Simulating sedimentary burial cycles: <u>I.</u> Investigating the role of apatite fission track annealing kinetics using synthetic data

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Abstract

Age dispersion is a common feature of apatite fission track (AFT) and apatite (U–Th)/He (AHe) thermochronological data and it can be attributed to multiple factors. One underappreciated and underreported cause for dispersion is variability in apatite composition and its influence on thermal annealing of fission tracks. <u>Using</u> <u>synthetic data</u> we investigate how multikinetic AFT annealing behaviour, defined using the r_{mr0} parameter, can be exploited to recover more accurate, higher resolution thermal histories than are possible using conventional interpretation and modelling approaches. Our forward model simulation spans a 2 Gyr time interval with two

- 15 separate heating and cooling cycles and <u>was used to generate synthetic AFT and AHe data for three different apatite</u> populations with significantly different annealing kinetics. The synthetic data <u>were then</u> used as input for inverse modelling in the Bayesian QTQt <u>software to recover thermal history</u> information under various scenarios. Results show that essential features of the dual peak thermal history are captured using the multikinetic AFT data alone, with or without imposed constraints. Best results are achieved when the multikinetic AFT data are combined with
- 20 the AHe data and <u>geologic constraint boxes</u>, are included. In contrast, a more conventional monokinetic interpretation that ignores multikinetic AFT behaviour <u>reproduces all the input data but yields</u> incorrect thermal solutions. Under these conditions, incorporation of constraints can be misleading and fail to improve model results. In general, a close fit between observed and modelled parameters is no guarantee of a robust thermal-history solution if data are incorrectly interpreted. For the case of overdispersed AFT data, it is strongly recommended that
- 25 elemental data be acquired to investigate if multikinetic annealing is the cause of the <u>AFT apparent age</u> scatter. <u>Elemental analyses can also be similarly useful for broadly assessing AHe data.</u> A future companion paper will explore multikinetic AFT methodology and application to detrital apatite samples from Yukon, Canada.

1. Introduction

Studies focusing on upper crustal tectonics, landscape evolution, and sedimentary basin analysis often rely on apatite
 fission track (AFT) and apatite (U–Th)/He (AHe) low-temperature thermochronology to decipher spatial patterns of exhumation and burial through time (e.g., Zeitler et al., 1982; Naeser et al., 1989; van der Beek et al., 1995; House et al., 1998; Ehlers and Farley, 2003). These low-temperature techniques typically produce internally consistent

results in rapidly cooled, actively eroding mountain belts (e.g., Glotzbach et al., 2011), however, thermochronometric harmony commonly breaks down in slowly cooled settings. There are gaps in our knowledge of

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- 55 how fission tracks anneal in apatite (e.g., Ketcham, 2019), how ⁴He diffusion occurs over geologic time (e.g., McDannell et al., 2018), and if the mechanisms controlling these processes are fundamentally different, linked, or interact in complex and unforeseen ways (McDannell et al., 2019a). Poorly understood compound variables, both geological and analytical, sometimes yield apatite thermochronology data that are not straightforward to interpret. For example, AFT < AHe "age inversion" (e.g., Farley et al., 1996; Fitzgerald et al., 2006; Flowers and Kelley,
- 60 2011) is often encountered in continental interiors and has been attributed to the effects of slow cooling and accumulated radiation damage on He diffusion (e.g., Green et al., 2006). Highly overdispersed AFT data are also found, in slowly cooled, ancient terranes (McDannell et al., 2019a), suggesting there are unexplained complexities present in both systems.
- 65 The canonical temperature sensitivity for AFT dating is ~60-120, °C (Gleadow and Duddy, 1981) and ~45-75 °C for AHe dating (Wolf et al., 1998). However, temperature sensitivity varies as a function of multiple factors such as apatite chemistry (Green et al., 1985, 1986; Crowley et al., 1990; Ravenhurst et al., 1993; Carlson et al., 1999; Barbarand et al., 2003) and cooling rate for AFT, and radiation damage accumulation, grain size, parent nuclide zoning, and chemistry for AHe (e.g., Farley, 2000; Shuster et al., 2006; Gautheron et al., 2009; Gautheron et al.,
- 70 2013; Djimbi et al., 2015; Recanati et al., 2017). Radiation damage may also play a role in modifying apatite fission track annealing kinetics from old rocks (e.g., Carpéna et al., 1988; Hendriks and Redfield, 2005), or at least cause reduced thermal annealing resistance (McDannell et al., 2019a). This is a debated issue (Kohn et al., 2009) requiring further scrutiny and experimental work to verify empirical relationships (e.g., Carpéna and Lacout, 2010). However, observations of AHe age-U and age-elemental trends by Recanati et al. (2017) and joint AFT-AHe age-U trends by
- 75 McDannell et al. (2019a) imply a complex relationship between α -radiation damage, fission tracks, and apatite chemistry, where apparent ages increase and then decrease as a function of the estimated damage accumulated, similar to observations in zircon (Guenthner et al., 2013). This suggests a change in both helium and fission-track retention at high radiation damage levels and warrants a closer inspection of apatite chemistry, radiation damage, and track annealing for applications in thermal history analysis.

80 2. Motivation

There is clear experimental documentation that AFT annealing is influenced by composition (e.g., Gleadow and Duddy, 1981; Green et al., 1986; Carlson et al., 1999; Barbarand et al., 2003; Ravenhurst et al., 2003). The work of Carlson et al. (1999) remains one of the most detailed studies of fission track annealing with respect to apatite chemistry. They derived the empirical rnn0 kinetic parameter by characterizing track annealing with respect to

85 chemical composition to produce a multikinetic annealing model that relates one apatite to another for the purposes of comparing annealing behaviour at laboratory timescales. Laboratory annealing was then extrapolated to the geologic timescale for the purpose of time-temperature (t-T) modelling (Ketcham et al., 1999; Ketcham et al., 2007). Specifically, r_{mt0} is the reduced fission-track length of the more resistant apatite at the point in time and temperature where the less resistant apatite is totally annealed, allowing a direct comparison between any two

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105 apatites (Ketcham et al., 1999). Therefore, rmr0 values approaching one, signify lower retentivity, whereas those approaching zero are more retentive, with common fluorapatite defined by an rmr0 value of 0.83.

