 1.29 \times 10^{-4}$</td>
<td>$9.13 \times 10^{-5}$</td>
</tr>
<tr>
<td>Al carrier</td>
<td>5</td>
<td>$22 \times 9.14 \times 10^{-4}$</td>
<td>$1.95 \times 10^{-4}$</td>
</tr>
<tr>
<td>ANSTO</td>
<td>29</td>
<td>$151 \times 2.31 \times 10^{-3}$</td>
<td>$1.88 \times 10^{-4}$</td>
</tr>
<tr>
<td>UOW</td>
<td>25</td>
<td>$91 \times 1.10 \times 10^{-3}$</td>
<td>$1.15 \times 10^{-4}$</td>
</tr>
<tr>
<td>IMPERIAL</td>
<td>22</td>
<td>$118 \times 8.85 \times 10^{-4}$</td>
<td>$8.15 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

On the other hand, one may argue that, because there is no $\text{Al}_2\text{O}_3$ present in the pure $\text{Ag}$ sample, the total output from the ion source is much less than from regular $\text{Al}_2\text{O}_3$ samples and may impact the probability of $^{26}\text{Al}$ ions reaching the detector. Whilst this effect might be true, we believe the impact is within the uncertainties at these extremely low count rates.
than the ICP carrier, indicating an additional source of $^{26}\text{Al}$ in those samples.

A challenge with the general background correction Eq. (9) is that the $^{26}\text{Al} / ^{27}\text{Al}$ ratio in the carrier, $R_{26,c}$, might not be known with sufficient precision to improve the accuracy of the blank correction. Two end-member assumptions can be made to simplify Eq. (9). The first assumption is that the blank is dominated by the inherent $^{26}\text{Al}$ in the carrier, which is the likely scenario for the University of Wollongong and Imperial College London laboratories (see Table 3). In this case, $R_{26,b} \approx R_{26,c}$ and Eq. (9) simplifies to:

$$N_{26,q} \approx R_{26,s} \times \left[N_{27,q} + N_{27,c}^3\right] - R_{26,b} \times N_{27,c}^3.$$  \hspace{1cm} \text{(10)}

The alternative assumption is that the dominant source of contamination is from sample processing. In this case, $R_{26,c}$ becomes small compared with $R_{26,b}$ and Eq. (9) can be written as:

$$N_{26,q} \approx R_{26,s} \times \left[N_{27,q} + N_{27,c}^3\right] - R_{26,b} \times N_{27,c}^b.$$  \hspace{1cm} \text{(11)}

Equations (10) and (11) are similar to Eqs. (4) and (6) for $^{10}\text{Be}$, with the same conclusion that if the carrier itself is the dominant source of $^{26}\text{Al}$ or $^{10}\text{Be}$ atoms in the blank sample, then the background correction is the blank $^{26}\text{Al} / ^{27}\text{Al}$ ratio multiplied by the amount of carrier added to the sample. If no carrier is added to the sample, no blank correction is required. In contrast, if the dominant source of $^{26}\text{Al}$ (or $^{10}\text{Be}$) atoms in the blank is sample processing, the background correction is calculated with the amount of carrier added to the blank.

To demonstrate the impact of different background corrections – i.e. applying Eqs. (9), (10), and (11) – we have corrected a set of samples with $^{26}\text{Al} / ^{27}\text{Al}$ ratios from $1 \times 10^{-15}$ to $1 \times 10^{-13}$ and the three different methods and results are shown in Fig. 5. The shaded area in Fig. 5 highlights the difference between (i) assuming that the source of background is the carrier itself and (ii) assuming that the main source of background is contamination during sample processing, i.e. Eqs. (10) and (11), respectively. General background correction using Eq. (9) is shown with blue circles. Figure 5 demonstrates that for samples with $^{26}\text{Al} / ^{27}\text{Al}$ ratios above $1 \times 10^{-14}$ the choice of background correction is typically less significant, and all three methods lead to similar correction. In contrast, for samples with $^{26}\text{Al} / ^{27}\text{Al}$ ratios below $1 \times 10^{-14}$, not only can the magnitude of the background correction be similar to or larger than the measurement uncertainty (see Fig. 3), but also it can differ by up to 30% depending on which correction scheme is used. Therefore, knowing which correction method is the most applicable to each case is highly pertinent for low ratio $^{26}\text{Al}$ measurements.

The above sensitivity analysis differs philosophically from common approaches where varying blank values, e.g. the long-term mean or median, are subtracted to account for the effect of spurious high blank values (e.g. Corbett et al., 2017). Our approach addresses the uncertainty in the origin of the background events by using different correction methods. Using both approaches is recommended.

