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# Technical note: Improved calculation of volume, $F_T$ correction, and other derived data for polished zircon (U-Th)/He thermochronology

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**Abstract.** Polishing mounted zircon crystals prior to bulk grain (U-Th)/He thermochronology analysis provides opportunities for characterizing and subsampling each grain via in situ methods to obtain additional information relevant for (U-Th)/He date interpretation and the broader geologic questions of interest. However, polishing introduces complications for classifying grain geometry and determining grain volume (V), on which many derived (U-Th)/He data partially depend. Derived data that depend on volume include isotope concentrations, effective uranium (eU; a proxy for radiation damage), and alpha-ejection correction factors  $(F_T)$ , which are used to correct (U-Th)/He dates. These derived data are integral to interpreting (U-Th)/He dates, and, without a way to accurately calculate these values for polished grains, a choice must be made between polishing zircon to provide robust in situ data at the expense of the thermochronologic data or not polishing and limiting in situ data to grain rims or one-dimensional depth profiles. To address this issue, this paper presents a comprehensive protocol for calculating volume and alpha-ejection surface area for polished zircon grain fragments, from which additional data, including eU and  $F_T$ , are derived. This protocol is implemented after grains have been polished and in situ measurements have been made and can easily be integrated into existing workflows for characterizing and measuring grains for conventional (U-Th)/He analysis. An R script accompanying this paper can be used to perform the required calculations and assign uncertainties during analytical data reduction. Applying the new protocol to a synthetic dataset covering a range of zircon geometries, sizes, and grinding conditions shows that the method is an improvement over existing methods to calculate polished grain  $F_T$ , which only apply to a small subset of possible grain geometries and grinding conditions. The new protocol also calculates all derived data and uncertainties necessary and recommended for (U-Th)/He data reporting, aside from the (U-Th)/He dates themselves, to facilitate integrations with existing data reporting, date interpretation, and thermal history modeling.

### 1 Introduction

(U-Th)/He thermochronology dates and associated data are derived from analytical measurements of parent and daughter isotopes and the volume (V) of the individual mineral grains analyzed. These "derived data" include alpha-ejection correction factors  $(F_T)$ ,  $F_T$ -equivalent spherical radius  $(R_{FT})$ , effective uranium (eU), and parent isotope concentrations, and they are essential for interpreting dates and making other geological inferences.  $F_T$  corrections are applied to account for He lost through alpha-ejection and directly affect the reported (U-Th)/He dates (Farley, 2002). RFT is used to compare grain size and approximate He diffusion domain size in thermal history modeling (Flowers et al., 2022a, b; Ketcham et al., 2011). eU can affect how the thermal history of the grain is interpreted (e.g., Flowers et al., 2022b; Guenthner et al., 2013). Other derived data, such as isotope concentrations, may be used to characterize additional aspects of the samples' geologic history (e.g., sediment recycling history; Dröllner et al., 2022). Accurate V calculation is therefore critically important, as it informs all these other data.

In addition to V dependence,  $F_T$  also depends on another variable related to grain morphology: alpha-ejection surface area, or the surface area of the grain over which alpha particles are ejected (SA $_{\alpha}$ ). Both V and SA $_{\alpha}$  are typically determined for whole crystals by classifying each grain as one of several idealized geometries based on visual inspection and making two-dimensional (2D) measurements of grain size or using three-dimensional imaging methods (Cooperdock et al., 2019; Glotzbach et al., 2019; Ketcham et al., 2011; Reiners et al., 2005; Zeigler et al., 2023, 2024). However, many applications of (U-Th)/He thermochronology, such as detrital zircon applications, benefit from or require mounting and polishing crystals for in situ analyses to characterize chemical zonation, rare earth element abundances, U-Pb or other geochronology data, etc. prior to (U-Th)/He analysis. Grinding and polishing grains to prepare them for additional analysis removes part of the grain, resulting in grain geometries that deviate from the original whole grain and complications for calculating V and  $SA_{\alpha}$  for the remaining fragment. Existing whole-grain methods to calculate V and  $SA_{\alpha}$  (e.g., Farley, 2002; Ketcham et al., 2011; Reiners et al., 2005) are in many cases inapplicable when grains are ground and polished.

Although some previous work has addressed the effect of grinding and polishing on  $F_T$  corrections (He and Reiners, 2022; Marsden et al., 2021; Reiners et al., 2007), these contributions do not address other data derived from volume and surface area and apply to specific cases that do not reflect the full range of real zircon samples or sample preparation. To address the lack of a comprehensive approach to volume-derived data for polished zircon, this contribution presents a protocol and set of equations (Appendix A) coded in an R script (Code availability) that can be integrated with existing workflows for grain characterization and (U-Th)/He thermochronology data reduction and interpretation. Values calculated under this protocol include V,  $SA_{\alpha}$ , volume-to-alpha-ejection-surface-areaequivalent spherical radius  $(R_{SV})$ , mass (M), parent isotope concentrations, eU,  $F_T$ , and  $R_{FT}$ . Results of using the protocol are evaluated using a synthetic dataset encompassing a range of possible grain geometries, sizes, polishing orientations, and grinding depths (Sect. 4, Table S1 in the Supplement) and application to a real detrital zircon dataset (text in the Supplement, Table S2).

