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Technical Note: Benchmark time-temperature paths provide a shared framework for evaluating and communicating thermochronologic data interpretation

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1	Abstract. We present a set of six time-temperature (tT) histories, called benchmark paths, that
2	can be used as a shared framework for evaluating the sensitivity of a thermochronologic system
3	to the variables inherent in the interpretation of thermochronologic data (e.g., kinetics models,
4	mineral compositions or geometries, etc.) . These benchmark paths span 100 Myr, include
5	monotonic and nonmonotonic histories that represent plausible geologic scenarios, and have a
6	range of cooling rates through different chronometer partial-retention/annealing temperatures.
7	Here, we demonstrate their utility by presenting a method for tuning these paths to 11 different
8	kinetics models for the apatite (U-Th-Sm)/He (n=5), apatite fission-track (n=2), and zircon (U-
9	Th)/He (n=4) systems. These tuned tT paths provide a practical comparison of the kinetics
10	models for each system and the data patterns they predict, thereby offering anyone performing
11	thermal history analysis the ability to consider how their choice of kinetics model may impact
12	their data interpretation. The adoption of benchmark paths for evaluating kinetics models and
13	other variables provides a practical way for the thermochronology community to evaluate and
14	communicate the decision making processes that are inherent in thermochronologic modeling
15	and data interpretation.

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17 1. Introduction

We propose adopting a common set of thermal (time-temperature, *tT*) histories, called benchmark paths, for the apatite (U-Th-Sm)/He, apatite fission-track, and zircon (U-Th)/He systems (hereafter AHe, AFT, and ZHe, respectively). These benchmark paths can be used for a variety of applications because they are designed to highlight the sensitivity of each thermochronometric system to differences in kinetics models, tT history features, mineral compositions/geometries, and other variables critical to the interpretation of thermochronologic data. For example, here we demonstrate the utility of these benchmark paths by using them to





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- 25 visualize and quantify the consequences of choosing different kinetics models to interpret
- 26 cooling ages.
- 27
- 28 **2. Designing the benchmark thermal histories**
- 29 Figure 1 presents a general representation of our proposed benchmark paths, which are
- 30 inspired by the paths in Wolf et al. (1998) and designed with the following criteria. Together,
- 31 these paths:
- 32 1. include simulations of both monotonic and non-monotonic thermal histories
- 33 2. explore a range of cooling rates through a chronometer's closure temperature window
- 34 3. represent geologically plausible thermal histories
- 35 The proposed 100-Myr-long benchmark paths represent distinct but realistic geologic
- 36 histories that capture simple monotonic cooling (Paths 1, 2) and complete thermal resetting
- 37 (Path 6), in addition to complex thermal conditions such as sustained residence in the closure
- temperature window (Paths 3, 4) and reheating that results in partial resetting (Path 5) that tend
- 39 to produce more complicated data sets.

40 Each of our six proposed benchmark thermal histories are representative of a geologic 41 setting in the following ways. Path 1 simulates rapid cooling, like that associated with post-42 eruptive cooling of a volcanic rock. Path 2 represents protracted cooling, typical of cratonic 43 erosion. Path 3 represents rapid rock cooling, such as is associated with rift initiation settings. 44 Path 4 shows cooling representative of erosion patterns in emerging topography, like that in an 45 active thrust belt. Path 5 includes heating at rates typical of basin burial followed by cooling 46 associated with basin inversion and exhumation. Path 6 simulates transient localized heating 47 and cooling, similar to what may happen next to a near-surface igneous intrusion. Each of these 48 geologic scenarios has a different duration and rate of cooling through the closure temperature 49 window (Fig. 1).





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50 In this contribution, we decided to tune these paths such that they all predict a 40 Ma age for 51 a specific grain composition and/or size because this facilitates an inverse approach. In other words, we visualize the results as the range of tT paths that are all tuned to produce a 40 Ma 52 age, where the tuned differences in the tT paths reflect the consequences of the thermal history 53 54 model inputs (e.g., kinetics model, etching protocols, grain geometry, mineral chemistry). This 55 mimics the most common thermochronologic workflow, where cooling age(s) are measured and 56 tT modeling is used to find the range of tT histories that fit those data. Designing each 57 benchmark path to produce a single 40 Ma age also means that they inherently demonstrate the 58 nonuniqueness of individual cooling ages (Wolf et al., 1998).



Figure 1: Proposed benchmark paths with relative temperature histories. Paths 1-5 are inspired
by Wolf et al., (1998) and modified by Murray et al., (2022) demonstrating the non-uniqueness
of a single cooling age.