4 Calculating isotope ratios

During an AMS measurement, a sample is typically measured between 3 and 10 times for a few minutes each, where the number of repetitions and length of each measurement may vary depending on the AMS laboratory. These multiple measurements are then converted to a final result with an uncertainty that is either based on the number of rare isotope counts or that is spread between individual measurements (Elmore et al., 1984; Wacker et al., 2010). However, when the measured signal is small and the number of rare isotope counts is also low, the final result becomes sensitive to how the uncertainty is defined and how the individual measurements are combined. For more information on how to calculate an uncertainty when the number of counts are low, the reader is referred to earlier works (e.g. Currie, 1972; Schmidt et al., 1984; Feldman and Cousins, 1998).

To demonstrate the impact of different algorithms for calculating the final ratios and to validate our method, we show a sensitivity analysis based on a couple of low ratio $^{26}\text{Al}$ samples. We selected five $^{26}\text{Al}$ samples that were each measured ~ 100 min during which 4–83 counts were recorded with an average $^{27}\text{Al}^{-}$ current of 200–300 nA. To combine individual measurements to a final ratio, one may either sum the total counts and charge before calculating the final ratio or one may calculate a weighted mean from the individual measurement ratios. Whilst the former process is independent of measurement sequence, the latter is easier to normalise for drifts in the spectrometer and is our preferred approach. To calculate weighted mean

$$R = \frac{\sum w_i R_i}{\sum w_i},$$  \hspace{1cm} \text{(12)}
Table 4. Relative uncertainties used in the sensitivity analysis when the number of rare isotope counts is low, based on Schmidt et al. (1984).

<table>
<thead>
<tr>
<th>( N_i )</th>
<th>( X_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.84</td>
</tr>
<tr>
<td>1</td>
<td>2.30</td>
</tr>
<tr>
<td>2</td>
<td>1.32</td>
</tr>
<tr>
<td>( 2 &lt; N_i &lt; 10 )</td>
<td>( (1 + \sqrt{N_i})/N_i )</td>
</tr>
<tr>
<td>( N_i \geq 10 )</td>
<td>( 1/\sqrt{N_i} )</td>
</tr>
</tbody>
</table>

where \( w_i \) is the weighting factor, \( r_i \) is the single isotope ratio measurement, and \( R \) is the final ratio, for example Bevington and Robinson (2003), the following weighting factors are considered:

i. Equal weights, where \( w_i = 1 \) and the final ratio is a simple arithmetic mean of the individual measurements;

ii. Integrated current, where the weighting factor is the average \( ^{27} \text{Al} \) current multiplied by measurement time;

iii. Uncertainty, where \( w_i = 1/\sigma_A^2 \), and \( \sigma_A = r_i X_i \), with \( r_i \) being the measured ratio and relative uncertainty \( X_i \) is assigned based on the number of \( ^{26} \text{Al} \) counts \( N_i \) during that run as shown in Table 4;

iv. Normal uncertainty, where \( w_i = 1/\sigma_B^2 \), and \( \sigma_B = r_i / \sqrt{N_i} \), with \( r_i \) and \( N_i \) being the measured ratio and number of \( ^{26} \text{Al} \) counts during that run, respectively.

Using the above weighting factors, we calculate the weighted mean of individual measurement ratios as a function of a single measurement duration for the selected five low ratio samples as shown in Fig. 6. Single measurement durations from 30 s to \( \sim 100 \) min were considered. To obtain non-zero weighting factors when these are based on uncertainties, one count was assumed in cases where none were recorded.

Our sensitivity analysis (Fig. 6) demonstrates that the measured \( ^{26} \text{Al} / ^{27} \text{Al} \) ratio is dependent on the duration of the measurement if the arithmetic mean or uncertainty based weighting factors are used to calculate the mean. Increasing the duration of a measurement will alleviate the differences until all the results converge to a single value that corresponds to a scenario where all the data for a sample were collected during one measurement. Differences in the measured \( ^{26} \text{Al} / ^{27} \text{Al} \) ratio and resulting isotope concentration can be 50% or more if only very few \( \lessapprox 10 \) counts were recorded or about 30% if a single measurement is shorter than 10 min. In contrast, if the integrated \( ^{27} \text{Al} \) current is used to calculate the weighted mean, the final \( ^{26} \text{Al} / ^{27} \text{Al} \) ratio and subsequent nuclide concentration is independent of the measurement duration, as shown in Fig. 6.

