

Modeling apparent Pb loss in zircon $^{206}\text{Pb}/^{238}\text{U}$ geochronology

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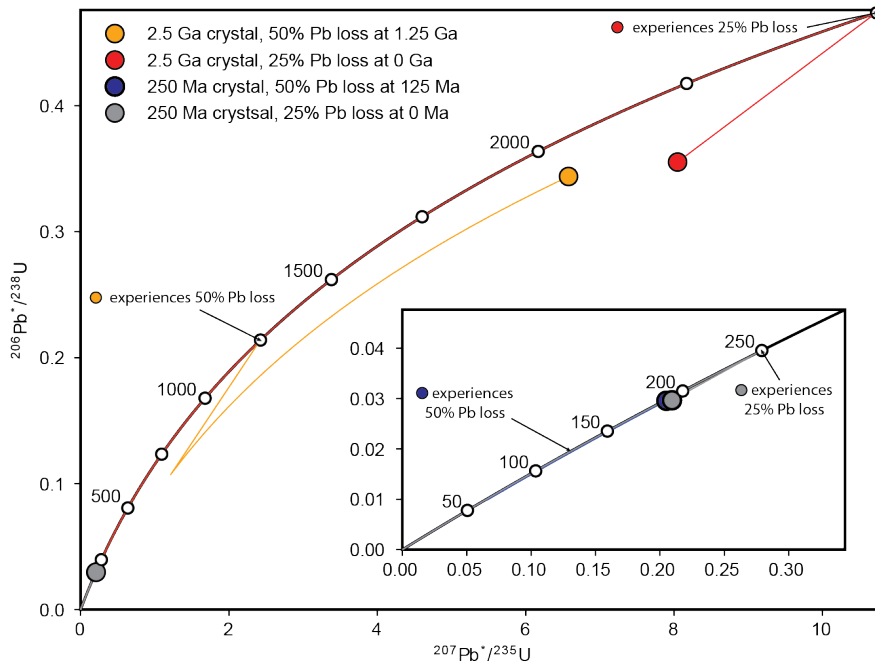
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Abstract. ~~Because~~ The loss of radiogenic Pb from zircon is known to be a major factor that can cause inaccuracy in the $^{206}\text{Pb}/^{238}\text{U}$ geochronological system, hence there is a need to better characterize the distribution of Pb loss in natural samples. Treatment of zircon by chemical abrasion (CA) has become standard practice in isotope dilution-thermal ionization mass spectrometry (ID-TIMS), but CA is much less commonly employed prior to *in-situ* analysis via laser ablation-inductively coupled plasma-mass spectrometry (LA-ICP-MS) or secondary ionization mass spectrometry (SIMS). Differentiating the effects of low levels of Pb loss in Phanerozoic zircon with relatively low precision *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ dates, where the degree of Pb loss is insufficient to cause discernible discordance, is challenging. We show that $^{206}\text{Pb}/^{238}\text{U}$ isotopic ratios that have been perturbed by Pb loss may be modeled by convolving a Gaussian distribution that represents random variations from the true isotopic value stemming from analytical uncertainty with a distribution that characterizes Pb loss. We apply this mathematical framework to model the distribution of apparent Pb loss in 10 igneous samples that have both non-CA LA-ICP-MS or SIMS $^{206}\text{Pb}/^{238}\text{U}$ dates and an estimate of the crystallization age, either through CA $^{206}\text{Pb}/^{238}\text{U}$ or $^{40}\text{Ar}/^{39}\text{Ar}$ geochronology. All but one sample showed negative age offsets that were unlikely to have been drawn from an unperturbed $^{206}\text{Pb}/^{238}\text{U}$ date distribution. Modeling apparent Pb loss using the logit-normal distribution produced good fits with all 10 samples and showed two contrasting patterns in apparent Pb loss: samples where most zircon $^{206}\text{Pb}/^{238}\text{U}$ dates undergo a bulk shift and samples where most zircon $^{206}\text{Pb}/^{238}\text{U}$ dates exhibited low age offset but fewer dates had more significant offset. Our modeling framework allows comparison of relative degrees of apparent Pb loss between samples of different age, with the first and second Wasserstein distances providing useful estimates of the total magnitude of apparent Pb loss. Given that the large majority of *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ dates are acquired without the CA treatment, this study highlights a pressing need for improved characterization of apparent Pb loss distributions in natural samples to aid in interpreting non-CA *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ data and to guide future data collection strategies.

1 Introduction

Zircon $^{206}\text{Pb}/^{238}\text{U}$ geochronology is arguably one of the most important radiometric dating approaches used by geoscientists, with widespread application to constraining the age of Pleistocene and older geologic materials (Davis et al., 2003; Schoene,

30 2013; Gehrels, 2014). We rely on zircon $^{206}\text{Pb}/^{238}\text{U}$ dates for calibrating the geological time scale (e.g., Compston, 2000a;
 31 2000b; Bowring and Schmitz, 2003; Gradstein et al., 2004; Kaufmann, 2006), constraining the timing of important Earth
 32 history events (Froude et al., 1983; ~~Schoene et al., 2010~~; Burgess et al., 2014), and determining the rates of Earth processes
 33 (Rioux et al., 2012; ~~Schoene et al., 2012~~; Johnstone et al., 2019). The zircon $^{206}\text{Pb}/^{238}\text{U}$ geochronometer is particularly
 34 powerful due to the ability to assess agreement between the $^{238}\text{U} \rightarrow ^{206}\text{Pb}$ and $^{235}\text{U} \rightarrow ^{207}\text{Pb}$ decay chains, with $^{206}\text{Pb}^*/^{238}\text{U}$ and
 35 $^{207}\text{Pb}^*/^{235}\text{U}$ dates in agreement plotting on the Concordia line, where * indicates radiogenic Pb (Wetherill, 1956).
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 38
 39 **Figure 1. Illustration of the influence of Pb loss on 250 Ma and 2.5 Ga zircon. Two Pb**
loss scenarios are shown: 25% loss at half the age of the zircon and 50% loss at
present-day (0 Ma). The approximately linear nature of the $^{206}\text{Pb}^*/^{238}\text{U}$ vs $^{207}\text{Pb}^*/^{235}\text{U}$
Concordia line near the origin results in Pb loss producing limited discordance if the
Pb loss occurs within several 100s of Myr of crystallization. Note that a greater amount
of ancient Pb loss is required to produce the same shift in $^{206}\text{Pb}^*/^{238}\text{U}$ relative to recent
Pb loss. Thin, colored lines represent the path of each zircon.

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 38
 39 The causes and complications of open system behavior (e.g., radiogenic Pb loss) in zircon have long been a topic of study
 40 (Tilton et al., 1955; Pidgeon et al., 1966). Although Pb loss events may be discerned on $^{206}\text{Pb}/^{238}\text{U}$ Concordia diagrams in
 41 some circumstances and can provide useful geologic information about the thermal and/or fluid flow history of a region (Silver
 42 and Deutsch, 1963; Blackburn et al., 2011; Morris et al., 2015; Kirkland et al., 2017), recognizing Pb loss remains a challenge
 43 when it occurs within several 100's Myr of crystallization (Fig. 1; Anderson et al., 2019). For example, due to the shape of the

44 $^{206}\text{Pb}^*/^{238}\text{U}$ versus $^{207}\text{Pb}^*/^{235}\text{U}$ Concordia line, Pb loss in Phanerozoic zircon results in a ‘sliding along concordia’ effect that
45 can make Pb loss difficult to discern, particularly in relatively low-precision *in-situ* (i.e., LA-ICP-MS or SIMS) datasets when
46 the Pb loss produces concordant or only modestly discordant analyses (e.g., <10%; Ashwal et al., 1999; Bowring and Schmitz,
47 2003; Ireland and Williams, 2003; Reimink et al., 2016; Spencer et al., 2016; Watts et al., 2016; Anderson et al., 2019). Such
48 low levels of Pb loss have been termed ‘cryptic’ and may be associated with spatial heterogeneities including radiation-
49 damaged U-rich zones and microstructures (Nasdala et al., 2005; Kryza et al., 2012; Watts et al., 2016). Although there are
50 many potential causes of Most-Pb loss in zircon, open system behavior is often associated with elevated α -dose and associated
51 metamictization likely a consequence of recrystallization or Pb transport in crystals with severe radiation damage and exposure
52 to hydrothermal alteration (Silver and Deutsch, 1963; Pidgeon et al., 1966; Mezger and Krogstad, 1997; Cherniak and Watson,
53 2001; Marsellos and Garver, 2010). Mechanisms for Pb loss ~~may include~~ recrystallization of metamict zircon during
54 metamorphism (Kröner et al., 1994; Mezger and Krogstad, 1997; Orejana et al., 2015; Zeh et al., 2016) and, leaching of Pb
55 from metamict zones by hydrothermal alteration or (Geisler et al., 2002, 2003); diagenetic fluids or fluid flow (Geisler et al.,
56 2002, 2003; Willner et al., 2003; Morris et al., 2015; Kirkland et al., 2020); and/or during chemical weathering (Stern et al.,
57 1966; Black, 1987; Balan et al., 2001; Pidgeon et al., 2017; Andersen and Elburg, 2022). Pb loss is thought to primarily occur
58 at temperatures <250°C in which radiation damage in zircon is unable to be annealed over geologic timescales (Schoene,
59 2013).