The main purpose of this paper is to show that multikinetic AFT samples with significantly different annealing characteristics carry far more thermal history information than single AFT populations with typical annealing

- 110 temperatures (~100–110°C) and under certain circumstances it is possible to recover information about multiple heating events from a single multikinetic AFT sample. Here, we present simple examples demonstrating this point using synthetic AFT data derived from forward models utilizing the rmr0 kinetic parameter based on apatite composition (Carlson et al., 1999; Ketcham et al., 1999). The synthetic data are <u>idealized and</u> exaggerated when <u>compared to most natural samples</u>, implementing extreme endmember kinetics that are rare, but not unheard of, in
- 115 natural crystalline basement samples and more commonly encountered in detrital samples. This was done to illustrate that multikinetic AFT samples provide an expanded range in thermal sensitivity and <u>demonstrate that</u> statistically valid, yet spurious, thermal histories may be recovered if potential kinetic sub-populations governed by composition are not accounted for during data interpretation, or are alternatively unresolvable due to collection of low precision kinetic data (Issler et al., 2018; Schneider and Issler, 2019) such as D_{par} (mean etch-figure width),

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This is a synthetic resolution test and a single example drawn from a nearly infinite number of possibilities. We chose a deep-time problem involving slow cooling and multiple reheating events because it is harder to deal with than a Phanerozoic case that may have more geological constraints available. In general, deep-time problems suffer from greater uncertainty that could be addressed by having thermochronometers with a broad range of temperature

- 125 sensitivity (McDannell and Flowers, 2020). These exercises were performed assuming that we knew the true thermal history, which is almost always not the case, and they are ultimately meant to encourage users of low-temperature thermochronology to thoroughly interpret data and explore kinetic models before undertaking thermal history simulations. The results in this paper give us confidence in our treatment of real data and support the idea that the multikinetic AFT approach yields higher resolution thermal histories than the conventional method. We will 130
- analysis of natural detrital samples from Yukon, Canada in a future companion paper.

We believe that it is best to use an ideal endmember synthetic sample with well-defined kinetic populations to illustrate that it is possible, in principle, to recover information about multiple heating events from a single

- 135 multikinetic AFT sample using inverse modelling techniques. We emphasize that natural samples are rarely this perfect and our synthetic examples are idealized in the sense that apparent age dispersion is low for individual kinetic populations, but dispersion is high for the overall sample which is the normal starting condition for most natural overdispersed samples that then require further interpretation. For natural samples, complicated thermal history information may be retained in multikinetic AFT samples and the degree to which this information can be
- 140 recovered will vary from sample to sample. Consideration of kinetics is most important for histories involving persistence at, or reheating to, a temperature range that differentiates the thermal response of the grains present, and

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We recognize chemical composition has an effect on both AFT and AHe dates, but careful investigation of this property for both chronometers remains problematic. The main factors preventing this are practical in nature, in that most AFT studies utilize compositional proxies due to ease of measurement (i.e., Dpar mean etch figure width parallel to c-axis; Burtner et al., 1994; Donelick, 1993) and neglect elemental data to fully characterize samples. Likewise, the bulk AHe method is a destructive technique that precludes single-grain elemental characterization. The overwhelming majority of published studies featuring age inversion present AFT and AHe data from different grains, making direct comparisons between individual apatites challenging (Danišík, 2019). There is also the impractical comparison or statistical problem of likening AFT central ages to mean or single-grain AHe dates. The "central age" for AFT data is utilized to provide an approximate geometric mean apparent age for a population of grain approximate geometric mean apparent age to a population of grain ages in the case of excess age dispersion (Galbraith and Laslett, 1993). Therefore, if an AFT sample fails the χ^2 test and contains discrete age components or a continuous mixture of ages (Galbraith and Green, 1990; Galbraith and Laslett, 1993), then the meaning of the central age is somewhat misleading for comparative purposes. The same applies to averaged AHe dates if accumulated radiation damage varies between grains.

In the overall context of age scatter, another equally viable possibility is that overdispersed or inverted dates for the AFT and AHe thermochronometers occur as a result of variable intrasample retentivity (i.e., resistance to track annealing and diffusive He loss) for both systems due to the effects of apatite chemical composition Fission-track kinetics have also been used to describe changes in ⁴He diffusivity in the apatite (U-Th)/He system (e.g. Flowers et al., 2009). The development of a model to explain radiation damage effects on He diffusivity (Shuster and Farley, 2009; Shuster et al., 2006) resulted in the radiation damage accumulation and annealing model (RDAAM) by using fission-track annealing kinetics of Ketcham et al. (2007) as a proxy for α -damage or bulk radiation damage annealing (Flowers et al., 2009). The fundamental assumption being that α -damage and fission-track damage anneal at the same rate, enabling the use of the r_{mr0} parameter in the RDAAM, set to typical fluorapatite kinetics ($r_{mr0} = 0.83$). This allows a comparison between fission track and He data within the same kinetic framework. However, there is an apparent divergence in. [1]

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thus the apparent ages and lengths recorded. Our ability to resolve kinetic populations depends on the number of AFT age and length measurements and their distribution across different populations. For example, multikinetic 265 AFT data with low U apatite grains can pass the X_{k}^{2} test due to large uncertainties on single-grain apparent ages and these can be misinterpreted as single populations if not carefully investigated using elemental data. If compositional zoning is present, those apatite grains can be assigned to the wrong kinetic population, or some populations may be too highly track retentive (or pice versa) to be sensitive to key parts of a thermal history. To be clear, not all natural samples are multikinetic and the ability to retain a record of a complex thermal history depends strongly on the 270 relative timing and magnitudes of different thermal events and this in turn feeds back into whether kinetic populations have experienced enough differential annealing to be clearly resolved. Unlike AFT, there is limited empirical evidence to suggest ⁴He diffusivity is strongly affected by apatite chemistry Deleted: 1 (e.g., Warnock et al., 1997; Gautheron et al., 2013; Recanati et al., 2017), whereas *ab initio* modelling (e.g., Djimbi Formatted: Font: Italic 275 et al., 2015; Recanati et al., 2021) suggests some effect. None of the diffusion studies (e.g., Warnock et al., 1997) show a direct connection between changes in diffusivity and apatite composition but their results indicate hypothetical offsets in temperature sensitivity between compositional endmember apatites. The development of a model to explain radiation damage effects on He diffusivity (Shuster and Farley, 2009; Shuster et al., 2006) resulted in the radiation damage accumulation and annealing model (RDAAM; Flowers et al., 2009) that used the rmr0

- 280 parameter and fission-track annealing kinetics of Ketcham et al. (2007) as a proxy for α -damage or bulk radiation damage annealing. The fundamental assumption being that α -damage and fission-track damage anneal at about the same rate, enabling the use of the rmr0 parameter in the RDAAM set to typical fluorapatite kinetics (rmr0 = 0.83). This allows a comparison between fission track and AHe data within the same kinetic framework.
- 285 We include synthetic AHe ages in some of our modelling examples since many modern studies include both AFT and AHe data and reconciliation of these complementary datasets is often difficult in slowly-cooled settings. In situations where this occurs, AHe apparent age scatter is often attributed to the effects of radiation damage (or secondarily grain size), yet unexplained dispersion often persists even when these variables are considered. The commonly implemented kinetic models for the AHe system (Flowers et al., 2009; Gautheron et al., 2009) utilize
- 290 fission track annealing as a proxy for radiation damage annealing therefore it is unclear whether chemistry truly affects He diffusion or if this is an illusion due to the use of a composition-based fission-track kinetic model. The assumption here is that apatite chemistry does in fact influence diffusivity and that the rmd parameter adequately describes radiation damage annealing in most geologic settings. Gautheron et al. (2013) and Powell et al. (2020) successfully adopted the approach of varying rand to investigate AHe age dispersion in natural samples from the
- 295 Paris Basin, France and Mackenzie Plain in northern Canada, respectively. We corroborate this and show that AHe ages from grains of identical size and U content may still be highly dispersed due to differences in rgroup values implying that apatite composition may be an additional source of dispersion that is mostly unaccounted for in routine applications. In in the absence of retentivity information for the AHe system, using a default fluorapatite rmt