## 2 Existing methods and limitations for polished grains

Previous work has addressed the impact of polishing or other means of removing part of the grain on derived data, particularly on  $F_T$  corrections (He and Reiners, 2022; Marsden et al., 2021; Reiners et al., 2007). These contributions have

largely focused on direct comparisons between  $F_T$  corrections for polished grain fragments and  $F_T$  corrections for corresponding whole crystals from which polished grains were derived (Marsden et al., 2021) or focused on a subset of possible polishing scenarios that do not reflect the full range of real zircon samples or sample preparation (He and Reiners, 2022; Reiners et al., 2007). A common approach to simplify  $F_T$  corrections is to polish grains to a plane of symmetry (e.g., halfway through the original c-axis perpendicular width), such that the  $F_T$  value of the fragment is the same as the  $F_T$  value for the entire whole grain (Reiners et al., 2007). However, polishing exactly halfway is often extremely difficult, if not impossible, and inaccuracy in polishing depth can result in  $F_T$  uncertainty greater than  $1\sigma = 5\%$  (Marsden et al., 2021). Alternatively, the same symmetry logic can be applied to crystals broken perpendicular to an axis of symmetry when the true original axis length is unknown (He and Reiners, 2022). The broken interior face of the crystal is treated as a plane of symmetry such that the fragment has the same  $F_T$ as a whole grain with an axis length double the axis length of the fragment. V and  $SA_{\alpha}$  of the fragment can be calculated by dividing the V and  $SA_{\alpha}$  of the reconstructed whole grain in half. Although this approach can be applied to any crystal geometry and plane of symmetry, the He and Reiners protocol is focused on cylindrical grains polished or broken perpendicular to the c axis. For grains polished parallel to the c axis, Reiners et al. (2007) provide a protocol for a limited number of cases: cylindrical and orthorhombic prisms ground and polished to a depth between one alpha-stopping distance and less than half of the original c-axis perpendicular thickness of the crystal.

In reality, zircon encompass a range of morphologies depending on lithology and geologic history beyond what has previously been considered in the literature. Zircon can be approximated as cylinders, ellipsoids, and orthorhombic prisms with or without pyramidal terminations (commonly referred to as "tetragonal" geometries even when a- and baxis measurements are not equivalent). The grinding and polishing orientation of individual crystals can be parallel or perpendicular to the crystallographic c axis, and, because of the natural variation in crystal size, it is common for polishing to remove a variable amount of crystal when multiple crystals are mounted and prepared together (e.g., Fig. 1a). Protocols to determine  $F_T$  corrections and other derived data for polished zircon based on geometry and volume must therefore encompass these different scenarios in order to maximize the number of grains that can be used for analysis in a given sample and grain mount.

### 3 Required measurements, grain classification, and calculation of values

The protocol presented here adapts existing approaches for determining whole-grain V,  $SA_{\alpha}$ , and  $F_T$  for ground and

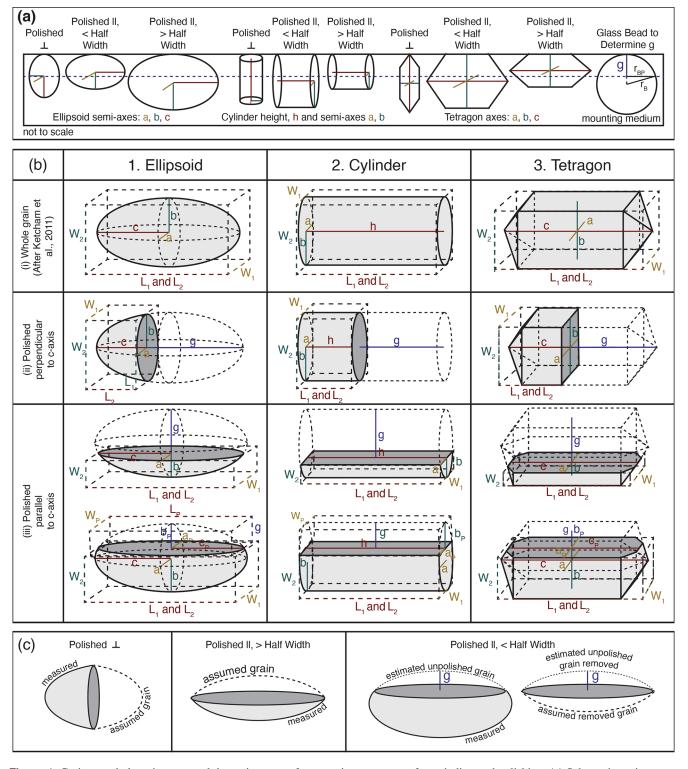


Figure 1. Grain morphology impacts and the assignment of geometric parameters after grinding and polishing. (a) Schematic grain mount showing a variable amount of grain removed depending on original grain geometry, size, and orientation with respect to polishing surface (dashed line). (b) Relationship between 2D grain measurements  $(L_1, L_2, W_1, W_2)$  and geometric parameters (a, b, c, h) for each geometry expressed mathematically in Table 1. (i) Whole grains (after Ketcham et al., 2011). (ii) Grain fragments arising from polishing grains perpendicular to the c axis. (iii) Grain fragments arising from polishing grains parallel to the c axis. In all panels, the light-gray shaded region corresponds to the V calculated. The dark-gray surface is the polished surface not included in  $SA_{\alpha}$ . (c) Illustration of the method to calculate V and  $SA_{\alpha}$  as half of the "assumed grain" or estimate of the removed portion of grain from the estimated whole grain.

polished grain fragments. First, the polished grains are removed from the mounting medium and are inspected and measured using a binocular microscope with a digital camera and microscope imaging software. Grains are classified as ellipsoidal, cylindrical, or "tetragonal" geometries, which can include two, one, or no pyramidal terminations. In order to be classified as cylindrical or tetragonal, the unpolished part of the grain must include visible crystal faces that are unrelated to the polished face. For cylinders, these faces are only perpendicular to the long axis, while, for tetragonal grains, some must be parallel to the long axis (Fig. 1). If there are no observed crystal faces, the grain is classified as an ellipsoid. Like standard approaches for calculating whole-grain V (e.g., Zeigler et al., 2024), two orthogonal sets of length and width measurements  $(L_1, W_1 \text{ and } L_2, W_2)$  parallel to orthogonal crystal axes are made by rotating the grain fragment (Fig. 1b). Polishing orientation is also classified as perpendicular or parallel to the crystallographic c axis based on visual inspection of the grain fragment.