60
61 Zircon domains that have lost Pb may be preferentially removed by first thermally annealing the zircon at high temperature
62 (e.g., 800-1100°C) and then partially dissolving the zircon in a heated HF solution in a technique called chemical abrasion
63 (CA) (Mattinson, 2005). The CA treatment is now routinely applied in ID-TIMS analysis and has contributed to both improved
64 precision and accuracy of CA-ID-TIMS U-Pb-U-Pb data (Schoene, 2013). Although some *in-situ* U-Pb-U-Pb laboratories
65 practice thermal annealing routinely (e.g., Allen and Campbell, 2012; Solari et al., 2015), CA has been applied much less
66 frequently (Crowley et al., 2014; von Quadt et al., 2014; Watts et al., 2016; Ver Hoeve et al., 2018; Ruiz et al., 2022). Several
67 studies that have conducted paired analysis of non-CA and CA of the same samples via *in-situ* U-Pb-U-Pb geochronology have
68 found the non-CA U-Pb-U-Pb dates to skew younger than the CA U-Pb-U-Pb dates (Crowley et al., 2014; von Quadt et al.,
69 2014; Watts et al., 2016). A growing number of maximum depositional age studies with tandem non-CA LA-ICP-MS and CA-
70 ID-TIMS dating have shown the youngest non-CA U-Pb-U-Pb dates tend to be younger than expected relative to CA U-Pb-U-
71 Pb dates or other geologic constraints, even when considering measurement uncertainty (e.g., Herriott et al., 2019; Schwartz
72 et al., 2022; Howard et al., 2022; Sharman et al., 2023). However, there is a lack of quantitative constraints on the relative
73 importance of Pb loss in influencing non-CA U-Pb-U-Pb date distributions acquired via *in-situ* mass spectrometry, particularly
74 as related to influencing depositional age constraints (Copeland, 2020).

75
76 This study builds upon past research on open system behavior in zircon by presenting a mathematical framework for
77 characterizing the distribution of apparent Pb loss on untreated (i.e., non-CA) U-Pb-U-Pb date distributions. We first suggest

78 that U-Pb isotopic ratios that have been perturbed by Pb loss may be viewed as the convolution of two signals: a Gaussian
 79 distribution that reflects measurement uncertainty about the true isotopic ratio and the distribution that characterizes Pb loss.
 80 We then apply this mathematical framework to model the distribution of apparent Pb loss that has affected 10 igneous samples
 81 of Miocene to Carboniferous age. Our results highlight the importance of quantifying distributions of apparent Pb loss
 82 magnitude to better understand the potential influence on non-CA zircon U-Pb date distributions.
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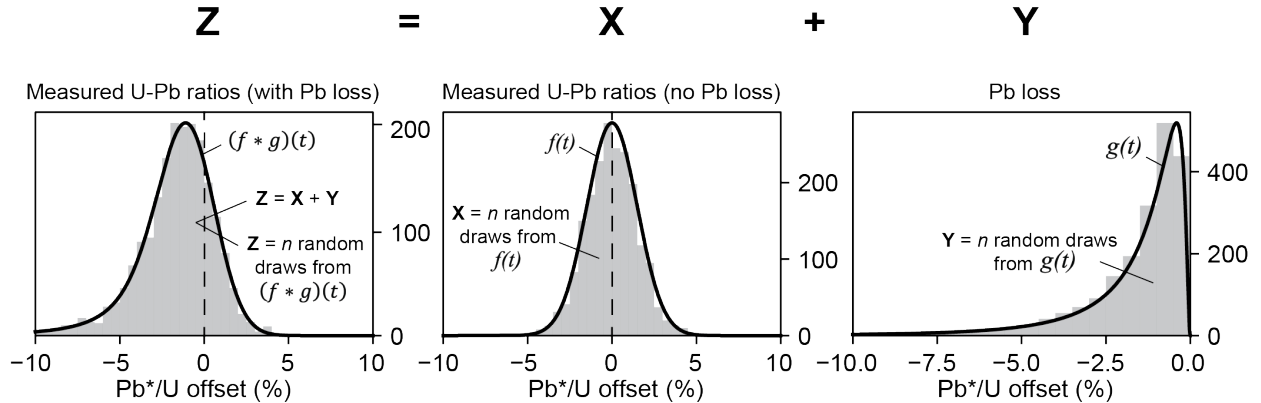


Figure 2. Illustration of how Pb*/U isotopic ratios from n zircon analyses that have been perturbed by Pb loss (Z) may be modeled as the summation of n non-perturbed Pb*/U ratios (X) and the amount of Pb loss encountered by each (Y). X is drawn from $f(t)$ that reflects the Gaussian distribution of Pb*/U ratios that are unperturbed by Pb loss and Y is drawn from $g(t)$ that represents the distribution of Pb loss in the sample. The distribution that characterizes Z may be found by convolving $f(t)$ and $g(t)$. Although we assume that $f(t)$ is a Gaussian distribution, the distribution type of Pb loss, $g(t)$, shown in this example as a logit-normal distribution ($\mu=-4.5$, $\sigma=1.0$) could take a number of discrete or continuous forms (Fig. 3). Note that in our modeling framework, values of X , Y , and Z are normalized as percentage deviation from the true isotopic ratio (i.e., the mean of $f(t)$), where negative values indicate that measured Pb*/U is lower than the true ratio. See Supplemental Video 1 for an animation that illustrates the process of convolution and Supplemental Video 2 for an exploration of the logit-normal distribution in μ and σ parameter space.

84 2 Mathematical framework

85 A series of n Pb*/U measurements that have undergone Pb loss, Z , may be modeled as the sum of the corresponding
 86 unperturbed Pb*/U values, X , and the amount that Pb*/U changed due to Pb loss for each date, Y ,

$$87 \quad Z = X + Y \quad (\text{Equation 1})$$

88 where Z , X , and Y are all 1-D matrices with n values and units of percentage offset from the true isotopic value (Fig. 2).
 89 Because Pb loss produces a lower Pb*/U ratio, the values of Y must be negative in our formulation of Equation 1. If X is drawn
 90 from a Gaussian distribution $f(t)$ whose mean (μ) approximates the true isotopic value and whose standard deviation (σ) reflects
 91 dispersion from the true value related to measurement uncertainty (e.g., Schoene, et al., 2013) and if Y is drawn from a
 92 distribution that reflects Pb loss, $g(t)$, then Z may be viewed as being drawn from the convolution of $f(t)$ and $g(t)$

$$93 \quad (f * g)(t) = \int_{-\infty}^{\infty} f(\tau)g(t - \tau)d\tau \quad (\text{Equation 2})$$

94 provided that X and Y are independent (Fig. 2; Supplemental Video 1). Convolution simply represents the summation of two
 95 random variables, in this case one related to analytical precision (i.e., random variation around the true isotopic value stemming
 96 from the measurement process) and the other related to the geologic process of Pb loss. We model Pb loss as percentage offset
 97 from the true Pb^*/U value rather than deviation in absolute time (i.e., Myr) to promote comparison of samples of different age
 98 (Fig. 2).

99

100 Equation 2 may be solved analytically for some forms of $f(t)$ and $g(t)$. For example, the convolution of Gaussian and
 101 exponential distributions is known as the exponentially modified Gaussian distribution (Grushka, 1972). However,
 102 $(f * g)(t)$ may also be solved numerically, which has the advantage of allowing both $f(t)$ and $g(t)$ to take any form.