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value may yield "acceptable" t-T solutions that are inaccurate, especially when data containing more thermal history information, such as AFT ages and lengths, are not collected or jointly modelled,

305 **3. Forward and inverse modelling of multikinetic synthetic data**

3.1 Forward modelled synthetic AFT and AHe data from a predetermined thermal history

Synthetic AFT data were generated from forward modelling a two-pulse heating history over 2000 Myr using the QTQt software v. 5.7.3 (Gallagher, 2012) implementing Ketcham et al. (1999) annealing kinetics (Fig. 1), with one maximum heating event occurring at 1000 Ma (110°C) and the other at 300 Ma (60°C). AFT ages and track length

- 310 data (Fig. 2) were randomly predicted for three kinetic populations as external detector method (EDM) data in QTQt. In this paper, we utilize the relationship established between rmm0 and measured Cl to calculate an "effective Cl" (eCl) value in atom per formula unit (apfu) from collected electron microprobe data (see McDannell et al., 2019b for further explanation). Effective Cl is the Cl concentration required to yield an equivalent rmm0 value for the Ketcham et al. (1999) annealing model based on the published correlation between Cl and rmm0 in Carlson et al.
- **315** (1999). The eCl value (e.g., Issler et al., 2018; McDannell et al., 2019b) is used to transform the nonlinear r_{mr0} parameter to a linear form for data interpretation using the equation (given in Figure 7 of Ketcham et al., 1999):

$$r_{mr0} = 1 - \exp\left[2.107(1 - Cl) - 1.834\right]_{-1}$$

(1)

- 320 Low retentivity apatite with r_{mr0} values exceeding the 0.84 limit of the Ketcham et al. (1999) model transform to negative eCl values. We specified three AFT kinetic populations of 10 age grains each, increasing in retentivity with r_{mr0} values of 0.882 (eCl = -0.144 apfu), 0.820 (eCl = 0.057 apfu), and 0.263 (eCl = 0.726 apfu) using individual-fit *c*-axis projected length kinetic data for distinct apatites from Ketcham et al. (1999). Population one is set to the Holly Springs (Georgia, USA) hydroxyapatite r_{mr0} that typifies the lowest calculated retentivity in the Carlson et al.
- 325 (1999) dataset, population two uses Durango apatite kinetics (laboratory age standard), whereas population three is set to Tioga (Pennsylvania, USA) Fe-Cl apatite, which is characterized by high retentivity and is an outlier of the Carlson et al. rmr0-fitting dataset. The specified thermal history produced three AFT model ages of 670 Ma, 843 Ma, and 1602 Ma (Fig. 2). Seventy-five tracks were generated for each kinetic population with mean *c*-axis projected track lengths (MTL) of 13.32 ± 1.33 µm (1σ), 14.24 ± 1.42 µm, and 14.65 ± 1.47 µm, respectively. The initial (pre-
- 330 annealed) track lengths (*l_{oc}*) for each kinetic population were calculated as 16.17 μm, 16.40 μm, and 17.16 μm with increasing retentivity and were estimated from the equivalent D_{par} calculated from the indicated r_{mr0} value for each kinetic population using the *l_{oc}*-D_{par} relation from Carlson et al. (1999). Three AHe ages, were also forward modelled using the radiation damage accumulation and annealing model (RDAAM) of Flowers et al. (2009), which implements the Ketcham et al. (2007) kinetics for radiation damage annealing. We applied Holly Springs, typical
- 335 endmember fluorapatite ($r_{mr0} = 0.83$ and the RDAAM default), and Tioga apatite r_{mr0} values to AHe grains, all with spherical grain radii of 50 µm and 25 ppm U (Th and Sm discounted for simplicity). The uncorrected AHe <u>ages (α </u> ejection-corrected <u>age in brackets</u>) were 585 Ma [813 Ma], 610 Ma [848 Ma], and 819 Ma [1139 Ma] predicted using the same t–T history (<u>Fig. 1</u>) as the AFT data.

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derived r_{mr0} parameter

The empirical rmr0 kinetic parameter was derived by characterizing track annealing with respect to chemical composition (Carlson et al., 1999) to produce a multikinetic annealing model (Ketcham et al., 1999). Later work updated the equation and annealing data fits (Ketcham et al., 2007) by combining the dataset of Barbarand et al. (2003) with the 1999 dataset. However, the later reformulation of rmr0 is different due to the dominant influence of Cl and OH (and generally lower cation concentrations) in the 2003 dataset, which considerably changes the fitting parameterization. Although the rmr0 kinetic model shows you can reconcile the experimental annealing data with apatite composition, this does not necessarily mean that more data equates to a better calibration. More data changes the calibration, but "improvement" depends on whether the calibration data are representative of the natural range of apatite compositions or are skewed to a particular composition. The Ketcham et al. (2007) model still suffers from an uneven distribution of data and includes a subset of possible compositional ranges that cause the revised equation to narrow the range of rmr0 slightly from the original model. In our view, the 2007 multikinetic model is no better or worse than the original model, however the 1999 model is less dominated by chlorapatite compositions, which aids in clearer multikinetic interpretation (i.e., less kinetic population overlap) for natural AFT samples. It is a reasonable assumption that the same annealing ... [3]

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In addition, the Ketcham et al. (1999) expression relating $r_{\rm mr0}$ to D_{par} is:

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525 Figure 1: Thermal history used to predict synthetic AFT and AHe data. This t–T path is referred to as the "true" thermal history throughout this paper. The predicted synthetic data were then used as input for QTQt to recover the thermal history through inverse modelling. PAZ = partial annealing zone for fission tracks.