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62 3. Tuning benchmark paths to specific kinetics models

63 We demonstrate the utility of our proposed benchmark paths by using them to illustrate the different temperature sensitivities of three low-temperature thermochronometers (AHe, AFT, 64 65 ZHe), and then, within each system, how kinetics models also require different temperatures to 66 produce the same age. This is useful because although experimentally-derived kinetics models 67 provide the foundation for the interpretation of thermochronologic data, it can be difficult to 68 develop a practical understanding of if or how choosing one kinetics model over another might 69 impact one's thermal history model results. This is critical for both project design and data 70 interpretation.

71 Most publications that introduce new kinetics models use example tT histories that are 72 calibrated to demonstrate the nuances of that specific kinetics model, in addition to the 73 mathematical calibrations that include intrinsic mineral features including chemistry, radiogenic 74 element concentration, and geometries (e.g., Wolf et al., 1996; Carlson et al., 1999; Donelick et 75 al., 1999; Ketcham et al., 1999; Farley, 2000; Reiners et al., 2004; Flowers et al., 2009; 76 Gautheron et al., 2009; Guenthner et al., 2013; Willett et al., 2017; Ginster et al., 2019; 77 Guenthner, 2021). For example, Flowers et al. (2009) demonstrated the RDAAM AHe kinetics 78 model using the ~300 Myr history of the Esplanade Sandstone and the ~1800 Myr history of 79 basement samples from the Canadian Shield. The α-recoil damage AHe kinetics model was 80 introduced by Gautheron et al. (2009) using the ~300 Myr duration geologic history of the 81 French Massif Central. Willet et al. (2017) uses the predicted ages from a ~550 Myr duration 82 geologic history from the Grand Canyon to present the ADAM AHe kinetics model. These 83 individualized tT histories remain a fundamental contribution because they demonstrated 84 behaviors distinctive to a particular kinetics model and the rocks these models were first applied 85 to. Our benchmark paths complement these contributions by providing a universal reference 86 frame that can be used to compare these kinetics models.





87	All benchmark paths are tuned to produce a 40 Ma age in crystals with the following
88	standard sizes and compositions. For the AHe system, the crystal is assigned a spherical radius
89	(Rs) of 60 μ m and an effective uranium concentration ([eU] = [U] + 0.234*[Th] + 0.0047*[Sm]) of
90	60 ppm. All benchmark paths are tuned for the AFT system using a Dpar = 2.05 μ m for grains
91	etched in 5.5M HNO_3 for 20 seconds (Sobel & Seward, 2010). All benchmark paths are tuned
92	for the ZHe system using a crystal with Rs = 60 μ m and [eU] = 600 ppm.
93	To tune a general benchmark path (Fig. 1) to a specific thermochronometer and an
94	associated kinetics model, we held constant the timing of heating and cooling events but
95	modified the maximum temperatures that control the timing and duration of passage through the
96	system's closure temperature window to produce a 40 Ma age (Fig. 2, Table 1). Practically, this
97	requires changing the temperature of one node of the tT path for each kinetics model (Fig. 2,
98	Table 1). Additionally, for each system (AHe, AFT, ZHe), benchmark paths 3 and 4 are
99	assigned an initial temperature at 100 Ma that is necessary for simulating slow cooling or
100	isothermal holding within the chronometer's closure temperature window (Fig. 2, Table 1). Then,
101	we further tuned the benchmark paths for each chronometer to all produce a 40 Ma age using
102	the following specific kinetics models:(1) the AHe system including Wolf et al. (1998), Farley
103	(2000), Flowers et al., (2009), Gautheron et al. (2009), and Willett et al., (2017); (2) the AFT
104	system including Ketcham et al., (1999) and Ketcham et al. (2007); and (3) the ZHe system
105	including Reiners et al., (2004), Guenthner et al. (2013), Ginster et al. (2019), and Guenthner
106	(2021) implementation of the ZRDAAM without annealing (Fig. 2, Table 1).
107	Within each chronometric system, this exercise provides a sensitivity test of kinetics
108	models. For example, for the AHe, AFT, and ZHe systems, the same temperature conditions
109	predict the same cooling age for rapid cooling associated with igneous processes (Fig. 2, Paths
110	1, 6). This suggests that the choice of a kinetics model in these thermal conditions will not
111	change the interpretation of the data, as has been previously discussed in the papers that