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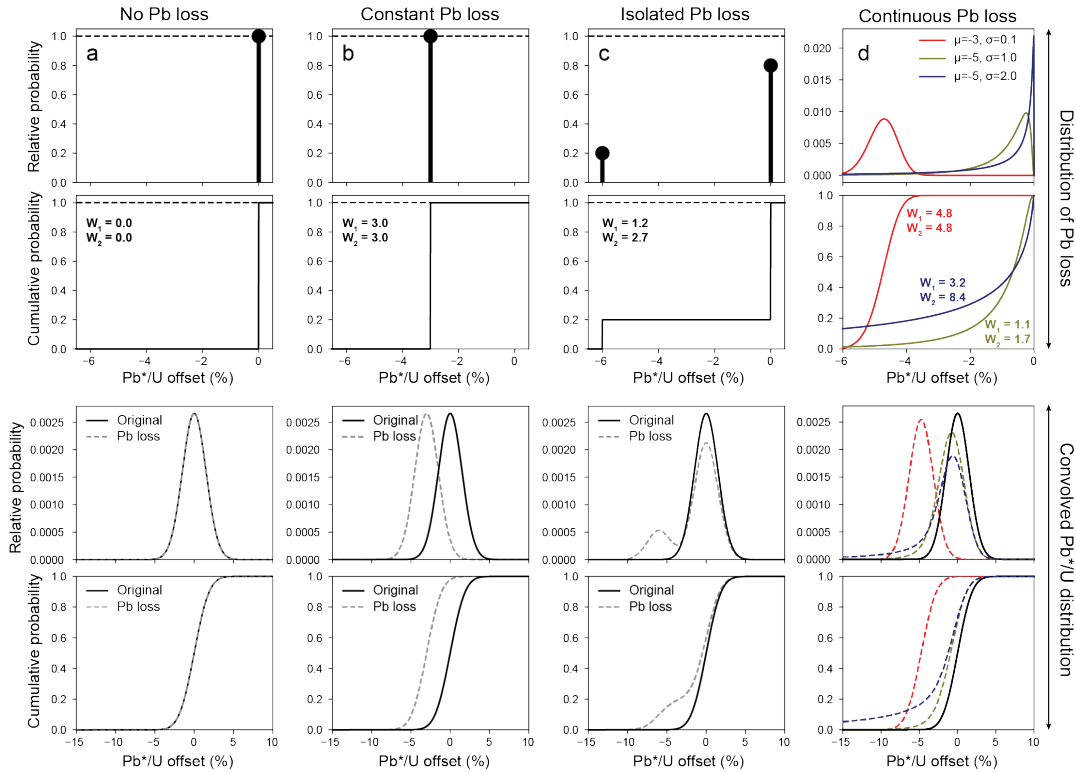


Figure 3. Illustration of how normally distributed zircon Pb^*/U values may be perturbed by discrete (a-c) or continuous (d) distributions of Pb loss. The top row represents the distribution of Pb loss in the sample expressed as a percentage of the true isotopic ratio (e.g., $^{206}Pb^*/^{238}U$ or $^{207}Pb^*/^{235}U$) at the time of Pb loss, where the height of the black bar and ball indicates the relative probability of the specified Pb^*/U offset. Three discrete scenarios are shown: a) no Pb loss, b) constant Pb loss, and c) isolated Pb loss. A logit-normal distribution is shown as an example of continuous Pb loss in d). Additional examples of continuous Pb loss distributions are shown in Figure A1. The bottom row shows both the relative (above) and cumulative (below) probabilities of the unperturbed (solid black line) and Pb loss-perturbed (dashed line) Pb^*/U distributions.

105

106 3 Methods

107 3.1 Modeling approach

108 We use the mathematical framework described above to model both the distribution of apparent Pb loss, $g(t)$, experienced by
109 a group of cogenetic crystals and their unperturbed U-Pb/U-Pb date distribution, $f(t)$. Because Pb loss is isotopically
110 indiscriminate, Equation 2 may be equally applied to $^{206}\text{Pb}^*/^{238}\text{U}$ and $^{207}\text{Pb}^*/^{235}\text{U}$. However, we model $^{206}\text{Pb}^*/^{238}\text{U}$ ratios as
111 these have much lower analytical uncertainty for the Carboniferous and younger samples analyzed in this study.

112
113 To model $g(t)$, we allow the μ of $f(t)$ to vary within the 95% confidence interval associated with an independent estimate of
114 the crystallization age. We then estimate both $g(t)$ and σ of $f(t)$ by iteratively solving for the combination of parameters that
115 minimize the misfit between the measured Pb^*/U values and the modeled distribution $(f * g)(t)$ using the Python
116 `scipy.optimize.minimize()` function. We define misfit as the sum of squared residuals between the empirical cumulative
117 distribution function (ECDF) of the measured Pb^*/U values and the cumulative density function (CDF) of the modeled Pb^*/U
118 distribution.

119
120 If both non-CA and CA analyses are available from the same sample, then the distribution of CA U-Pb/U-Pb dates may be
121 used to constrain the parameters of $f(t)$. For such samples, we modify the approach described above by first finding the
122 Gaussian distribution $f(t)$ that most closely approximates the treated Pb^*/U distribution. We then use this best-fitting $f(t)$ in
123 estimating $g(t)$ using the minimization-of-misfit technique described above. Such datasets have the advantage of providing
124 constraints on σ of $f(t)$, which is otherwise treated as an unknown parameter during modeling if only non-CA U-Pb/U-Pb dates
125 are available.

126
127 In order to estimate $g(t)$ as described above, we must choose one or more reasonable parametric models that are appropriate
128 for describing distributions of Pb loss. One possibility is that all zircon crystals in the sample experienced the same amount of
129 Pb loss, which could shift Pb^*/U from 0% to -100% of its value. Such a scenario of constant Pb loss may be modeled by a
130 discrete form of $g(t)$ where a single parameter specifies the percentage of Pb lost. Convolution of such a discrete form of $g(t)$
131 simply produces a negative shift in the Pb^*/U values (i.e., Fig. 3b).

132
133 Another possibility is that Pb loss was experienced by only a subset of crystals (i.e., isolated Pb loss). This scenario may also
134 be modeled by assigning $g(t)$ to a discrete distribution with two parameters: one that indicates the fraction of Pb lost and one
135 that specifies the proportion of crystals that underwent Pb loss (Fig. 3c). This parameterization of $g(t)$ will produce a bimodal
136 pattern in U-Pb/U-Pb values, particularly if the degree of Pb loss is significant relative to measurement uncertainty (Fig. 3c).

137

138 Instead of modeling $g(t)$ as a discrete distribution where Pb loss is restricted to certain values, we may also consider a
 139 continuous probability distribution where values of Pb loss can take on any value between 0% and 100% (Fig. 3d). Rather than
 140 assume *a priori* the form(s) that $g(t)$ might take, we considered a wide range of 1- or 2-parameter distributions for the purposes
 141 of exploratory modeling (Appendix A). Of the distribution types considered, we identified the logit-normal distribution, also
 142 known as the logistic normal distribution, as perhaps the most reasonable for modeling Pb loss. The logit-normal distribution
 143 has the property of having a logit (i.e., the quantile function of the logistic distribution) that is normally distributed with a
 144 geometric mean of μ and standard deviation of σ (Aitchison and Shen, 1980; Mead, 1965)

$$145 \quad f(x, \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \frac{1}{x(1-x)} e^{-\frac{(\text{logit}(x)-\mu)^2}{2\sigma^2}} \quad (\text{Equation 3})$$

146 for $0 < x < 1$. The logit-normal distribution is well-suited for modeling constrained data types (e.g., compositional data; Atchison
 147 and Bacon-Shone, 1999; Vermeesch, 2018b) in part due to it being defined
 148 over $0 < x < 1$. We invert and scale the distribution to extend from -
 149 $100\% < x < 0\%$ to match the sign and units of Pb*/U offset due to Pb loss
 150 when expressed as a percentage (Fig. 3d).