Once grains have been classified and measured, V and  $SA_{\alpha}$  are calculated (Appendix A) by relating grain measurements to the geometric parameters of the relevant geometric classification (a, b, and c semi-axes; a and b semi-axes and height, h; or a, b, and c axes for ellipsoids, cylinders, and tetragons, respectively; Table 1, Fig. 1b). Only external grain surfaces are subject to alpha-ejection; thus the polished surface is not considered to be part of  $SA_{\alpha}$ . In most cases, calculating these values is accomplished by adopting the same approach as He and Reiners (2022) in which the polished grain is treated as a crystal broken along a plane of symmetry such that V and  $SA_{\alpha}$  of the polished fragment are half of a whole "assumed grain" created by reflecting the existing fragment across the plane of polishing (Fig. 1c).  $F_T$  of the fragment is thus equal to  $F_T$  of the assumed grain. This is the approach used for all grains polished perpendicular to the c axis or parallel to the c axis and greater than halfway through the original c-axis perpendicular width of the grain (Fig. 1c), which can be determined by visual inspection of the polished grain and does not require measurements of thickness pre-polishing. For grains polished parallel to the c axis and less than halfway through the original width of the grain (again, determined by visual inspection of the grain postpolishing), a different approach to determining V and  $SA_{\alpha}$ is used. In these cases, the original whole-grain dimensions are estimated by combining the grain measurements with the grinding depth (g) determined by measurements of spherical glass beads mounted and polished alongside the grains. Polishing depth is calculated using Eq. (1) (Pickering et al., 2020) and measurements of the radius of the polished bead surface  $(r_{BP})$  relative to the full bead radius  $(r_B)$  (Fig. 1a).

$$g = r_{\rm B} - \sqrt{r_{\rm B}^2 - r_{\rm BP}^2} \tag{1}$$

Uncertainty on g can be determined through duplicate measurements of multiple embedded beads scattered throughout

the grain mount. The estimated whole-grain dimensions are used to estimate V and  $SA_{\alpha}$  for the whole original grain. To calculate V and  $SA_{\alpha}$  of the remaining fragment, the V and  $SA_{\alpha}$  of the removed portion of the grain are also estimated and subtracted from the estimated whole-grain values. V and  $SA_{\alpha}$  of the removed portion are determined by treating removed portions of the crystals as half crystals of a whole assumed grain in the same manner as grains polished parallel to the c axis and more than halfway through the original grain width (Fig. 1c). This calculation requires additional measurements of the polished grain surface for ellipsoid and cylinder geometries: length  $(L_P)$  and width  $(W_P)$  of the polished face. In practice,  $L_P$  and  $W_P$  are often indistinguishable from  $L_1$ and  $W_1$  for small and medium grains, but, for larger grains, the difference between the polished face and total axis measurements can be much greater.

Volume uncertainty reflects the assumptions made in applying an idealized geometry and human measurement error to imperfect natural zircon and is applied as  $1\sigma = 21\%$  or 13 % for ellipsoid or tetragonal grains, respectively, following recommendations in Zeigler et al. (2024). Volume uncertainty arising from geometric assumptions has not been quantified for cylindrical grains like it has for other geometries (Cooperdock et al., 2019; Zeigler et al., 2023, 2024), so, in the absence of this quantification, the largest quantified uncertainty for zircon from Zeigler et al. (2024),  $1\sigma = 21 \%$ , is applied as a conservative estimate. Future work should establish a quantitative V uncertainty value and correction for cylinders, as this is a common geometry for abraded grains.  $SA_{\alpha}$  uncertainty is unquantified for all geometries. Data that are derived directly from volume ( $R_{SV}$ , mass, parent isotope concentrations, and eU) are calculated using equations in Appendix A and include propagated volume uncertainty and analytical isotope measurement uncertainty when applicable. Like most whole-aliquot (U-Th)/He thermochronology data reduction, the grains are assumed to have homogenous parent isotope concentrations (e.g., no zonation). Deviation from this assumption would impact the calculated dates in similar ways to zonation in whole grains (e.g., Danišík et al., 2017; Hourigan et al., 2005).

 $F_T$  depends not just on volume, but also on  $SA_\alpha$ , which is represented here using the term  $R_{SV}$ , or volume-to-surfacearea equivalent spherical radius, calculated using Eq. (2) as in Ketcham et al. (2011).

$$R_{\rm SV} = \frac{3V}{{\rm SA}_{\alpha}} \tag{2}$$

 $R_{SV}$  serves the same function as the  $\beta$  term introduced by Farley (2002) to relate grain measurements to  $F_T$  via a polynomial function with the general form of Eq. (3).

$$F_T = 1 + a_1 \beta + a_2 \beta^2 + a_3 \beta^3 + \dots$$
 (3)

Polynomial coefficients  $a_1$ ,  $a_2$ ,  $a_3$ , etc. are determined via series of Monte Carlo simulations of variable grains and fitting

 $c = \frac{(L_1 + L_2)}{4}$   $c_p = \frac{L_p}{2}$   $h = \frac{(L_1 + L_2)}{2}$ 

Orientation and depth	Ellipsoid	Cylinder	Tetragon
Perpendicular	$a = \frac{W_1}{2}$	$a = \frac{W_1}{2}$	$a = \min(W_1, W_2)$
to c axis	$b = \frac{(L_1 + W_2)}{4}$	$b = \frac{W_2}{2}$	$b = \max(W_1, W_2)$
	$c = L_2$	$h = \frac{(L_1 + L_2)}{2}$	$c = \frac{(L_1 + L_2)}{2}$
Parallel to	$a = \frac{W_1}{2}$	$a = \frac{W_1}{2}$	$a = \min(W_1, 2W_2)$
c axis,	$b = W_2$	$b = W_2$	$b = \max(W_1, 2W_2)$
> halfway	$c = \frac{(L_1 + L_2)}{4}$	$h = \frac{(L_1 + L_2)}{2}$	$c = \frac{(L_1 + L_2)}{2}$
Parallel to	$a = \frac{W_1}{2}  a_p = \frac{W_p}{2}$	$a = \frac{W_1}{2}  a_p = \frac{W_p}{2}$	$a = \min(W_1, W_2 + g)$ $a_p = \min(W_1, 2g)$
c axis,	$b = \frac{W_2 + g}{2}  b_p = g$	$b = \frac{W_2 + g}{2}  b_p = g$	$b = \max(W_1, W_2 + g)$ $b_p = \max(W_1, 2g)$