3.2 Methods for inverting AFT and AHe synthetic data for thermal history

We attempted to recover the true thermal history used to predict the synthetic data from Sect. 3-1 using the QTQt

- 530 software. QTQt implements a reversible jump Markov Chain Monte Carlo (rjMCMC) algorithm to systematically search t-T space (Gallagher, 2012). These exercises imitate real thermal history investigation in the context of incomplete geologic knowledge, complex or imperfect datasets, and judgement calls that are typically made by researchers implementing thermochronology data and performing modelling to infer quantitative information about geologic processes. We also explore the effects of kinetic assumptions for AHe ages, or the consequences of
- 535 neglecting the identification of multikinetic populations during AFT modelling. An important point is that QTQt uses the ratio of data fit, or likelihood, between a current and proposed model and will accept thermal histories regardless of feasibility, therefore it is up to the user to understand the ramifications of this and make sensible decisions about modelling input and output (Vermeesch and Tian, 2014; Gallagher and Ketcham, 2018). Conversely, other software such as HeFTy (Ketcham, 2005) or AFTINV (Issler, 1996) implement a nondirected
- 540 Monte Carlo (MC) search algorithm and an absolute approach using the *p*-value as a threshold measure of statistical <u>fit</u>. We used QTQt because it is sensitive to the number and quality of data during history inference (i.e., notionally improving model results with additional, high quality data) and specifically because it *will accept* model histories regardless of the physical or geologic plausibility for a history simulation — this was done to explore the possible effects of improper data treatment or <u>data</u> misinterpretation.

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Figure 2: Predicted synthetic AFT data from the thermal history in Figure 1. Multikinetic age populations were individually predicted using distinct rmr0 kinetics shown in (b) panels (discussed in the text). These data were then input in QTQt and inverted 555 in an attempt to recover the true thermal history in Figure 1 (see Fig. 3). (a) Central age and 1 o errors are indicated for each kinetic population. Throughout this paper, "central age" is used for historical reasons to refer to the approximate geometric mear of a population of single-grain AFT ages (Galbraith and Laslett, 1993). The first radial plot shows all thirty individual grains and demonstrates that when taken together, the combined sample fails the X^2 test (p < 0.05) for homogeneity (i.e., that all grains belong to a single underlying age population) suggesting multiple age populations. This is the scenario most researchers would 560 start with before evaluating the sample for potential multikinetic behaviour. Mixture modelling was subsequently performed on the combined sample and the model age peaks that were picked seamlessly align with the individual kinetic population central ages. Kinetic populations one, two, and three are displayed as arms on their respective radial plots, with individual AFT ages closer to the origin being less precise. This aligns with how populations would be defined and compared with the elemental chemistry for individual age grains during multikinetic interpretation. (b) The predicted track length distributions for the 565 combined and individual kinetic populations derived from the thermal history in Figure 1 using the specified kinetic parameter value. Numbers on the histogram are the number of tracks in each µm bin. Abbreviations: eCl = effective Cl; MTL = mean track length.

The r_{mr0} values for AFT and AHe data were held fixed for simulations and noise was added to the synthetic dataset by randomly adding age scatter to single-grain AFT apparent ages by varying spontaneous/induced (Ns/Ni) track

- 570 <u>ratios</u> and setting typical <u>analytical</u> uncertainties for predicted AHe <u>apparent ages</u> (all information given in ascending retentivity/kinetic population order). The AFT data were recast from QTQt individual synthetic output files using random Ns/N₄ ratios that produced central ages for each kinetic group that were in agreement with forward model predictions using identical EDM parameters with a ζ -calibration value = 350 yr cm⁻², induced track density (p_{Di}) = 2.5 x 10⁶ cm⁻², and dosimeter tracks (Nd) = 10000. These common values made it so <u>that</u> each
- 575 population was simulated as being from the same grain mount for the purposes of easy comparison and t–T inversion. The synthetic AFT sample has an overall central age of 934 ± 64 Ma (1σ, X² = 0.0, MSWD = 9, 34% dispersion, n = 30) when all age grains are combined. The central AFT age for population one was calculated as: 670 ± 26 Ma, population two was calculated as: 843 ± 29 Ma, and population three was calculated as: 1602 ± 79 Ma. Three mixture model age peaks of 687 ± 34 Ma, 828 ± 34 Ma, and 1602 ± 78 Ma (1σ) were selected in IsoplotR
- 580 (Vermeesch, 2018) for the combined AFT data, which are in agreement with the individual kinetic population



central ages. The uncorrected AHe <u>ages</u> used all default RDAAM settings with the exception of r_{mr0} and the <u>ages</u> were input as: 585 ± 17 Ma, 610 ± 18 Ma, and 819 ± 25 Ma ($l\sigma$).

615 We ran QTQt in multiple stages to tune Bayesian sampling and to ensure the acceptance rates for time and temperature were between ~0.1–0.7, within the acceptable limits discussed in Gallagher (2012). Inversions were run for >500,000 to >1,000,000 total iterations (burn-in and post_burn-in) and were considered complete when the likelihood distribution was stationary (i.e., there was no trend in the likelihood values with a stable or "flat" mean; Gallagher, 2012). The modelling t–T space (prior) was designated as 1000 ± 1000 Ma and 150 ± 150_°C with a

620 maximum allowed heating/cooling rate of 5_°C/Myr. Sampling proposed outside of the prior was prevented and more complex models were rejected for proposed models of equivalent likelihood. Therefore, t–T points were only accepted if they provided a better fit to the input data, which is a newer feature in QTQt that essentially prevents overly complex model paths from being accepted if they do not provide any benefit or improvement in data fit.

- 625 The long time interval for these model inversions are styled after a typical cratonic history and the only constraint that was consistently enforced was starting the model at $300 \pm 1^{\circ}$ C at 2000 ± 1 Ma. For our purposes, this scenario is considered a "no constraint" model, since we apply this as a starting condition for all inverse models well above the sensitivity of our thermochronology data. We also ran models that enforced constraint boxes (i.e., with either one or two boxes) at $20 \pm 10^{\circ}$ C at 1650 ± 100 Ma and $20 \pm 10^{\circ}$ C at 500 ± 50 Ma, requiring t–T paths to pass through them.
- 630 These t–T boxes were treated as "known" geologic information for the inversions and represent common geologic situations for cratons with Proterozoic and Phanerozoic basement nonconformities. However, these boxes purposefully represent an incomplete period of time at surface conditions with respect to the true thermal history, the repercussions of which will be discussed below in Section 5.2.
- 635 For all models presented hereafter, we show the QTQt Maximum Likelihood (ML; i.e., usually more complex, best fit t-T path to the observed data, red line) and Expected models (EX; i.e., ~weighted mean ± 95% credible interval; black lines) with respect to the true thermal history (white line) used to predict the synthetic data (Fig. 1). In our thermal history plots, the individual t-T paths are coloured by [log] path density, which is proportional to the relative probability, with higher intensity (brighter) colours denoting higher path density and higher relative
- 640 probability. Note that in Bayesian inference, the posterior probability is proportional to the likelihood multiplied by the prior, and in QTQt the prior acts as a penalty against making the model too complex and thus the Maximum Posterior (MP) model will <u>commonly</u> be the simpler t–T path when compared to the ML path (i.e., <u>equal or fewer t–</u> T points; Gallagher, 2012). We have excluded the MP model for plot clarity for most output because the ML and MP paths are identical or nearly so for most scenarios, which implies a well sampled and constrained ensemble of solutions (Gallagher and Ketcham, 2020).