151
 152 Figure 4 explores the relationship of the logit-normal distribution to its
 153 two parameters (μ and σ) (see also Supplemental Video 2). The
 154 distribution has a ‘spiky’ character when σ is a very small number (e.g.,
 155 0.001; Fig. 4a), which would be a reasonable approximation for samples
 156 that underwent an approximately constant amount of Pb loss (e.g., Figs.
 157 3a and 3b). Although the logit-normal distribution cannot model 0% or
 158 100% Pb loss, these values may be approximated by making μ a large
 159 negative or positive number, respectively. A sample where most zircon
 160 exhibit very little Pb loss but with fewer zircon experiencing significant
 161 Pb loss could be produced by $\mu = -4$ and $\sigma = 1.0$ (Fig. 4c). Alternatively,
 162 a sample with a peak probability of Pb*/U offset $< 0\%$ may be modeled
 163 using moderate values of σ (e.g., 0.25-1; Figs. 4b and 4c). The logit-
 164 normal distribution produces bimodal distributions where most probability
 165 is close to 0% and -100% when σ values are high (e.g., $\gg 1$; Fig. 4d).

166 3.2 Samples

167 We apply the mathematical and modeling framework presented above to estimate the distribution of apparent Pb loss in 10
 168 igneous samples that range in age from Carboniferous to Miocene, nine of which have been published previously (Table 1).
 169 Samples CTU, RCP, and SRF are all from upper Eocene rhyolites of the Caetano caldera system of the western United States

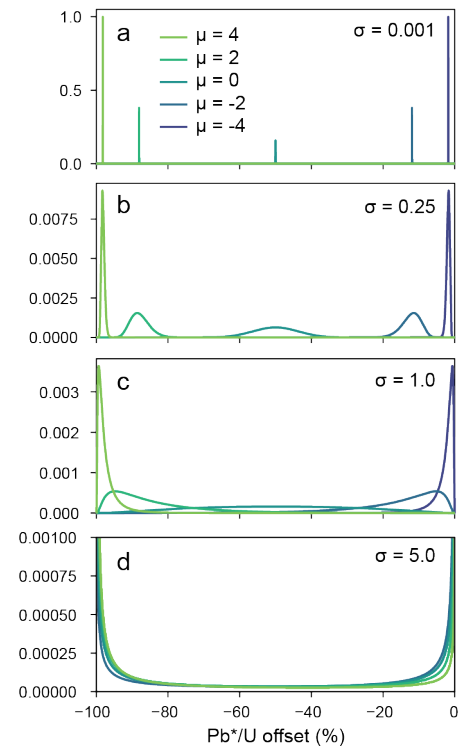


Figure 4. Exploration of the logit-normal distribution's parameter space. Note that we have rescaled the x-axis of the logit-normal distribution such that $-100 < x < 0$.

170 (Watts et al., 2016). These samples were split into non-CA and CA aliquots prior to analysis via SIMS (Watts et al., 2016).
 171 We used the error-weighted mean age of the CA $U-Pb/U-Pb$ dates as an estimate of the true crystallization age for each sample,
 172 with weighted means approximately 0.4-0.6 Myr older than the corresponding $^{40}Ar/^{39}Ar$ sanidine ages (Watts et al., 2016).
 173 The number of analyses per aliquot (non-CA or CA) ranges from 17-34 for these three samples (Table 1).
 174

Table 1. Sample Summary

Sample	Age (Ma) \pm 1 σ (2 σ)	Reference	N (non-CA)	N (CA)	Mean $\log(D_0)$ ⁸	Model results (best fit logit-normal distribution)					
						$f(t)$ (Ma) \pm 1 σ (1 σ)	$g(t)$ sum of squared residuals (σ) sum of squared residuals	$g(t)$ parameters (μ , σ)	$g(t)$ P2.5-P50- P97.5 (%) P2.5-P50- P97.5 (%)	W_1	W_2
ELM18 DVTC- 10ELM1 8DVTC- 10	15.7 \pm 0.2 (2 σ) ¹⁵⁻⁷	Miller et al. (2022) Miller et al. (2022)	144 44	n.a.	16.0	15.90 \pm 0.55 (1 σ) ¹⁵⁻⁹⁰	1.0	$\mu = -3.24$ $\sigma = 1.28$	-32.49 -3.77 -0.32 32.49 -3.77 -0.32	6.9 6.9	11.1 11.1
248- 2248-2	24.422 \pm 0.25 (2 σ) ²⁴⁻⁴²²	von Quadt et al. (2014) von Quadt et al. (2014)	303	555	16.8	24.42 \pm 0.64 (1 σ) ²⁴⁻⁴²	2.7	$\mu = -4.48$ $\sigma = 1.06$	-8.3 -1.12 -0.14 8.3 -1.12 -0.14	1.9 1.9	3.03 0
029- 5 ⁰²⁹⁻⁵	24.480 \pm 0.084 (2 σ) ²⁴⁻⁴⁸⁰	von Quadt et al. (2014) von Quadt et al. (2014)	424	484	16.9	24.47 \pm 0.79 (1 σ) ²⁴⁻⁴⁷	3.3	$\mu = -3.10$ $\sigma = 0.47$	-10.17 -4.31 -1.76 10.17 -4.31 -1.76	4.7 4.7	5.25 2
059- 1 ⁰⁵⁹⁻¹	24.57 \pm 0.28 (2 σ) ²⁴⁻⁵⁷	von Quadt et al. (2014) von Quadt et al. (2014)	414	363	17.0	24.50 \pm 0.95 (1 σ) ²⁴⁻⁵⁰	1.1	$\mu = -3.48$ $\sigma = 0.52$	-7.87 -2.99 -1.1 7.87 -2.99 -1.1	3.4 3.4	3.83 8
CTUCT U	34.41 \pm 0.26 (2 σ) ³⁴⁻⁴¹	Watts et al. (2016) Watts et al. (2016)	242	181	16.5	34.47 \pm 0.83 (1 σ) ³⁴⁻⁴⁷	2.1	$\mu = -3.21$ $\sigma = 0.29$	-6.65 -3.88 -2.23 6.65 -3.88 -2.23	4.0 4.0	4.24 2
RCPRCP	34.38 \pm 0.32 (2 σ) ³⁴⁻³⁸	Watts et al. (2016) Watts et al. (2016)	343	181	16.6	34.19 \pm 0.75 (1 σ) ³⁴⁻¹⁹	3.1	$\mu = -3.96$ $\sigma = 0.80$	-8.38 -1.87 -0.40 8.38 -1.87 -0.40	2.5 2.5	3.33 3
SRFSRF	34.62 \pm 0.37 (2 σ) ³⁴⁻⁶²	Watts et al. (2016) Watts et al. (2016)	174	174	16.7	34.25 \pm 0.75 (1 σ) ³⁴⁻²⁵	5.1	$\mu = -4.57$ $\sigma = 1.08$	-7.92 -1.03 -0.12 7.92 -1.03 -0.12	1.8 1.8	2.92 9

	62 ± 0.37 (2 σ) ²	ttt et al. (2016)				± 0.75 (1 σ)		$\sigma = 1.08$	-1.03 -0.12		
DG 026 026	76.41 ± 0.45 (2 σ) ² 76.41 ± 0.45 (2 σ) ³	von Quadt et al. (2014) von Quadt et al. (2014)	3131	3434	16.6	76.16 \pm 1.42 (1 σ) 76.16 ± 1.42 (1 σ)	3.03	$\mu = -3.74$ $\sigma = 0.56$ $\mu = -3.74$ $\sigma = 0.56$	-6.65 -2.32 -0.79 -6.65 -2.32 -0.79	2.7 2.7	3.13 1
MM20- EC- 109 20-EC- 109 ⁶	144.50 ± 0.07 (2 σ) ⁴ 4.50 ± 0.07 (2 σ) ⁴	This study This study	6868	n.a. n.a.	17.8	144.43 \pm 3.12 (1 σ) 144.4 3 \pm 3.12 (1 σ)	1.61	$\mu = -4.73$ $\sigma = 1.91$ $\mu = -4.73$ $\sigma = 1.91$	-27.16 -0.87 -0.02 -27.16 -0.87 -0.02	3.6 3.6	8.88 .8
AvQ 244 ⁷ 244 ⁷	333.60 ± 0.66 (2 σ) ³ 3.60 ± 0.66 (2 σ) ³	von Quadt et al. (2014) von Quadt et al. (2014)	1747	1949	17.0	333.64 \pm 10.86 (1 σ) 333.6 4 \pm 10.86 (1 σ)	12.31	$\mu = -2.69$ $\sigma = 0.82$ $\mu = -2.69$ $\sigma = 0.82$	-25.30 -6.36 -1.34 -25.30 -6.36 -1.34	8.1 8.1	10.3 10.3