**Table 1.** Relationship between 2D grain measurements and geometric values used to calculate volume and surface area. Grain measurements relative to each idealized geometry are shown in Fig. 1b.

the results (e.g., Hourigan et al., 2005; Ketcham et al., 2011) and depend on alpha-stopping distance and grain geometry. For the new protocol, the  $F_T$  equations and coefficients of Ketcham et al. (2011) are adopted as the basis for calculating  $F_T$  (Appendix A) because they are fit to the full range of grain geometries commonly seen in natural zircon. For grains that begin whole as ellipsoids, cylinders, or tetragons without terminations, grinding and polishing results in remaining grain fragments with morphologies that are still well described by the original geometries and  $F_T$  equations tailored to those geometries, such that minimal uncertainty is introduced by applying the geometry-specific coefficients of Ketcham et al. (2011) to these polished grains. The wholegrain coefficients are likely less applicable to grain geometries that change more significantly with grinding and polishing, namely tetragonal geometries with one or two terminations, and the new protocol should be applied with caution to these geometries. However, even with this limitation, the new protocol improves on existing protocols for polished grain  $F_T$  values through the addition of ellipsoid geometries and a range of polishing depth beyond half of the original grain width.

< halfway

In addition to isotope-specific  $F_T$  values (used to calculate corrected (U-Th)/He dates), combined  $F_T$  and  $F_T$ -equivalent spherical radius ( $R_{\rm FT}$ ) are calculated using equations from Cooperdock et al. (2019) (Appendix A). Combined  $F_T$  is useful as a summary of overall alpha-ejection correction and for comparison with other formulations of  $F_T$  (e.g., Reiners et al., 2007).  $R_{FT}$  is commonly reported as a proxy for grain size (e.g., Flowers et al., 2022a). Isotope-specific  $F_T$  uncertainties for ellipsoid and tetragonal geometries are applied following recommendations in Zeigler et al. (2024) for ellipsoid and tetragonal grain geometries; for cylindri-

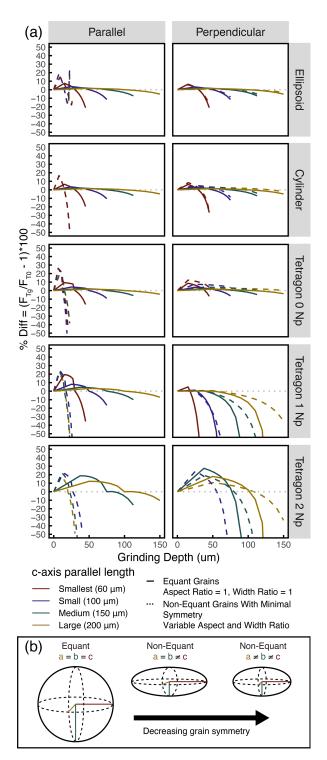
cal geometries, the larger of the recommended uncertainties for the other geometries is applied (ellipsoid: 3%, 4%, 4%, and 1% for  $F_{T,238}$ ,  $F_{T,235}$ ,  $F_{T,232}$ , and  $F_{T,147}$ , respectively; tetragonal/cylindrical: 3%, 4%, 5%, and 1% for  $F_{T,238}$ ,  $F_{T,235}$ ,  $F_{T,232}$ , and  $F_{T,147}$ , respectively). Combined  $F_{T}$  uncertainty is propagated from isotope-specific  $F_{T}$  values and parent isotope concentrations. Uncertainty on  $R_{\rm FT}$  is applied as  $1\sigma=8\%$   $R_{\rm FT}$  following recommendations in Zeigler et al. (2024).

 $c = \frac{(L_1 + L_2)}{2}$   $c_p = c - N_P \left(\frac{W_2 - g}{2}\right)$ 

### 4 Evaluating the new protocol

A synthetic dataset (Table S1) was used to evaluate the protocol and compare with existing approaches to calculating  $F_T$ values. The synthetic dataset was designed to test a range of original grain geometries, total grain sizes, grinding and polishing orientations, and grinding depths greater than the maximum average zircon alpha stopping distance ( $>\sim 18.5 \,\mu m$ ; Ketcham et al., 2011). Total grain size was defined by a combination of "size" corresponding to the c-axis parallel length - generally the longest grain axis corresponding to grain length measurements  $L_1$  and  $L_2$ , "width ratio" between the two c-axis perpendicular grain lengths (corresponding to a and b crystallographic axes and grain width measurements  $W_1$  and  $W_2$ ), and "aspect ratio" between the c-axis parallel and perpendicular axes lengths. First, whole, unpolished synthetic grains were created with sizes  $L_1$  and  $L_2$ , including "smallest" (60 µm), "small" (100 µm), "medium" (150 µm), or "large" (200 µm), a range of aspect ratios where the first axis  $(W_1)$ , was set to 0.3–1 times the size, and a range of width ratios where the second short axis  $(W_2)$  was set to 0.5– 1 times  $W_1$ . The range of c-axis parallel sizes was chosen to reflect sizes commonly seen in natural zircon. Aspect and width ratio ranges were chosen to reflect observed ranges of these ratios while also ensuring that grinding depth would always be greater than one alpha stopping distance. This was done to ensure no complications to interpreting  $F_T$  arising from incomplete removal of the alpha-ejection rim. Grains were created in this way for all common zircon idealized geometries: ellipsoid, cylinder, and tetragons with no, one, or two terminations. "Polished grains" were then created by assigning grinding depth as a fraction of the total width or length of the grain depending on whether grains were polished parallel or perpendicular to the c axis, respectively. The range of grinding depths includes 0 (unpolished grains) and 0.25–0.75 of the total width or length.