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4. Model inversion results

QTQt inversion results are shown in Eigure 3 and examine the implications of multikinetic AFT, joint models with multikinetic AFT and AHe grains using the correct kinetics (i.e., the kinetics implemented during forward modelling

- to predict AHe ages), and different combinations of incorrect monokinetic AFT models where the three multikinetic populations were combined and treated as a single AFT sample and/or AHe ages were assumed to have the endmember fluorapatite r_{mu0} value. Figure 4 depicts the results comparing observed synthetic data and model predictions for the inversions in Figure 3. The first three models are "multikinetic AFT only" models (Fig. 3a-c), whereas the second row of models depicts results for three multikinetic AFT populations and three AHe grains (Fig.
- 665 3d-D. The last three panels are the single population AFT models (Fig. 3g-i). To reemphasize, we prevented t-T points from being accepted during QTQt inversions unless the addition of points provided better agreement between observed and predicted data. Therefore, all of our preferred results and discussion focus on the <u>ML</u> model t-T path since this path is the best fit to the data and is, in these instances, not unnecessarily complex, yet we show the <u>EX</u> model and 95% credible interval for comparison and to provide a general picture of the overall model ensemble.

670 4.1 AFT-only models _____identified multikinetic age populations and correct kinetics

The first model was setup to simultaneously invert each AFT kinetic population without AHe data for scenarios with a "no constraint" model, a "single t–T constraint" model, and "two t–T constraints" model (Fig. $3a_{\overline{x}}$ Q). These simulations were meant to be the ideal case using a lone AFT chronometer with extended thermal sensitivity due to the presence of multikinetic apatite populations. We investigated the ability of QTQt to recover the true thermal

- 675 history using properly identified kinetic age populations while utilizing the <u>fixed</u>, true r_{mr0} value from forward modelling for each population under varying degrees of geologic assumptions or constraints. The general shape, timing, and magnitude of the true history form and peak temperatures are recovered for the multikinetic AFT models regardless of whether or not constraint boxes were used. This suggests to us that the combination of high-quality, distinct age and length populations enhance t–T history resolving power, which becomes progressively improved if
- 680 kinetic populations sample a broad range of kinetic space (predicted AFT parameters closely agree with the synthetic data; Fig. 4a-c).

4.2 AFT + AHe models $__$ consequences of the r_{mr0} parameter

The addition of the three AHe <u>ages</u> using their *correct* kinetics (i.e., r_{mr0} values) along with the three multikinetic AFT populations (Fig. 3d) marginally improved thermal history recovery with respect to the AFT-only models (Fig. 3a-c), while the addition of two constraint boxes produced a ML model t-T path that reproduced nearly all features of the true thermal history (Fig. 3c). Figure 3c is the best thermal history model that utilized all assumptions and

information used during forward model generation of the synthetic dataset and provides the closest fit to the synthetic data (Fig. 4c). Setting all three AHe grains to 0.83 r_{mmb} produces distortion of the ML model history with respect to the true history (Fig. 3f). The model predicts three AHe ages that are virtually identical but provide a poor fit to the input synthetic AHe ages (Fig. 4f). The 610 Ma AHe grain (true kinetic r_{mm0} value = 0.83) was on the

margin of acceptability. However, in this case the overall group of model paths is still similar to the other "AFT-

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740 only" and "correct kinetics AHe" models simply because the multikinetic AFT populations are the primary controls on the t-T history (i.e., exert more influence and contain more thermal information), and without them, the model ensemble would instead be highly inaccurate (e.g., Fig. 3i; see below).

4.3 Monokinetic AFT models ____incorrectly combined kinetic populations

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- In our experience, multikinetic behaviour is not uncommon for basement samples characterized by complicated 745 burial histories and nearly always present for detrital apatite samples derived from complex source areas that experience multiple heating events. In our "monokinetic" scenario, the multikinetic AFT data were incorrectly treated as a single population and modelled using the central age, MTL, and average eCl (or $r_{mr0}) \pm 1\sigma$ of the *entire pool* of synthetic single-grain ages. As previously mentioned, combining the three populations caused the sample to fail the chi-square test (X² = 0.0) and the calculated AFT central age was 934 ± 64 Ma, the overall MTL was 14.07 ±
- 750 1.40 μm (n = 225), and the average eCl is 0.213 ± 0.373 apfu for all grains (equivalent $r_{mr0} \approx 0.75$), AFT data are usually treated as such in the published literature and overdispersed data are often modelled regardless of χ^2 statistics. This situation could conceivably occur when the three kinetic populations were either ignored or there was insufficient kinetic parameter resolution to identify discrete kinetic groups. A sample could also simply not be multikinetic but the models here are meant to illustrate the hazards of monokinetic misinterpretation for thermal
- 755 history analysis. In the monokinetic simulation without constraints, both the ML and EX t-T paths do not accurately reproduce the true thermal history (Fig. 3g). In this instance the ML path simply passes through both true thermal maxima, and yet yields excellent fits to the observed synthetic data (Fig. 4g). The addition of two constraint boxes produced even more complex and highly inaccurate t-T solutions (Fig. 3h) and reproduce well the observed AFT data (Fig. 4h). The AFT sample was modelled as monokinetic again (Fig. 3i), but also included the three AHe ages
- 760 using uniformly applied default RDAAM r_{mr0} value of 0.83 for each apatite grain to provide further insight into whether this combination could yield a better outcome just from the addition of more data for the inversion. The EX model is still inaccurate but the addition of AHe grains made the ML path simpler, nevertheless it poorly reproduces the true thermal history. The true AHe apparent ages were not well reproduced and the same age was predicted for all three grains (Fig. 4). This may be because the second 610 Ma AHe grain utilized the true r_{mr0} value of 0.83 from
- 765 the forward modelling and was the best-predicted age of the three (close to the observed age upper uncertainty limit) and dominated the iterative sampling during the inversion. The AHe kinetics produced forward model ages that were distinctly older (819 Ma) and younger (585 Ma) than the (middle) 610 Ma grain but these were unable to be reproduced by the inverse model assuming incorrect r_{mr0} kinetics.