175

176 ¹Sanidine ³⁹Ar/⁴⁰Ar age (Snow and Lux, 1999)177 ²Error-weighted mean of chemically abraded U-Pb dates178 ³Concordia age (CA-ID-TIMS)179 ⁴Error-weighted mean 5 of 5 zircon crystals analyzed via CA-ID-TIMS180 ⁵U-Pb dates older than 28 Ma excluded from analysis181 ⁶U-Pb dates older than 158 Ma excluded from analysis182 ⁷U-Pb dates older than 360 Ma excluded from analysis183 ⁸D_α is the alpha dose (events g⁻¹)

184 N = Number of analyses

185 n.a. = Not available

186 W₁ = first Wasserstein distance187 W₂ = second Wasserstein distance

188

189 We present analysis of five samples reported in von Quadt et al. (2014), including upper Oligocene andesite/trachy-andesite
190 from Macedonia (248-2, 029-5, and 059-1), upper Cretaceous dolerite from Romania (DG 026), and middle Carboniferous
191 granite from West-Bulgaria (AvQ 244). These samples were also split into non-CA and CA aliquots prior to analysis via LA-
192 ICP-MS. For samples other than 059-1 we use concordia ages from CA-ID-TIMS analyses of between three and six crystals
193 for the crystallization age of each sample (von Quadt et al., 2014; Table 1). For sample 059-1 we used the weighted mean of
194 the CA U-Pb dates. The number of analyses per sample (non-CA or CA) ranged from 17-55 for this dataset (Table 1).

195

196 Sample ELM18DVTC-10 is from a Miocene ash-flow tuff from the Pangua Formation in the western United States that has
197 144 U-Pb dates acquired via LA-ICP-MS (Miller et al., 2022). We use a ⁴⁰Ar/³⁹Ar weighted mean age of 15.7 \pm 0.2 Ma
198 (2 σ) from the same unit as an estimate of the crystallization age of this sample (sample 592-GV1 of Snow and Lux, 1999).

199 Sample ELM18DVTC-10 was highlighted by Schwartz et al. (2022) who noted the youngest zircon U-Pb dates to be

200 much younger than the accepted $^{40}\text{Ar}/^{39}\text{Ar}$ age of this unit. Miller et al. (2022) also noted the presence of these young zircon
201 and suggested that they may be a consequence of surface contamination from units higher in the section.

202
203 Sample MM20-EC-109 is a Lower Cretaceous intermediate ash interbedded within marine carbonaceous mudstone from the
204 Rio Mayer Formation of Argentina with 68 zircon Pb-U-Pb dates acquired via LA-ICP-MS (Table A3). Laser ablation spot
205 locations were selected on the rim and/or core of the zircon guided by CL images (Figure A3), with 59 zircon crystals analyzed
206 in total. We use a crystallization age of 144.43 ± 0.07 Ma (2σ) derived from a weighted mean of five zircon crystals analyzed
207 via CA-ID-TIMS at the Boise State University Isotope Geology Laboratory (Table A4). This sample exhibits a large offset
208 between the youngest Pb-U-Pb dates acquired via LA-ICP-MS, up to ~60% younger than the CA-ID-TIMS weighted mean.

209 3.3 Statistical analysis

210 To evaluate the likelihood that the measured Pb^*/U distribution could have been drawn from the modeled $(f * g)(t)$, we apply
211 the nonparametric, 1-sided Kolmogorov-Smirnov (K-S) and Kuiper statistical tests that compare the ECDF with the cumulative
212 CDF of $(f * g)(t)$ (Press, 2007). The Kuiper statistic is relatively more sensitive in differences in the tails of the distributions
213 versus the K-S statistic (Vermeesch, 2018a). We reject the null hypothesis that the non-CA Pb-U-Pb dates were drawn from
214 $(f * g)(t)$ if the K-S or Kuiper p-value is <0.05 (i.e., 95% confidence level). We thus interpret p-values >0.05 to indicate that
215 the non-CA Pb-U-Pb dates could have been plausibly drawn from $(f * g)(t)$ at a 95% confidence level (Press, 2007).
216 However, it should be noted that Saylor and Sundell (2016) found that both K-S and Kuiper p-values more frequently reject
217 the null hypothesis than expected. We thus use p-values as a general guideline to model goodness-of-fit.

218
219 The Wasserstein distance has been recently proposed as a metric for quantifying the dissimilarity between detrital zircon Pb-U-Pb
220 age distributions (Lipp and Vermeesch, 2023). We consider the first and second Wasserstein distances, W_1 and W_2 ,
221 to be useful approximations for the total degree of negative Pb^*/U perturbation that a set of analyses has experienced,

$$222 \quad W_1 = \int_0^1 |M^{-1} - N^{-1}| dt \quad (\text{Equation 3})$$

$$223 \quad W_2 = \sqrt{\int_0^1 |M^{-1} - N^{-1}|^2 dt} \quad (\text{Equation 4})$$

224 where M^{-1} and N^{-1} are the inverses of the CDFs M and N . Because values of Pb loss are restricted to between 0% and 100%,
225 both W_1 and W_2 yield maximum possible values of 100 (i.e., 100% of analyses have -100% Pb^*/U offset, or the Pb-U-Pb
226 system is completely reset). The W_1 simply equates to the area beneath the cumulative probability distribution of $g(t)$ (e.g.,
227 Fig. 3). Because the W_2 distance involves a squaring of the distance between the quantile functions, it imparts a higher cost
228 penalty for the part of the distribution with strongly offset values. For example, the W_1 and W_2 distances are equal for a Pb
229 loss function characterized by constant Pb loss (e.g., 3% Pb loss produces W_1 and W_2 values of 3, Fig. 3b). However, the W_2
230 distance is often much larger than W_1 for Pb loss distributions with a heavy tail (Fig. 3d). As such, the W_2/W_1 ratio provides

231 an approximation of Pb loss distribution asymmetry, with values of 1 indicating constant Pb loss and values $\gg 1$ indicating
232 highly asymmetric Pb loss.

233 **4 Results**

234 Of the four primary types of Pb loss distributions considered (Fig. 3), the logit-normal distribution yielded the lowest average
235 misfit with a value of 3.5, followed by the isolated Pb loss scenario (average of 4.5) and the constant Pb loss scenario (average
236 of 10.5) (Table A2). The scenario of no Pb loss performed the worst of any scenario that we considered, with an average misfit
237 of 101.3 (Table A2). Correspondingly, both K-S and Kuiper p-values for the no Pb loss
238