 $F_T$  results of applying the protocol developed in this contribution to the synthetic dataset show a strong dependence on geometry and size (Fig. 2a), as expected based on  $F_T$ values for whole grains (Farley, 2002; Ketcham et al., 2011; Reiners et al., 2005). The Ketcham et al. (2011)  $F_T$  functions and polynomial coefficients adopted in the new protocol apply to  $F_T$  between 0.5 and 1: whole synthetic grains with  $F_T < 0.5$  were therefore rejected from further discussion, as were polished synthetic grains based on the rejected original whole-grain dimensions, leaving  $F_T$  results for 16 128 synthetic grains. Across all geometries and grain sizes, the majority of grains exhibit expected changes in  $F_T$  with increasing grinding depth: polished  $F_T$  is greater than whole  $F_T$  up to 50 % grinding depth, and polished  $F_T$  is less than whole  $F_T$  above 50 %. The smallest ellipsoid grains with the lowest aspect and width ratios (e.g., Fig. 2b) are an exception to this pattern, which is likely related to partial removal of the remaining fragment's alpha-ejection rim at higher grinding depths. The largest grains exhibit the smallest differences between whole-grain and polished grain  $F_T$ , but the difference increases once more than half the grain width is ground away as for other grain sizes (Fig. 2a). Very negative percent differences < -20% that are reached at high grinding depths are likely due to the increasing differences in polished  $SA_{\alpha}$  from whole-grain  $SA_{\alpha}$  at this degree of polishing. Percent difference between whole- and polished grain  $F_T$  does not vary systematically with overall grain symmetry - that is, with changes in grain aspect ratio and width ratio. Rather, the difference depends on the combination of axis measurements and other factors, such as the number of terminations in the case of tetragonal grains (Fig. 2a). Tetragonal geometries with zero terminations vary the least with polishing depth, while tetragonal geometries with two terminations vary the most. This result is not surprising given that termination morphology is heavily impacted by grinding such that the approximation becomes more and more tenuous with increasing removal of grain material. Terminations are approximated using a uniform assumption of symmetric pyramidal terminations sloped 45° to the prismatic core of the grain (Ketcham et al., 2011), which is also likely responsible for some of the unexpected behavior of these grains, as, in reality, this angle can vary from zircon to zircon.



**Figure 2.** (a) Percent difference between combined  $F_T$  for ground/polished zircon and whole zircon as a function of grinding depth. Color corresponds to c-axis parallel length. Solid lines show patterns for largest equant grains in each size group (aspect ratio = 1, width ratio = 1). Dashed lines show patterns for smallest non-equant grains in each size group with minimum symmetry that meet requirements for whole-grain  $F_T \geq 0.5$ . (b) Cartoon showing variability possible between equant and non-equant grains.

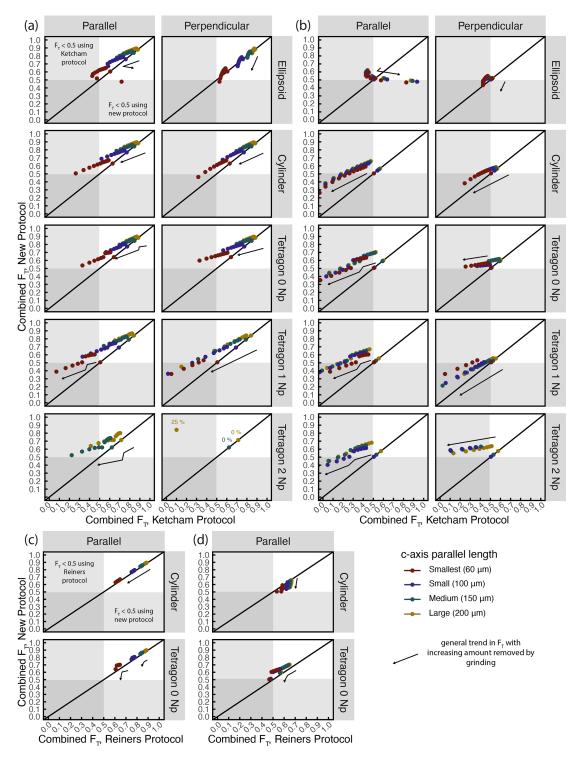


Figure 3. Comparison between combined  $F_T$  calculated using the new protocol and existing protocols. (**a, b**) Comparison with the protocol of Ketcham et al. (2011) for (**a**) equant grains (aspect ratio = 1, width ratio = 1) and (**b**) non-equant grains with minimum symmetry that meet requirements for whole-grain  $F_T \ge 0.5$ . (**c, d**) Comparison with the protocol of Reiners et al. (2007) for (**c**) equant grains and (**d**) non-equant grains with minimum grain symmetry. See Fig. 2b for schematic variability between equant and non-equant grains. Note that the Reiners et al. (2007) protocol only applies to cylindrical and non-terminated tetragonal geometries and grinding depths  $\le 50\%$  of the original width. In all plots, color corresponds to size defined as the c-axis parallel length. Black arrows indicate the general trend of  $F_T$  with increasing fraction of the grain removed through grinding. Gray shaded regions correspond to  $F_T < 0.5$ ; these grains would typically be discarded from (U-Th)/He date interpretations.

 $F_T$  values calculated using the new protocol were compared to existing  $F_T$  protocols from Ketcham et al. (2011) and Reiners et al. (2007) (Fig. 3). Although the Ketcham et al. (2011) protocol is not designed for polished grains, it might be assumed that the difference in final  $F_T$  value obtained by applying it might be negligible due to the application of the same polynomial coefficients in both methods. Here, the methods are compared to show that systematic biases are introduced when a whole-grain protocol is applied to polished grains that can result in limited utility of the dataset. This comparison was achieved by duplicating the synthetic dataset and setting the grinding depth g equal to 0 for all synthetic grains so that the code treated them as unpolished for calculating V,  $SA_{\alpha}$ , and  $F_T$ . For equant grains (aspect and width ratios of 1; Fig. 2b), applying the whole-grain Ketcham et al. (2011) protocol results in  $F_T$  values that are generally lower than the new protocol (Fig. 3a). This is expected: the Ketcham et al. (2011) protocol calculates  $SA_{\alpha}$  that is higher than the real polished  $SA_{\alpha}$ in all cases and, in the case of ellipsoids, calculates V that is significantly smaller than the real polished V. If the recommended 0.5  $F_T$  cutoff for accepting (U-Th)/He analyses is applied (e.g., Flowers et al., 2022b; Ketcham et al., 2011) to the polished fragments, use of the Ketcham et al. (2011) protocol would result in rejection of more ellipsoid, cylindrical, and terminated tetragonal grains than the new protocol, while more non-terminated tetragonal grains would be kept. This is because the only difference between the two protocols for non-terminated tetragonal grains is the inclusion of the polished face in  $SA_{\alpha}$ . For non-equant grains with varying degrees of symmetry (Fig. 2b), both protocols result in the rejection of most grain fragments (Fig. 3b), but the Ketcham et al. (2011) protocol results in more total rejections due to its inaccurate estimates of V and  $SA_{\alpha}$ . This is important for real datasets in which grain aspect and width ratios can be expected to vary widely and rarely match the equant case. By taking grinding and polishing into account, the new protocol results in  $F_T$  values that reflect the true  $SA_{\alpha}$  and V of the measured grain fragment and are more likely to meet the criteria for being accepted.