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5. Discussion

5.1 Apatite composition and multikinetic interpretation

The AFT and AHe modelling results presented here may seem intuitive based on the implemented kinetics and modelling exercises using synthetic <u>data but</u> are worth discussing, since situations where highly variable apatite compositions could influence thermochronometric <u>ages</u> are likely to be encountered in natural samples. The results shown here indicate the benefits offered by interpreting intrasample AFT kinetic populations for inverse modelling and also show how inappropriate assumptions regarding kinetic parameters can greatly influence model outcome. Our examples were determined for a single, distinct thermal history, and yet they establish that apatite composition



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and multikinetic interpretation (when appropriate) provide valuable information for thermal history modelling — 845 and are mostly unexplored, or at least underutilized by routine AFT studies,

Collection of elemental data and interpretation of multikinetic samples is particularly important for providing greater t-T resolution (Fig. 3a-0), whereas combining or overlooking kinetic populations effectively smears the t-T signal contained in the individual kinetic groups and produces a meaningless hybrid thermal history model (Fig. 3a-0). We

- 850 could disregard these incorrect model simulations as self-fulfilling due to forward modelling a synthetic dataset and assuming "perfect" kinetic models, however for real scenarios we would not know the true thermal history and without other information, this class of results could be interpreted as geologically meaningful. Perhaps more important are the broader implications for thermal history modelling if there are inappropriate assumptions regarding data interpretation and certain steps are not taken to fully evaluate multikinetic AFT samples (Fig. 3g-j).
- 855 especially at longer timescales where there is greater uncertainty and less geologic control. An important point is that if multikinetic populations exist and are properly interpreted, they have the potential to constrain a much broader range of t-T space than an incorrect monokinetic (single population) interpretation for an overdispersed AFT sample. Many readers may appreciate that assuming or inadvertently 'forcing' the wrong model is a problem, but this remains a highly reviewed topic (e.g., Vermeesch and Tian, 2014; Fox et al., 2019) and is seemingly

860 underexplored in studies, as multikinetic-focused literature remains practically negligible in the >20 years since multikinetic models were introduced. Gallagher and Ketcham (2020) also touch on these points in response to the lengthy modelling discussion sparked by Vermeesch and Tian (2014) and are the primary themes of this work. **Deleted:** Gallagher and Ketcham (2020) also touch on these points in response to the lengthy modelling discussion sparked by Vermeesch and Tian (2014) and are primary themes of this work. .

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Figure 4: QTQt inversion predictions compared to "observed" synthetic thermochronology data generated during forward modelling. Panel letters correspond to counterpart t–T model panels in Figure 3. All predictions are for the Maximum Likelihood models. Squares are observed AFT central age $\pm 2\sigma$, circles are predicted AFT age, diamonds are observed MTL $\pm 1\sigma$, and X-symbols are the predicted MTL. Individual model fits to each track length distribution for the AFT kinetic populations are also shown and color-coded the same as Figure 2. Observed apatite He ages shown by red H-symbol (spans the 1 σ error range quoted in the text) and predicted AHe ages are black bars. Panel E with star is our best model that accounts for all multikinetic AFT populations and utilizes the true AHe kinetics and two geologic constraints, all combined for the highest thermal history resolution. Note: track length distributions are arbitrarily placed next to their respective age population and were not plotted with respect to the MTL plot axis.

5.2 Data quality and kinetic parameter influence on t-T resolution

The overall temporal and thermal resolution contained in multikinetic AFT data is influenced by multiple factors such as, the amount and distribution of the data (i.e., if the majority of the data are contained in one population versus distributed more equally), thermal history (i.e., the magnitude and sequence of heating-cooling events), and kinetics (i.e., the range of temperature sensitivity). A greater number of different kinetic groups are sensitive to an

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<u>expanded t-T range than a single population.</u> However, the ability to recover thermal history information depends on the details of the thermal history; if maximum temperatures occur late in the history then previous events are thermally overprinted and the early history is obscured or erased entirely. We intentionally use an ideal synthetic dataset with well-defined kinetic populations that have an equal distribution of data across all populations. Natural 900 populations may have an uneven distribution of grains and therefore populations that contain the most data will best

- resolve distinct parts of the thermal history. Our QTQt inversions demonstrate the ability of these data to inform t–T modelling in the context of variable kinetics and different modeller assumptions. The similarity between Expected models that do and do not require paths to pass through explicit t–T boxes (e.g., Fig. 3a–c) is informative for general modelling practices using Bayesian methods. This tells us that the multikinetic data being inverted have enough
- 905 sensitivity to resolve the general t-T history without <u>necessarily</u> requiring explicit conditions imposed on the t-T search. This is perhaps unexpected, as the Bayesian sampling implemented by QTQt generally favours simpler models over complex ones, which is a possible deterrent for users investigating deep-time thermal histories (McDannell and Flowers, 2020). However, this should not preclude the use of QTQt for deep-time problems, as the addition of thermochronological data augments inferences regarding thermal-history complexity.
- 910

<u>However</u>, enforcing constraints while utilizing fewer chronometers and ignoring data complexity or <u>multikinetic</u> <u>trends are detrimental to obtaining accurate t–T solutions</u>. The main region of t–T space that proved difficult to resolve in all models was the prolonged periods at low temperature. This was anticipated since the kinetic models and chronometers themselves are rather insensitive to temperatures < 50°C. The EX model may define an envelope

- 915 that seems consistent with the known true history (Fig. 3a-c), however this does not take into account the form of individual thermal histories that may be inconsistent with the true history. There were individual paths that were more similar to the true history for these three simulations, yet they avere considered lower relative (posterior) probability due to constraint box placement. We may expect this compromise between accuracy (i.e., closer to the true solution) and precision (i.e., greater certainty) because subsequent heating event(s) erase t-T information and
- 920 the earlier or older, low-temperature parts of the history will be less and less resolvable with additional reheating and thus may require constraint boxes to focus the t–T search. However, imposing 'uncertain' constraints, or constraints that do not fully capture the geologic record where the model is less sensitive leads to exclusion of (potentially viable) solutions and tightens the 95% credible interval. These results suggest that data quantity, quality, and the use of t–T constraint boxes variably trade-off with one another and the validity or uncertainty of geologic constraints

925 should be carefully considered and tested for natural samples since model results are conditional on these factors,

Figure 3c shows the ideal case with the most accurate thermal history recovery (nearly identical to the true history) when two constraint boxes are implemented with three interpreted AFT kinetic populations and three AHe grains modelled using the proper kinetics. Importantly, this applies in the case of integrating multiple low-temperature 930 thermochronometers and/or multikinetic AFT data, especially multikinetic populations that progressively diverge in kinetics, therefore increasing thermal resolution. However, constraint boxes provide no obvious advantage when the three multikinetic populations are ignored and only the overall central AFT age is modelled (Fig. 3h). In light of

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965 the aid of constraints from geological evidence." This statement alludes to the non-uniqueness of t-T models and certainly applies in situations where a single AFT age population is modelled, or more generally when only one thermochronometer is used to elucidate complicated t-T histories. However, we propose that multikinetic AFT interpretations (or more generally, integration of independent information from multiple chronometers) demonstrate

- 970 that their view does not always apply, as we can see illustrated in Figure 3a. Green and Duddy (2020) also go on to state that slow, continuous cooling is often assumed in published thermal history models (seemingly referring to QTQt models) and that this is inappropriate. Of course, ignoring geologic information and blindly inputting thermochronology data into modelling software will always yield inappropriate thermal histories and there is nothing preventing the user from doing this. However, model simulations such as the one that we show in Figure 3g
- 975 tell us that the wrong model may *imply* slow monotonic cooling, although it is not outright assumed, whereas our examples that utilize high-quality data (Fig. 3a–e) demonstrate that universal slow cooling assumptions are invalid. Monotonic-cooling solutions that faithfully reproduce the observed data (Fig. 3g and Fig. 4g) are not necessarily correct and are a product of attempting to recover a complex history with low-resolution data and/or incomplete geologic information about the true history.