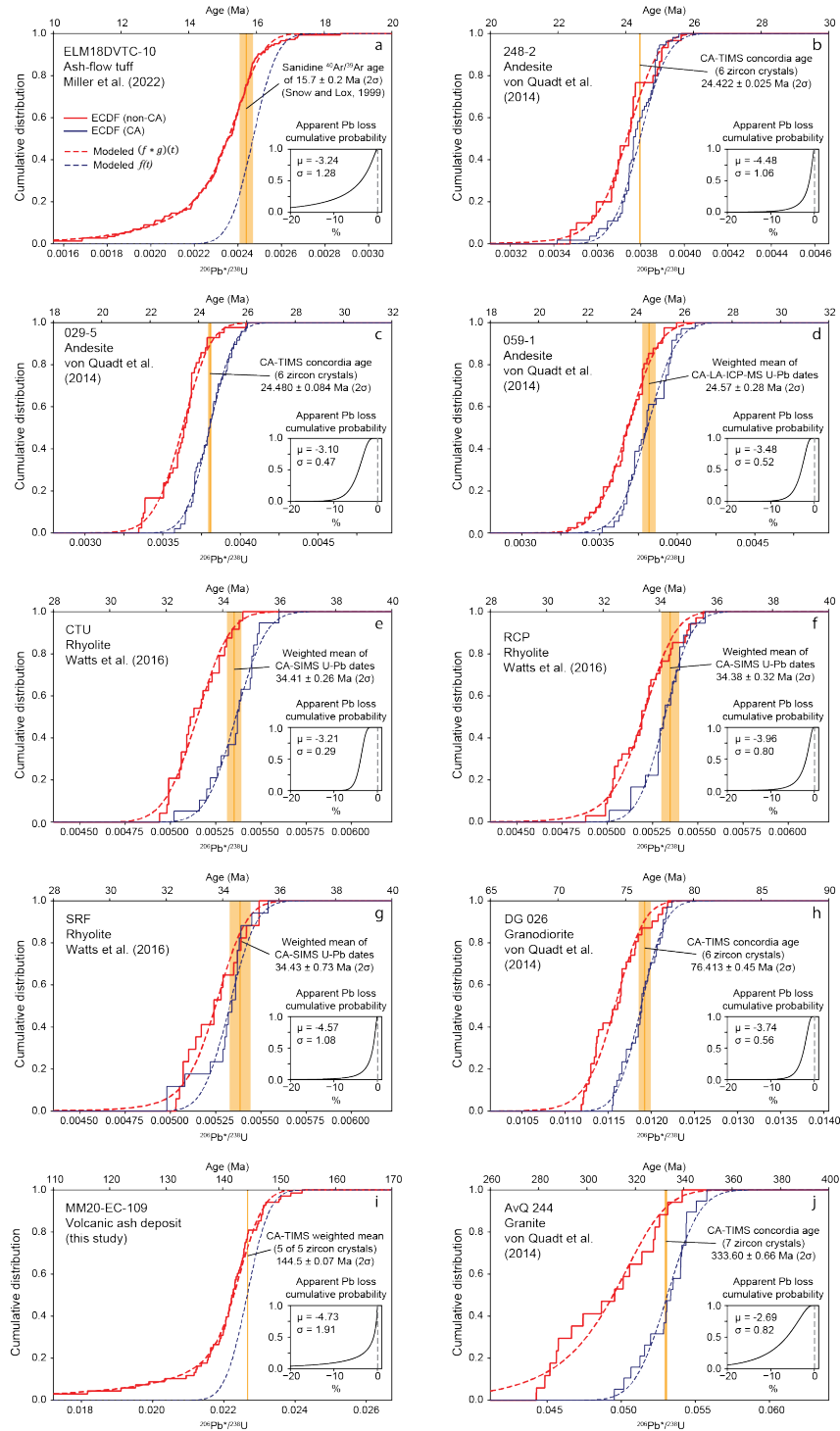


Figure 5. Modeling of apparent Pb loss in zircon U-Pb dates acquired via LA-ICP-MS or SIMS. The best-fitting logit-normal distribution of apparent Pb loss is shown (Table 1; see Figure A1 for plots of all samples and apparent Pb loss distribution types modeled). Empirical cumulative distribution functions (ECDFs) are shown as solid lines while model results are shown as dashed lines. See text for further discussion of model results.

239

240 scenario are $\ll 0.05$ for all samples except SRF, suggesting that the untreated LA-ICP-MS or SIMS U-Pb/U-Pb dates are
241 unlikely to have been drawn from an unperturbed U-Pb/U-Pb date distribution.

242

243 Figure 5 presents a comparison of actual versus modeled U-Pb/U-Pb date distributions for each sample, with the best-fitting
244 logit-normal distribution shown (Table 1; see Figure A1 for individual plots that show the fit for each sample and distribution
245 type). We chose to not consider discrete distributions of $g(t)$ for the “best” fit because we consider it unlikely that Pb loss (or
246 other processes that cause negative age offsets) would be limited to discrete values (e.g., Fig. 3). Values of μ for $g(t)$ ranged
247 from -2.69 to -4.73 with corresponding values of σ spanning 0.29 to 1.91. W_1 distances ranged between 1.8 (sample SRF) and
248 8.1 (sample AvQ 244) and W_2 distances between 2.9 and 11.1 (Table 1; Fig. 5).

249

250 A plot of the best-fitting logit-normal distributions displays two distinct behaviors of $g(t)$ (Fig. 6). (1) Four samples with $\mu <$
251 ~ -3 and $\sigma > 1$ and have a $g(t)$ maximum relative probability close to 0% suggesting a strongly decaying rate of offset (i.e.,
252 most zircon experienced very little Pb loss, while a few have more significant Pb*/U offset). These samples also displayed
253 $W_2/W_1 \geq 1.6$. (2) The remaining six samples that yielded $\sigma < 1$ and generally higher μ values (> -4) displayed a tendency for
254 the mode of $g(t)$ to be $> 0\%$, representing more of a bulk shift in age (e.g., most U-Pb/U-Pb dates have some offset, while
255 relatively few have very little or very much age offset). These samples produced $W_2/W_1 \leq 1.3$.

257 5.1 Assumptions and limitations

258 The mathematical and modeling framework that we present includes
 259 several underlying assumptions and limitations that should be
 260 considered.

261 1. Because $g(t)$ could represent any geological or analytical
 262 process that introduces negative age offsets, we use the phrase “apparent
 263 Pb loss” when describing our modeled estimates of $g(t)$. For instance,
 264 matrix-related systematic errors (Allen and Campbell, 2012), addition of
 265 U-Th during weathering (Pigeon et al., 2019), and even sample
 266 contamination from younger minerals could introduce negative age shifts
 267 exclusive of loss of radiogenic Pb. Common Pb corrections, particularly
 268 the ^{207}Pb -correction, may also introduce a bias towards artificially low
 269 Pb^*/U values (Anderson, 2002; Anderson et al., 2019). We recommend
 270 that these additional complexities in the U-Pb-U-Pb system be considered
 271 when interpreting modeled estimates of $g(t)$ as representing distributions
 272 of Pb loss.

273
 274
 275 2. Our approach of parameterizing $g(t)$ for the purpose of
 276 exploratory modeling has the advantage of yielding results that are
 277 interpretable while also being suitable for the relatively low- n datasets
 278 available. However, any parametric model is likely a simplification of the
 279 true $g(t)$, and thus we consider our modeled estimates of $g(t)$ to be first-order approximations. Analyzing a greater range of
 280 samples with a greater number of $\pm\text{CA}$ *in-situ* U-Pb-U-Pb analyses, with ideal datasets having 100s or even 1000s of analyses
 281 per sample (e.g., Pullen et al., 2014; Sundell et al., 2021), would likely improve our ability to constrain the form(s) of $g(t)$ and
 282 evaluate whether the logit-normal distribution or other forms of $g(t)$ are appropriate. Such datasets would also be more
 283 amenable to nonparametric solutions of estimating $g(t)$.

284
 285 3. For $g(t)$ to represent the true distribution of Pb loss, the process of convolution must be applied to Pb^*/U ratios at the
 286 time of Pb loss. Because Pb^* is progressively added to the crystal over time, a greater amount of ancient Pb loss is required to
 287 achieve the same reduction in Pb^*/U relative to recent Pb loss. This point is illustrated in Figure 1 where a 50% reduction in
 288 Pb^* at 125 Myr after crystallization produces a similar reduction in $^{206}\text{Pb}^*/^{238}\text{U}$ when compared to zircon of the same age that

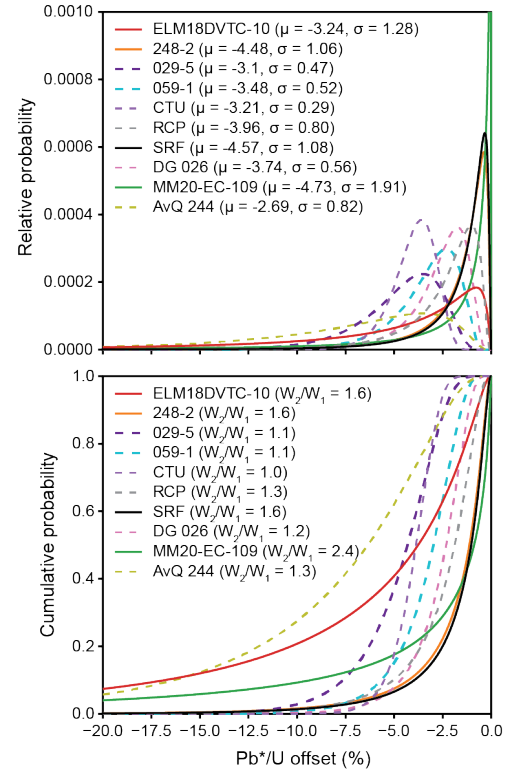


Figure 6. Distributions of apparent Pb loss when modeled as a logit-normal distribution. Samples with $\sigma < 1$ are shown as a dashed line.

289 lost 25% of its Pb* at 250 Myr (present day). For this reason, $g(t)$ can be viewed as a minimum estimate in the case of ancient
290 Pb loss. If the timing of Pb loss is known or can be estimated (e.g., Morris et al., 2015), the input Pb*/U ratios can be adjusted
291 prior to analysis such that $g(t)$ more accurately reflects the true magnitude of Pb loss.