The Reiners et al. (2007) protocol uses V and  $\mathrm{SA}_{\alpha}$  of grain fragments with the  $F_T$  formulas and polynomial coefficients of Farley (2002), but it applies only to cylindrical and non-terminated tetragonal grain geometries polished less than halfway through the original width of the crystal. For equant grains (Fig. 3c), the synthetic  $F_T$  results of the Reiners et al. (2007) protocol are almost identical to the new protocol, with all  $F_T$  values > 0.5. In these cases, the calculation of  $\mathrm{SA}_{\alpha}$  and V are the same between the two methods, and any discrepancy is the result of differences between the polynomial coefficients used. However, systematic offsets related to grain geometry appear when comparing  $F_T$  for cylindrical non-equant grains with less symmetry (Fig. 3d). For cylindrical grains, the Reiners et al. (2007) protocol results in higher  $F_T$  values than the new protocol reflecting

that the Reiners et al. (2007) protocol assumes grains are true cylinders with equant a and b semi-axes. This results in underestimates of  $SA_{\alpha}$  and V compared to the new protocol which treats cylinders as prisms with ellipsoidal pinacoid terminations. For tetragonal grains,  $F_T$  values calculated using the new protocol are larger than values calculated using the Reiners et al. (2007) protocol. Tetragonal  $SA_{\alpha}$  and V are calculated using the same formulas regardless of protocol, so differences arise solely from the difference in polynomial coefficients. Although there is not a significant difference in the number of grain fragments with  $F_T > 0.5$  between the new and Reiners protocols, the addition of ellipsoid grains and the greater range of grinding depths covered under the new protocol makes it an improvement over the existing Reiners et al. (2007) method.

The new protocol covers crystal morphologies commonly observed in the detrital zircon record and suggests grain size limits to guide selection of real grains for analyses involving polishing. For detrital zircon studies, grains are likely to be large due to grain size bias arising from abrasion during sedimentary transport (e.g., Fig. S1 in the Supplement), and size is generally less of a consideration for choosing grains. However, for other applications, in which a greater range of grain size is present, choice of grain targets will need to consider size, as in conventional whole-grain (U-Th)/He applications (e.g., Reiners and Farley, 2001). For thin, needle-like morphologies (Fig. 3b and d), grains with long axes < 150 are less likely to result in  $F_T > 0.5$  and then only when ground < 55 % of the original grain width. When grain aspect ratios are higher, long axis length can be shorter to include grains with c-axis parallel lengths  $< 100 \,\mu m$  (Fig. 3a and c). However, for the smallest grains, care must still be taken to remove minimal material through grinding in order for  $F_T$  values to be above 0.5.

An example of the applicability of the new protocol to detrital zircon datasets is provided in the Supplement. The new protocol can also be applied to certain non-sedimentary applications, though additional work is needed to accurately account for polishing tetragonal grains with terminations, such as those that are commonly found in igneous and metamorphic rocks.

#### 5 Conclusions

To combine (U-Th)/He dates with the maximum additional same-grain data, methods for calculating grain V and (U-Th)/He data derived from V must account for the grinding and polishing of grains necessary for many in situ analyses. Previous work has provided protocols to calculate some derived data, mainly  $F_T$  corrections, for some, but not all, grinding conditions. In particular, parent isotope concentrations and eU have previously been ignored. The protocol presented here provides a means to obtain V,  $\mathrm{SA}_\alpha$ , and all data derived from these values, including  $F_T$  and eU, re-

gardless of original grain geometry and polishing conditions. For a suite of synthetic zircon, the new protocol behaves as expected for grains that meet recommended grain size requirements for whole-grain analyses and have ellipsoidal, cylindrical, or non-terminated tetragonal original grain morphologies. This makes the new protocol well suited to applications involving detrital zircon, which generally include these grain morphologies and large grains. Additional work is needed to adapt existing protocols or create new ones for cases involving tetragonal grains with pyramidal terminations. (U-Th)/He datasets are usually small and may be limited by other grain selection factors that reduce the population of suitable grains for a given sample; this makes it especially important to maximize the number of grains with usable  $F_T$  values. The new protocol presented here achieves this through more accurate calculation of grain V and  $SA_{\alpha}$ for polished grain fragments used in the calculation of  $F_T$ . Even for cases where prior methods for calculating  $F_T$  for ground and polished grains (e.g., Reiners et al., 2007) apply, the new protocol is still an improvement, as it provides the full set of recommended reporting data (e.g., Flowers et al., 2022a). The new protocol includes calculation of all data derived from V (eU, parent isotope concentrations, and  $R_{\rm FT}$ ) and assigns uncertainty following current recommendations for zircon (Zeigler et al., 2024). The comprehensive nature of the new protocol enables the incorporation of polished grain (U-Th)/He dates into existing workflows for (U-Th)/He date interpretation and thermal history modeling.