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- We show additional QTQt models in Figure 5 to further establish the utility of modelling AFT grain populations with different annealing kinetics and the distinct temperature sensitivity provided by each kinetic group. These is simulations were carried out for each kinetic population individually and utilizing their true kinetics to demonstrate the sensitivity of each population to the multiple heating and cooling events present in the true forward history. The
- 985 model in Figure 5a demonstrates that population one is only sensitive to post_l Ga cooling and the second reheating a event, whereas the model in Figure 5b shows that population two is only sensitive to peak temperatures achieved a during the first heating event. Population three is sensitive to the initial cooling from high temperature and requires some poorly resolved reheating to partially reset the AFT age and match the track length distribution. The high retentivity of population 3 makes it mostly insensitive to the two heating and cooling cycles. Each of these
- 990 simulations illustrate that a single AFT population lacks sufficient t-T information to adequately resolve the (entire) true thermal history, yet when each kinetic population is combined and modelled simultaneously (Fig. 3), their consolidated sensitivities enhance recovery of the true t-T solution,



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Figure 5: QTQt models of each individual AFT kinetic population plotted with respect to the true thermal history. (a) Kinetic population one (b) Kinetic population two (c) Kinetic population three. The magenta dashed line indicates the approximate sensitivity of each kinetic population within the overall model history (also see Fig. 6b retention ages). All other explicit boundary conditions are the same as previous models.

5.3 Comparison with nondirected Monte Carlo t-T simulation

Multikinetic AFT data may record complicated thermal histories that are difficult to simulate using classical randomized Monte Carlo algorithms and model success can depend strongly on the choice of boundary conditions that are used to limit the model search space. The synthetic AFT data were inversely modelled using the newest version of AFTINV (Issler, 1996), a derivative of the Willett (1997) model that is similar to the HeFTy software (Ketcham, 2005) in using a nondirected Monte Carlo scheme and *p*-values to generate and evaluate thermal histories. Unlike HeFTy, AFTINV uses fixed, user-specified time points of arbitrary spacing and generates thermal histories by randomly selecting heating and cooling rates to calculate temperature points forward and backward in

- 1080 time. Thermal histories are constructed by piecewise assembly of different thermal history styles (e.g., heating or cooling only, or heating/cooling cycles) that are separated by randomly-selected thermal minima within user-specified time ranges that incorporate uncertainty in the time of deposition or onset of reburial. Monte Carlo calculations are performed to obtain a set (typically 300) of solutions exceeding the 0.05 level of significance and then a controlled random search (CRS; Price, 1977) learning algorithm is used to update the solution set to the 0.5
- 1085 level. Up to four different AFT kinetic populations can be modelled simultaneously. Failure to find any solutions at the 0.5 level may indicate a problem with the boundary conditions, the style of thermal history, or incompatibilities among the kinetic populations and further investigations should be undertaken to determine the source of the problem.
- 1090 Model sensitivity runs were undertaken to determine the boundary conditions needed to obtain close fitting solutions and Figure 6 shows the final preferred model results obtained from the CRS calculations. Previous models that used broad rate limits required millions of trial model solutions that produced a wide range of marginally acceptable solutions (0.05 level) that could not be updated by the CRS algorithm to produce the narrower thermal peaks needed to closely fit the AFT data at the 0.5 level. Limiting the heating/cooling rates to 0.2 °C/Myr from 1700 Ma to 1200
- 1095 Ma and 1 °C/Myr for the post-1200 Ma history improved model performance dramatically and yielded 44 solutions at the 0.5 significance level (dark gray lines; Fig. 6a). These limits kept temperatures closer to surface conditions prior to the first heating event and eliminated spurious temperature fluctuations associated with rates that are much higher than those used to generate the synthetic data (Fig. 1). Unlike the QTQt model results of Figure 3, all individual thermal histories in Figure 6a provide statistically significant fits to the AFT data. The minimum
- 1100 objective function solution (green curve; Fig. 6a) provides the closest fit to the AFT age and length data (Fig. 6c). The exponential mean of all 300 solutions (blue curve; Fig. 6a) provides acceptable fits for kinetic populations two and three but fails to fit population one lengths due to insufficient annealing; the wide range of permissible solutions for the low temperature peak results in an exponential mean peak temperature that is lower than cach of the individual solutions. Retention ages (Fig. 6b) are model ages representing the oldest track (approximately 2 µm) in

Deleted: Multikinetic AFT-only QTQt models without constraint boxes and same inversion setup as figure 3A-C. (A) QTQt run where more complex models were allowed. (B) Inversion where noise was added in the form of \pm 0.05 apfu to the kinetic parameter. (C) Inversion where kinetic population two was ignored. ...

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each population and they indicate the approximate times when thermal history information is retained by each AFT
 population. Population one retention ages are younger than thermal peak one, implying total annealing and accumulation of new tracks after the peak one maximum temperatures. Population two shows a bimodal retention age distribution indicating that some solutions have tracks with older retention ages that were not reset during the first cycle of heating. The very old population three retention ages suggest that tracks were retained at temperatures > 290 °C.



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Figure 6: (a) AFTINV software thermal history inversion results using random MC and the CRS algorithms (e.g., Willett et al., 1997; McDannell et al., 2019b). Model in (a) was set up to find 300 random MC solutions at the 0.05 fit level (not shown), which are then used as a 'seed' pool for the CRS algorithm to iteratively recombine and refine the solution set to the better 0.5 statistical fit level. In this example, not all solutions reached the 0.5 significance level (only 44 did; dark gray lines) and are therefore ≥ 0.05 level (light gray lines). The exponential mean t–T path is shown for all 300 solutions (blue line) along with the 'minimum objective function' or overall best-fit solution (green line). (b) Retention ages, or hypothetical age of the oldest retained fission tracks for each kinetic population. Retention ages give a rough sense of temperature sensitivity. (c) Track length distribution model fits for the exponential mean and minimum objective function t–T paths for each kinetic population. Observed versus predicted goodness-of-fit (GOF) for AFT age and track length for the min. obj. function solution. See McDannell et al. (2019b) for further discussion of AFTINV modelling methods.