292

293 4. The modeling framework presented above is designed for a group of cogenetic crystals with a shared crystallization
294 age (e.g., autocrystic zircon from the same magmatic episode; Miller et al., 2007). This requirement stems from our definition
295 of apparent Pb loss as a relative shift, or percentage deviation from the true isotopic value (Fig. 2). The assumption that all
296 zircon are coeval is a simplification, as even autocrystic zircon crystallize over a period of time, typically 10^3 - 10^4 yr timescales
297 (Miller et al., 2007; Rossignol et al., 2019). Multimodal detrital samples or igneous samples with xenocrystic or inherited
298 zircon are not easily modeled because these samples would violate our assumption of a shared crystallization age. Failure to
299 recognize the true heterogeneity in crystallization age in such a sample could cause an incorrect interpretation of the apparent
300 Pb loss distribution.

301

302 5. For datasets with paired non-CA and CA measurements, our modeling approach assumes that the relative precision
303 of the analyses is similar. This is because the Gaussian distribution that best approximates the CA U-Pb/U-Pb date distribution,
304 $f(t)$, is convolved with the apparent Pb loss distribution $g(t)$ to fit the non-CA U-Pb/U-Pb date distribution. The Watts et al.
305 (2016) SIMS dataset shows similar relative precision regardless of treatment approach (non-CA versus CA). Some samples
306 from the von Quadt et al. (2014) LA-ICP-MS dataset exhibit slightly lower relative precisions for non-CA versus CA, with
307 sample AvQ 244 yielding the largest difference with an average relative precision of 1.1% (1σ) for non-CA dates and 0.8%
308 (1σ) for CA dates. We suggest that for the purposes of modeling apparent Pb loss, paired non-CA and CA U-Pb/U-Pb datasets
309 should be collected on the same instrument using similar acquisition parameters to avoid introducing large changes in
310 measurement precision. Alternatively, the CA U-Pb/U-Pb dates may be used to only constrain the μ of $f(t)$ in the model, with
311 σ treated as an unknown parameter (e.g., for paired non-CA LA-ICP-MS and CA-ID-TIMS datasets; Figs. 5a and 5i).

312

313 6. For datasets with paired non-CA and CA measurements, we do not consider any imperfections of the chemical
314 abrasion process. For example, although the CA treatment aims to completely remove all radiation damaged zones of the
315 crystal (Mattinson, 2005), it is possible to have remaining residual zones of Pb loss following treatment (e.g., Schoene et al.,
316 2010). Any such remaining compromised domains of the crystal will yield at least some apparent Pb loss when analyzed. For
317 instance, Watts et al. (2016) interpreted three zircon U-Pb/U-Pb analyses from SRF to have some residual Pb loss that was not
318 fully accounted for by the CA process (Fig. 5g). Incorporation of Pb loss-perturbed U-Pb/U-Pb dates when modeling $f(t)$ would
319 likely produce an underestimate of the true magnitude of the apparent Pb loss.

320

321

322

323 5.2 Distributions of apparent Pb loss

324 What distribution type(s) characterize apparent Pb loss in natural samples? Our results strongly suggest that at least nine of the
325 10 samples modeled have at least some systematic negative offset in $^{206}\text{Pb}^*/^{238}\text{U}$ that cannot be explained by random
326 measurement uncertainties alone. This is because the K-S and Kuiper statistical tests are unable to reject the null hypothesis
327 for many of the apparent Pb loss distribution types considered (Table A1). For example, only the no Pb loss scenario produced
328 a p -value < 0.05 for sample MM20-EC-109, suggesting that any of the other modeled distributions of apparent Pb loss may be
329 statistically plausible for this sample. These results suggest that we cannot confidently distinguish between discrete (constant
330 or isolated) or continuous distributions of apparent Pb loss in the datasets modeled. Except for ELM18DVTC-10 which has
331 144 non-CA LA-ICP-MS analyses, the samples we analyzed have relatively low numbers of analyses (between 17 and 68,
332 average of 32) for a given sample and treatment category (non-CA or CA) (Table 1). We suspect that collection of larger- n
333 datasets would allow better resolution of which parameterizations of $g(t)$ might be most appropriate.

334
335 Even if the specific distribution type(s) that characterizes $g(t)$ cannot be uniquely identified, our analysis suggests two
336 contrasting behaviors in apparent Pb loss (Fig. 6). We speculate that U-Pb-U-Pb dates that undergo a bulk shift (i.e., $W_2/W_1 \cong$
337 1) may reflect a population of zircon crystals with relatively homogenous characteristics (e.g., size, U content, etc.) that have
338 all experienced a similar post-crystallization history. Correspondingly, the population of zircon that produces U-Pb-U-Pb dates
339 with a highly asymmetric distribution of age offset (i.e., $W_2/W_1 > \sim 1.5$) may reflect heterogeneity between crystals, with
340 variable characteristics. For example, Pb loss is thought to be promoted in small zircon crystals and in zircon with elevated U
341 (Ashwal et al., 1999; Gehrels et al., 2020), and thus distributions of particle size and/or trace element geochemistry may
342 influence asymmetric patterns in $g(t)$. Collection of size measurements and trace element concentrations from zircon in
343 addition to measurement of the U-Pb-U-Pb date (e.g., Watts et al., 2016) would likely help evaluate hypotheses about the
344 underlying factors that influence apparent Pb loss distributions. Furthermore, given the relatively small number of samples
345 modeled in this study, we suggest that there is a need for more samples to undergo paired non-CA and CA characterization to
346 improve understanding of the range of behaviors that may be typical. For example, it is presently unclear whether it is more
347 common for samples to have their U-Pb-U-Pb dates bulk shifted (e.g., samples 029-5, 059-1, CTU, DG 026) versus having
348 relatively few U-Pb-U-Pb dates highly offset (e.g., samples MM20-EC-109 and ELM18DVTC-10; Fig. 5).

349
350 Why do some samples experience more overall apparent Pb loss than others? Although we anticipated that apparent Pb loss
351 would be greater for older samples with greater radiation damage due to U and Th decay, our analysis shows no clear
352 trend by sample age or alpha dose (Table 1). However, ~~(although~~ we acknowledge that the relatively high degree of apparent Pb
353 loss modeled in the youngest sample, ELM18DVTC-10, may be a consequence of contamination from overlying units, instead
354 of true Pb loss; (Miller et al., 2022). Even the three samples from the same Eocene caldera system (CTU, RCP, and SRF)
355 showed contrasting amounts of apparent Pb loss (W_2 ranges from 2.9 to 4.2; Table 1) as noted by Watts et al. (2016).

356 Characterizing the overall magnitude of apparent Pb loss in a wider range of samples would likely help elucidate predictive
357 factors, if any.

358

359 **5.3 Importance of quantifying the distribution of apparent Pb loss in *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ geochronology**

360 The overwhelming majority of published *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ dates from zircon, minimally >600,000 and likely in the millions
361 of analyses (Puetz et al., 2021), have not been treated using CA. In contrast, CA is now practiced routinely in the ID-TIMS
362 community which has contributed to growing precision and accuracy over the past two decades (Schoene, 2013). However,
363 the strategy of mitigating Pb loss through avoidance is perhaps less easily adopted to routine *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ geochronology.
364 For instance, there may be practical limitations with chemically abrading large numbers of zircon crystals, including the
365 potential loss of certain age modes that would be detrimental to provenance analysis. We thus suggest that there is a pressing
366 need to improve quantitative characterization of apparent Pb loss distributions in non-CA *in-situ* $^{206}\text{Pb}/^{238}\text{U}$ datasets to aid in
367 interpreting these datasets and to guide strategies for future data collection.