# Appendix A: Equations to calculate volume, alpha-ejection surface area, $R_{\rm SV}$ , mass, parent isotope concentrations, eU, $F_T$ , and $R_{\rm FT}$

### A1 Ellipsoid volume and alpha-ejection surface area

The ellipsoid semi-axes (a, b, and c) and polished surface semi-axes  $(a_P, b_P, and c_P)$  are related to 2D grain measurements  $L_1, L_2, W_1, W_2, L_P, W_P, and g$ , as given in Table 1 and shown in Fig. 1b for each polishing orientation and depth. The ellipsoid coefficient (p) used in the calculation of  $SA_\alpha$  is 1.6075 (Ketcham et al., 2011). When the grain is polished perpendicular to the c axis or polished parallel to the c axis and more than halfway through the original c-axis perpendicular width  $(g > (W_2 + g)/2)$ , the grain is treated as half a symmetric ellipsoid broken perpendicular or parallel to the c axis, and V and  $SA_\alpha$  are calculated using formulas for half an ellipsoid Eqs. (A1) and (A2).

$$V = \frac{2}{3}\pi abc \tag{A1}$$

$$SA_{\alpha} = 2\pi \left(\frac{a^{p}b^{p} + b^{p}c^{p} + a^{p}c^{p}}{3}\right)^{1/p}$$
(A2)

When the grain is polished parallel to the c axis and less than halfway through the original width  $(g < (W_2 + g)/2)$ , V and

 $SA_{\alpha}$  are calculated using Eqs. (A3) and (A4), which combine the estimated V and surface area of the whole original grain and the removed portion of the grain approximated as half a symmetric ellipsoid broken parallel to the c axis.

$$V = \frac{4}{3}\pi abc - \frac{2}{3}\pi a_{\rm P}b_{\rm P}c_{\rm P} \tag{A3}$$

$$SA_{\infty} = 4\pi \left( \frac{a^{p}b^{p} + b^{p}c^{p} + a^{p}c^{p}}{3} \right)^{1/p}$$

$$-2\pi \left(\frac{ap^{\mathrm{p}}bp^{\mathrm{p}} + bp^{\mathrm{p}}cp^{\mathrm{p}} + ap^{\mathrm{p}}cp^{\mathrm{p}}}{3}\right)^{1/p} \tag{A4}$$

### A2 Cylinder volume and alpha-ejection surface area

"Cylinders" can more accurately be represented as prisms with height (h) and ellipsoidal, rather than circular, pinacoid terminations with semi-axes a and b (Fig. 1b). V and  $SA_{\alpha}$  are calculated using the area of an ellipse ( $\pi ab$ ) and Ramanujan's formula for the perimeter of an ellipse (Eq. A5).

$$P_{\text{ellipse}} = \pi(a+b) \left[ 1 + \frac{3k}{10 + \sqrt{4-3k}} \right]$$
 (A5)

Semi-axes of the ellipsoid cross-section are denoted as a and b, k is defined as  $(a-b)^2/(a+b)^2$ , and h is the height or length of the cylinder. The semi-axes are related to the 2D grain measurements and g depending on the degree of polishing, as given in Table 1. When the grain is polished perpendicular to the c axis, the grain is treated as half a symmetric prism broken perpendicular to the c axis, and V and  $SA_{\alpha}$  are calculated using Eqs. (A6) and (A7).

$$V = \pi abh \tag{A6}$$

$$SA_{\alpha} = \pi ab + \pi (a+b) \left( 1 + \frac{3k}{10 + \sqrt{4-3k}} \right) h$$
 (A7)

When the grain is polished parallel to the c axis and more than halfway through the original width  $(g > (W_2 + g)/2)$ , V and  $SA_{\alpha}$  are calculated using Eqs. (A8) and (A9), which treat the fragment as half of a cylinder.

$$V = \frac{1}{2}\pi abh \tag{A8}$$

$$SA_{\infty} = \pi ab + \frac{\pi(a+b)}{2} \left( 1 + \frac{3k}{10 + \sqrt{4-3k}} \right) h$$
 (A9)

When the grain is polished parallel to the c axis and less than halfway ( $g < (W_2 + g)/2$ ), V and  $SA_{\alpha}$  are calculated using Eqs. (A10) and (A11), which combine the estimated V and surface area of the whole original grain and the removed portion of the grain approximated as half a symmetric prism bro-

ken parallel to the c axis.

$$V = \pi h \left( ab - \frac{1}{2} a_{P} b_{P} \right)$$

$$SA_{\alpha} = 2\pi \left( ab - \frac{1}{2} a_{P} b_{P} \right)$$

$$+ \pi h \left[ (a+b) \left( 1 + \frac{3k}{10 + \sqrt{4 - 3k}} \right) - \frac{1}{2} (a_{P} + b_{P}) \left( 1 + \frac{3k_{P}}{10 + \sqrt{4 - 3k_{P}}} \right) \right]$$
(A10)

### A3 Tetragon volume and alpha-ejection surface area

The tetragon axes (a, b, and c) are related to 2D grain measurements  $(L_1, L_2, W_1, W_2, \text{ and } g)$ , as given in Table 1 and shown in Fig. 1b for each polishing orientation and depth.  $N_p$  is the number of pyramidal terminations (0, 1, or 2). When the grain is polished perpendicular to the c axis, the grain is treated as half a symmetric prism broken perpendicular to the c axis, and V and  $SA_{\alpha}$  are calculated using Eqs. (A12) and (A13).

$$V = abc - N_{\rm p} \left(\frac{a}{4}\right) \left(b^2 + \frac{a^2}{3}\right)$$

$$SA_{\alpha} = 2(ab + bc + ac)$$
(A12)

$$-N_{\rm p}\left(\frac{a^2-b^2}{2} + \left(2-\sqrt{2}\right)ab\right) - ab$$
 (A13)

When the grain is polished parallel to the c axis and more than halfway  $(g > (W_2 + g)/2)$ , the grain is treated as half a symmetric prism broken parallel to the c axis, and V and  $SA_{\alpha}$  are calculated using Eqs. (A14) and (A15).

$$V = \frac{abc - N_{\rm p}\left(\frac{a}{4}\right)\left(b^2 + \frac{a^2}{3}\right)}{2}$$
 (A14)

$$SA_{\alpha} = \frac{2(ab + bc + ac) - N_{p}\left(\frac{a^{2} - b^{2}}{2} + \left(2 - \sqrt{2}\right)ab\right)}{2}$$
 (A15)