The above results show that the ability to find solutions that fit multikinetic AFT data will depend on the choice of modelling strategy and how it is implemented. QTQt uses systematic random sampling where the next sample is dependent on the existing one — to ultimately refine solutions as the model evolves and it can perform well with broad boundary conditions. Models like HeFTy and AFTINV use a nondirected Monte Carlo scheme that may require more stringent boundary conditions to force the model to sample more favourable areas of solution space and require iterative modelling to adjust boundary conditions to obtain good-fitting solutions. A key point is that

1185 both MCMC and nondirected MC methods yield similar results, but purely random MC methods need more user input to assist the software in finding an answer. Therefore, even if kinetic populations are assigned correctly, if the thermal history style (i.e., number of heating/cooling events), values of kinetic parameters, and/or boundary conditions are incorrect, the inability to find good-fitting model solutions may be erroneously attributed to the wrong cause (e.g., input data).

1190 6. Conclusions

Using synthetic <u>multikinetic AFT (and AHe data)</u> derived from forward modelling, we show that, under ideal conditions, it is possible to extract multi-cyclic heating and cooling history information <u>using inverse modelling</u> methods when kinetic parameters for AFT annealing are correctly specified. Essential details of a two-phase heating and cooling history are reproduced using AFT multikinetic data alone without imposing constraint boxes but the

- 1195 closest fit to the true solution is achieved using all the synthetic data with constraint boxes. Alternative monokinetic interpretations that ignore multikinetic behaviour generate solutions that significantly depart from the true solution while providing close fits to the interpreted AFT data; under these conditions, imposing constraint boxes can <u>further</u> <u>degrade modeled</u> t–T solutions with respect to the true thermal history style and the timing and magnitude of heating events, Within the context of our simulations and assumptions regarding helium diffusion kinetics, ignoring apatite
- 1200 composition (r_{m0} kinetic parameter) when it truly deviates from fluorapatite kinetics can cause observed AHe ages to be reproduced poorly and yield inaccurate model thermal histories. Therefore, if apatite composition does appreciably modify He diffusivity, this effect may be an additional, and unaccounted for, source of overdispersion in AHe datasets and disagreement between observed and modeled ages may be due to incorrect (kinetic) model assumptions rather than poor quality data. We recommend the routine collection of elemental data for apatite dated 1205 using the fission-track method as a means to better quantify sample chemical variation and relate this to kinetic
- behaviour for thermal history analysis. Elemental data may also prove useful to characterize first-order

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"thermochronology data in isolation cannot define periods when samples were cooler and subsequently reheated. This can only be defined with the aid of constraints from geological evidence." This statement alludes to the non-uniqueness of t-T models and applies in situations where a single AFT age population is modelled, or more generally when only one thermochronometer is used to elucidate. [8]

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compositional variation in AHe datasets. The use of r_{mr0} , while imperfect, still provides the best resolution for kinetic interpretation when compared to other kinetic proxies. The ability to recover high-resolution thermal histories from natural multikinetic AFT samples depends on the details of the thermal history and characteristics of

1405

the data_{xx}These topics are discussed more fully in a future companion paper that examines detrital AFT samples from Yukon, Canada to illustrate multikinetic AFT interpretation and modelling methods_{xx}

7, Appendix

The appendix contains the true thermal history and the synthetic AFT data set. See the main text for further details.

8. Author Contributions

1410 KTM designed research and performed <u>QTQt</u> modelling. DRI <u>performed AFTINV modelling and</u> was involved in conceptual discussions and model evaluation. KTM and DRI wrote the paper.

9. Competing interests

The authors declare that they have no conflict of interest.

10, Acknowledgements

1415 These ideas were developed while KTM was a postdoc at the Geological Survey of Canada and supported by the Natural Resources Canada Geo-mapping for Energy and Minerals (GEM) Program. The authors graciously thank Kerry Gallagher, Rich Ketcham, and an anonymous reviewer for thoughtful comments to improve the clarity of this manuscript and Noah McLean for efficient editorial handling and correspondence. K. Gallagher is also acknowledged for making changes to QTQt specifically for these modelling exercises. KTM thanks his partner

1420 Jennifer for all of her help during the writing of this manuscript. <u>NRCan contribution number 20200758</u>.

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Figure Captions

Figure 1: Thermal history used to predict synthetic AFT and AHe data. This t–T path is referred to as the "true" thermal history throughout this paper. The predicted synthetic data were then used as input for QTQt to recover the thermal history through inverse modelling. PAZ = partial annealing zone for fission tracks.¶ Figure 2: Predicted synthetic AFT data from the thermal history in figure 1. Multikinetic age populations were individually predicted using distinct r_{mr0} kinetics shown in (B) panels (discussed in the text). These data were then input in QTQt and inverted in an attempt to recover the true thermal history in figure 1 (see fig. 3). (A) Central age and 1σ errors are indicated for each kinetic population. Kinetic populations one, two, and three are displayed as arms on their respective radial plots, with individual AFT ages closer to the origin being less precise. The last radial plot shows all thirty individual grains and demonstrates that when taken together, the combined sample fails the χ^2 test (p < 0.05) for homogeneity (i.e., that all grains belong to a single underlying age population) suggesting multiple age populations. This is the scenario most researchers would start with before evaluating the sample for potential multikinetic behaviour. Mixture modelling was subsequently performed on the combined sample and the model age peaks that were picked seamlessly align with the individual kinetic population central ages. This aligns with how populations would be defined and compared with the elemental chemistry for individual defined and compared with the elemental chemistry for individual age grains during multikinetic interpretation. (**B**) The predicted track length distributions for each kinetic population from the thermal history in Figure 1 using the specified kinetic parameter value. The last panel on the right combines all tracks from each kinetic population. Numbers on the histogram are the number of tracks in each μ m bin. Abbreviations: eCl = effective Cl; MTL = mean track length.

Figure 3: Thermal history inversion results from QTQt under different imposed kinetic and t-T assumptions. (A-C) show the "AFT only" models that utilized three multikinetic AFT populations (discussed in the text) as the only input data. The true t_{max} kinetics applied during forward modelling were entered in the input files and held fixed for each kinetic population during the inversion. (D-E) show the results of models that correctly utilized three multikinetic AFT kinetic populations and three AHe dates all with the true kinetics held fixed. Panel E is the best model inversion incorporating all correct thermochronometer information used during forward modelling of the synthetic data set. The panel (F) model was completed under the same conditions as panels (D-E) except that the three AHe grains all employ the incorrect (in the oldest and youngest cases) RDAAM default fluorapatite t_{may} value of 0.83 as the kinetic parameter. Panels (G-I) were modelled assuming a "monokinetic" or traditional single population AFT sample that combines all three multikinetic population mode lest fit) t-T path from QTQt; dashed gray lines are the Expected model (-T path with light gray 95% credible interval envelope. Assumed t-T constraints are black boxes that require thermal histories to pass through them during the inversion.⁹ ... [11]

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