368

369 It is somewhat concerning that nine of the 10 samples analyzed in this study exhibited statistically significant amounts of
370 negative age offset from the estimated true crystallization age. Even a small age offset of a few percent, or cryptic Pb loss
371 (Kryza et al., 2012; Watts et al., 2016), has potentially important repercussions for interpreting the age and rates of geologic
372 events and processes. For example, there is a growing awareness in the detrital geochronological community that the youngest
373 zircon $^{206}\text{Pb}/^{238}\text{U}$ dates often skew unexpectedly young relative to the plausible crystallization age (e.g., Herriot et al., 2019;
374 Gehrels et al., 2020; Schwartz et al., 2022). Presently, there is no consensus on the importance of post-depositional Pb loss on
375 influencing depositional age interpretations (e.g., Herriott et al., 2019; Copeland, 2020; Schwartz et al., 2022). Sample MM20-
376 EC-109 illustrates the risk well; we initially interpreted the young tail on the $^{206}\text{Pb}/^{238}\text{U}$ date distribution to suggest a
377 depositional age of ~125 Ma based on the youngest cluster of overlapping $^{206}\text{Pb}/^{238}\text{U}$ dates. The youngest single analysis was
378 a 60.5 ± 2.4 Ma rim on a 135.3 ± 3.0 Ma core, with the second youngest being a 79 ± 1.2 Ma date measured from the core of
379 a zircon crystal, with the corresponding rim yielding an older 129.8 ± 3.6 Ma date (Table A2). Interpretation of the youngest
380 single $^{206}\text{Pb}/^{238}\text{U}$ date or dates as the depositional age of this sample would have produced a highly erroneous estimate, off by
381 up to -58% of the true eruption age of 144.50 ± 0.07 (2σ) Ma as determined by CA-ID-TIMS. Because this ash is interbedded
382 within a sequence of organic rich marine mudstone in the Austral Basin of Argentina, the misinterpretation in this case could
383 have led to an erroneous depositional age model with implications for interpreting the paleoclimatic and geodynamic context
384 of these sediments.

385

386 Although modeling detrital samples was outside of the scope of this study, we believe that our results bear upon maximum
387 depositional age analysis. The tendency for the youngest $^{206}\text{Pb}/^{238}\text{U}$ dates in a sample to be affected by Pb loss (or other similar

388 process) complicates even conservative estimates of the maximum depositional age (Dickinson and Gehrels., 2009; Coutts et
389 al., 2019; Schwartz et al., 2022). If apparent Pb loss follows a continuous distribution (e.g., Fig. 3d), then it is ill-advised to
390 assume that outlying $U-Pb-U-Pb$ dates may be rejected while the rest are considered unperturbed (see also discussion in
391 Copeland, 2020). Even an interpretation based on the peak age probability of the youngest age mode is likely to be too young,
392 because the process of convolution produces a young shift in the mode of the distribution, in addition to creating a young tail
393 (Fig. 3d; Fig. A1). Because existing methods of calculating the maximum depositional age (Dickinson and Gehrels, 2009;
394 Coutts et al., 2019; Vermeesch, 2021) do not account for systematic negative age offsets, our analysis suggests that there is a
395 higher probability for erroneous estimates of the maximum depositional age if (1) there are a large number of zircon crystals
396 with crystallization ages that are close to the age of deposition, (2) the overall number of measured $U-Pb-U-Pb$ analyses is very
397 high, and/or (3) the magnitude of apparent Pb loss is high. In addition, a heavy-tailed distribution of apparent Pb loss (i.e.,
398 $W_2/W_1 \gg 1$) will result in a greater probability of finding extremely offset Pb^*/U values.

399

400 6 Conclusions

401 This study presents a mathematical framework for quantifying the distribution of apparent Pb loss on $U-Pb-U-Pb$ date
402 distributions, which could include true loss of radiogenic Pb or other processes that also produce a systematically negative age
403 offset. We show that a Pb loss-perturbed $U-Pb-U-Pb$ date distribution from a set of zircon crystals with a shared crystallization
404 age can be represented by the convolution of a Gaussian distribution that reflects measurement uncertainty in Pb^*/U with a
405 distribution that characterizes Pb loss, $g(t)$. Our approach relies on analyzing differences between the untreated Pb^*/U
406 distribution from *in-situ* $U-Pb-U-Pb$ geochronology (i.e., LA-ICP-MS or SIMS) and an independent estimate of the true
407 crystallization age, which could include $U-Pb-U-Pb$ dates from a thermally annealed and chemically abraded aliquot of the
408 same sample or from another geochronometer (e.g., $^{40}Ar/^{39}Ar$). We suggest that the first and second Wasserstein distances (W_1
409 and W_2) of the apparent Pb loss distribution can be used to quantify the total degree of apparent Pb loss that a set of zircon
410 analyses has undergone, with maximum possible W_1 and W_2 values of 100.

411

412 We apply this modeling framework to ten igneous samples (Miocene to Carboniferous) analyzed with LA-ICP-MS or SIMS.
413 All but one of the samples showed a high probability that the untreated $U-Pb-U-Pb$ date distribution has been perturbed by Pb
414 loss or other equivalent process. Although our analysis shows that multiple parameterizations of $g(t)$ can achieve statistically
415 acceptable fits (i.e., K-S or Kuiper p -value >0.05), we suggest that the logit-normal distribution may be a reasonable choice
416 for exploratory modeling of apparent Pb loss distributions. However, we caution that the number of analyses in the samples
417 we analyzed was generally low (17-144, average of 39); future efforts to characterize $g(t)$ may be promoted by collection of
418 larger- n datasets and through development of nonparametric methods of estimating $g(t)$. Furthermore, our estimates of $g(t)$
419 should be viewed as minimum estimates of the true amount of Pb lost, as we assumed present-day Pb loss in our analysis.

420 These caveats aside, we noted two behaviors of apparent Pb loss; samples with a bulk shift in $U-Pb/U-Pb$ date distributions
421 ($W_2/W_1 < \sim 1.3$) and samples where most analyses had very little offset but fewer had much larger offsets ($W_2/W_1 > \sim 1.6$). The
422 overall magnitude of Pb^*/U decrease was also found to be variable, with median values varying from -0.9% to -6.4%.

423
424 Given the widespread application of *in-situ* $U-Pb/U-Pb$ geochronology of untreated zircon across many disciplines of
425 geosciences, improved characterization of both the distribution type(s) and magnitude of apparent Pb loss is warranted,
426 particularly for Phanerozoic zircon where cryptic Pb loss is difficult to identify. We highlight a need for increased sampling
427 and high- n characterization of paired non-CA and CA *in-situ* $U-Pb/U-Pb$ datasets. In addition, we recommend simultaneous
428 collection of parameters such as zircon size and trace elemental concentrations to aid in future efforts to understand the
429 mechanisms of negative age offsets. Ultimately, we anticipate that improved characterization of the magnitude of apparent Pb
430 loss will aid in interpreting non-CA *in-situ* $U-Pb/U-Pb$ datasets and guide strategies for future data collection.

431 Data availability

432 Data are archived under <https://doi.org/10.5281/zenodo.8302521>. Appendix A provides a description of exploratory modeling
433 of different parameterizations of $g(t)$. Figure A1 includes examples of eight continuous distribution types not explored in the
434 main text. Table A1 and Figure A2 include summaries of all model results. Table A2 presents a summary of model fit for each
435 sample and distribution type considered. Tables A3 and A4 provide $U-Pb/U-Pb$ analytical results for sample MM20-EC-109
436 from the University of Arizona LaserChron Center (LA-ICP-MS) and Boise State University Isotope Geology Laboratory
437 (CA-ID-TIMS), respectively. Figure A3 includes CL images from the University of Arizona LaserChron Center. Supplemental
438 Video 1 provides an example of convolution. Supplemental Video 2 presents an exploration of the parameter space for the
439 logit-normal distribution.

441 Code availability

442 Code used in this research is available on GitHub (https://github.com/grsharman/Pb_loss_modeling) with the v2.0.0 commit
443 archived under <https://doi.org/10.5281/zenodo.8302313>.

445 Video supplement

446 Supplemental Video 1 is available at <https://doi.org/10.5281/zenodo.8302521>. This animation provides an illustration of how
447 a Gaussian distribution of $U-Pb/U-Pb$ dates (solid, blue line), $f(t)$, may be perturbed by logit-normal Pb loss, $g(t)$ (solid, red
448 line). The Pb loss distribution is first reflected about the y-axis and then iteratively shifted by small values of t , $g(t-\tau)$ (dashed,
449 red line). The convolution of $f(t)$ and $g(t)$ at any given value of t equals the summed area underneath the product of $f(t)$ and
450 $g(t-\tau)$. Supplemental Video 2 is also available at <https://doi.org/10.5281/zenodo.8302521> and illustrates how the logit-normal
451 distribution varies with respect to its two parameters μ and σ . Note that we have rescaled the x-axis of the logit-normal
452 distribution such that $-100 < x < 0$.

454 Author contribution

455 G. Sharman and M. Malkowski co-designed the study. G. Sharman developed the code. M. Malkowski produced the $U-Pb/U-$
456 Pb data from sample MM20-EC-109. G. Sharman and M. Malkowski wrote the manuscript.

457

458 **Competing interests**

459 The authors declare that they have no conflict of interest.

460

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