When the grain is polished parallel to the c axis and less than halfway ( $g < (W_2 + g)/2$ ), V and  $SA_{\alpha}$  are calculated using Eqs. (A16) and (A17), which combine the estimated V and surface area of the whole original grain and the removed portion of the grain, which is approximated as half a symmetric

prism broken parallel to the c axis.

$$V = abc - N_{p} \left(\frac{a}{4}\right) \left(b^{2} + \frac{a^{2}}{3}\right)$$

$$-\frac{1}{2} \left[a_{p}b_{p}c_{p} - N_{p} \left(\frac{a_{p}}{4}\right) \left(b_{p}^{2} + \frac{a_{p}^{2}}{3}\right)\right]$$

$$SA_{\alpha} = 2(ab + bc + ac)$$

$$-N_{p} \left(\frac{a^{2} - b^{2}}{2} + \left(2 - \sqrt{2}\right)ab\right)$$

$$-\frac{1}{2} \left[2\left(a_{p}b_{p} + b_{p}c_{p} + a_{p}c_{p}\right)\right]$$

$$-N_{p} \left(\frac{a_{p}^{2} - b_{p}^{2}}{2} + \left(2 - \sqrt{2}\right)a_{p}b_{p}\right)$$

$$(A17)$$

### A4 Mass, parent isotope concentrations, and eU

M is calculated assuming an average zircon density  $4.65 \times 10^{-12} \,\mathrm{g}\,\mu\mathrm{m}^{-3}$  using Eq. (A18) and inherits uncertainty from V.

$$M = \left(4.65 \times 10^{-12}\right) V \tag{A18}$$

Parent isotope concentrations for uranium (U), thorium (Th), and samarium (Sm) in ppm are calculated from parent isotope masses in ng and total M using Eq. (A19). Parent isotope concentration uncertainty is propagated from the total analytical uncertainty on the ng measurements and M uncertainty inherited from V.

$$[X] = \frac{(\text{ng}X)/1000}{M} \tag{A19}$$

eU is calculated using Eq. (A9) from Cooperdock et al. (2019), Eq. (A20) below. Uncertainty on eU is propagated from uncertainties on the U, Th, and Sm concentrations combining total analytical uncertainty and V uncertainty.

$$eU = [U] + 0.238[Th] + 0.0083[^{147}Sm]$$
 (A20)

A5  $F_T$  and  $R_{FT}$ 

 $F_T$  values are calculated using the weighted mean stopping distances  $S_x$  of an alpha particle for a given parent isotope decay chain (15.55, 18.05, 18.43, and 4.76 µm for  $^{238}$ U,  $^{235}$ U,  $^{232}$ Th, and  $^{147}$ Sm, respectively; Ketcham et al., 2011),  $R_{\rm SV}$  dependent on the crystal volume and ejection surface area (Eq. 2), and geometry-specific  $F_T$  equations from Ketcham et al. (2011) (Eqs. A21–A23 below). Equation (A22) for cylinders has been modified from Ketcham et al. (2011) to be in terms of  $R_{\rm SV}$  and h rather than r and h.

For ellipsoidal grains,  $F_T$  is given by Eq. (A21):

$$F_{T,x} = 1 - \frac{3}{4} \left( \frac{S_x}{R_{SV}} \right) + \left[ \frac{1}{16} + 0.1686 \left( 1 - \frac{a}{R_{SV}} \right)^2 \right]$$

$$\left( \frac{S_x}{R_{SV}} \right)^3. \tag{A21}$$

For cylindrical grains,  $F_T$  is given by Eq. (A22):

$$F_{T,x} = 1 - \frac{3}{4} \frac{S_x}{R_{SV}} + \frac{0.3183}{h + \left[\frac{\frac{2}{3}R_{SV}h}{h - \frac{2}{3}R_{SV}}\right]} \frac{S_x^2}{R_{SV}} + \frac{0.153}{\left[\frac{\frac{2}{3}R_{SV}h}{h - \frac{2}{3}R_{SV}}\right]^3} S_x^3.$$
(A22)

For tetragonal grains,  $F_T$  is given by Eq. (A23). If the grain is polished perpendicular to the c axis, c from Table 1 is multiplied by 2 in Eq. (A23). If the grain is polished parallel to the c axis, b from Table 1 is multiplied by 2.

$$F_{T,x} = 1 - \frac{3}{4} \left( \frac{S_x}{R_{SV}} \right) + \frac{0.2095(a+b+c)S_x^2}{2V} - N_p(a+b) \left( 0.096 - 0.013 \frac{a^2 + b^2}{c^2} \right) \frac{S_x^2}{2V}$$
(A23)

Combined  $F_T$  is calculated for each grain using equations from Cooperdock et al. (2019) and activities for <sup>238</sup>U and <sup>232</sup>Th and  $A_{238}$  and  $A_{232}$ , respectively (Eqs. A24–A26).

$$A_{238} = (1.04 + 0.247[\text{Th/U}])^{-1}$$
 (A24)

$$A_{232} = (1 + 4.21[\text{Th/U}])^{-1} \tag{A25}$$

$$\overline{F_T} = A_{238}F_{T,238} + A_{232}F_{T,232} + (1 - A_{238} - A_{232})$$

$$F_{T,235} \tag{A26}$$

*R*<sub>FT</sub> is calculated using Eq. (6) from Cooperdock et al. (2019) and related equations (Eqs. A27–A29).

$$S/R = 1.681 - 2.428\overline{F_T} + 1.153\overline{F_T}^2 - 0.406\overline{F_T}^3$$
 (A27)

$$\overline{S} = A_{238}S_{238} + A_{232}S_{232} + (1 - A_{238} - A_{232})S_{235}$$
 (A28)

$$R_{\rm FT} = \frac{\overline{S}}{S/R} \tag{A29}$$

Code and data availability. An R script to apply the protocol presented in this work is available with potential future updates on GitHub (https://github.com/Barra-Peak/polished-ZHe-derived-values, last access: 28 October 2025). A static version of all code scripts and data used to produce the results presented here is available in repository form (Peak, 2025). All data used to evaluate the protocol are also included in Tables S1 and S2 in the Supplement.

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