To ensure that our results are independent of the measurement sequence, which is arbitrary in our case, our standard method is to calculate the final isotope ratio by weighing the individual measurements with the integrated current as described in Wacker et al. (2010). However, as illustrated by our analysis, differing \( ^{26} \text{Al} \) (or \( ^{10} \text{Be} \)) concentrations may be obtained from the same data if alternate data reduction algorithms are used.

5 Conclusions

The challenge with measuring low \( ^{10} \text{Be} \) or \( ^{26} \text{Al} \) nuclide concentrations is to combine high AMS measurement efficiency with low backgrounds. Achieving an increase in ionisation efficiency will not help if losses elsewhere in the instru-
rection. Our simple sensitivity analysis has shown that when background events dictates the most appropriate blank correction between samples and blanks, and the dominant source of the most appropriate correction method. For the background events is an important factor in deciding the whether batch specific or long-term average, as the origin of the process blanks should not be done purely on the basis of process blanks, concentration can be 50% or more if only very few (5%–50%). In both cases, using the 2+ charge state would increase ion transmission to around 60%, but whether this gain can be harnessed with equal or better backgrounds remains to be assessed. Using our measurement setup, we show that 26Al can be measured to similar precision as 10Be even for samples with 26Al/27Al ratios in the range of 10^{-15}, provided that measurement times are sufficiently long. For example, for an early Holocene sample with 10Be/9Be and 26Al/27Al ratios on the order of 5 × 10^{-14} we would expect the uncertainties to be around 3%–5%, whereas for a late Holocene sample with 10Be/9Be and 26Al/27Al ratios of ∼5 × 10^{-15} we would expect the uncertainties to be in the range of 8%–20%.

With low 10Be/9Be or 26Al/27Al ratios, the importance of background correction is obvious. However, this correction should not be done purely on the basis of process blanks, whether batch specific or long-term average, as the origin of the background events is an important factor in deciding the most appropriate correction method. For 26Al, for example, it is often not feasible to keep the mass of the carrier equal between samples and blanks, and the dominant source of the background events dictates the most appropriate blank correction. Our simple sensitivity analysis has shown that when 26Al/27Al ratios are in the range of (5–10) × 10^{-15}, typical for late Holocene surface exposure dating samples, or for burial dating samples, one can expect 30% differences in blank corrected concentrations and corresponding ages, depending on how blank corrections are done.

When the measured signal is small and the number of rare isotope counts is also low, the calculated final 10Be/9Be or 26Al/27Al ratio becomes sensitive to how the uncertainty is defined and how the individual measurements are combined. Our analysis demonstrates that the measured isotope ratio is dependent on the duration of the measurement, if the arithmetic mean or uncertainty based weighting factors are used to calculate the mean. Differences in the resulting isotope concentration can be 50% or more if only very few (<10) counts were recorded or about 30% if a single measurement is shorter than 10 min. In contrast, if the integrated 9Be or 27Al current is used to calculate the weighted mean – our standard method – the final 10Be/9Be or 26Al/27Al ratio and subsequent nuclide concentration is independent of the measurement duration.

To summarise, our study presents a comprehensive method for analysis of cosmogenic 10Be and 26Al nuclide concentrations. To isolate concentrations of a few thousand atoms per gram of sample, which opens the door to new and more varied applications of cosmogenic nuclide analysis.

Data availability. The data presented in this study are available by contacting the corresponding author.

Author contributions. KMW was responsible for the AMS analyses, ATC and RHF for the sample preparation at University of Wollongong, KS and SK for the sample preparation at ANSTO, and AHR, DHR, and AJS for the sample preparation at Imperial College London. All authors contributed to the writing of the manuscript.

Competing interests. The contact author has declared that neither they nor their co-authors have any competing interests.

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Acknowledgements. We acknowledge the Traditional Custodians of the lands on which we have worked, and their continued spiritual and cultural connection to Country.

Financial support. This research has been supported by the University of Wollongong, Imperial College London, and the Centre for Accelerator Science at ANSTO through the National Collaborative Research Infrastructure Strategy (NCRIS).

Review statement. This paper was edited by Yeong Bae Seong and reviewed by two anonymous referees.

References


Yokoyama, Y., Koizumi, M., Matsuzaki, H., Miyairi, Y., and Ohkouchi, N.: Developing ultra small-scale radiocarbon sample measurement at the University of Tokyo, Radiocarbon, 52, 310–318, 2010.