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112 originally presented these kinetics models (e.g., Ketcham et al., 1999; Flowers et al., 2009;

113 Guenthner et al., 2013).

114 By contrast, paths that feature slow cooling or prolonged residence at and/or reheating 115 to partial retention/annealing temperatures require different temperatures to predict the same 116 cooling age; making the corollary also true: measured cooling age(s) may fit different cooling 117 histories if using different kinetics models (Fig. 2). For example, the thermal histories that 118 produce a Path 4, 40 Ma cooling age for the AHe system require that the crystals are held at 119 temperatures between 75 and 29.5 Ma, but the difference in this holding temperature can vary 120 by nearly 30°C depending on the kinetics model used (Fig. 2). This variability in holding 121 temperatures is much lower, ~ 10°C, for the AHe kinetics models that incorporate the effects of 122 radiation damage and annealing (Flowers et al., 2009; Gautheron et al., 2009; Willett et al., 123 2017), but could still modify the geologic interpretations of such a data set. Interpretations using 124 kinetics from a legacy AHe kinetics model that does not consider the effects of radiation 125 damage and annealing (e.g., Wolf et al., 1996; Farley, 2000) should be reevaluated. For the 126 AFT system, Path 4 benchmark thermal histories also vary. The legacy kinetics model of 127 Ketcham (1999) requires a retention temperature ~ 10°C higher than the kinetics model of 128 Ketcham et al. (2007). By contrast, Path 4 benchmark thermal histories for ZHe kinetics models 129 from Guenthner et al. (2013) and Ginster et al., (2019) differ by only ~ 1°C indicating that the 130 choice of one kinetics model over the other will not modify the interpretation of such a data set. 131 We propose that for any new kinetics model, a new tuned set of benchmark paths is 132 made that can be compared with those tuned to existing kinetics models (Fig. 2). This set of 133 benchmark paths would be tuned by modifying the maximum temperature within the closure 134 temperature window of each mineral system to generate a predicted cooling age of 40 Ma ± 1 135 Ma using a particular kinetics model (Fig. 2, Table 1).

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	kinetics model		Path 1 Path 2				2	Path 3				Path 4				Path 5			Path 6				
	citation	time (Ma)	40	39.9	0	100	0	100	21	19	0	100	75	30	0	100	5	0	100	41	40.5	40	0
apatite (U-Th)/He	Wolf et al., 1996	Temperature (°C)	200	5	5	150	5	90	51	5	5	90	62	62	5	5	64	5	20	20	200	5	5
	Farley, 2000	Temperature (°C)	200	5	5	130	5	90	42	5	5	90	54	54	5	5	57	5	20	20	200	5	5
	Flowers et al., 2009	Temperature (°C)	200	5	5	145	5	90	61	5	5	90	71	71	5	5	83	5	20	20	200	5	5
	Gautheron et al., 2009	Temperature (°C)	200	5	5	185	5	90	76	5	5	90	82	82	5	5	90	5	20	20	200	5	5
	Willett et al., 2017	Temperature (°C)	200	5	5	150	5	90	65	5	5	90	73	73	5	5	83	5	20	20	200	5	5
apatite fission track	Ketcham et al., 2007	Temperature (°C)	200	5	5	230	5	130	81	5	5	120	93	93	5	5	99	5	20	20	200	5	5
	Ketcham et al., 1999	Temperature (°C)	200	5	5	255	5	130	96	5	5	120	105	105	5	5	111	5	20	20	200	5	5
zircon (U-Th)/He	Reiners et al., 2004	Temperature (°C)	200	5	5	440	5	240	149	5	5	300	172	172	5	5	180	5	20	20	260	5	5
	Guenthner et al. 2013	Temperature (°C)	200	5	5	400	5	240	140	5	5	300	164	164	5	5	181	5	20	20	260	5	5
	Guenthner, 2021	Temperature (°C)	200	5	5	435	5	240	145	5	5	300	168	168	5	5	182	5	20	20	260	5	5
	Ginster et al., 2019	Temperature (°C)	200	5	5	421	5	240	141	5	5	300	165	165	5	5	180	5	20	20	260	5	5
	change Temperature across																						
	chronometer																						

- change Temperature across kinetics model
- 138 Table 1: Benchmark Paths tuned to produce a 40 Ma cooling age for common legacy and
- 139 modern kinetics models for the apatite (U-Th)/He, apatite fission track, and zircon (U-Th)/He
- 140 systems.





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- 141 Figure 2: Benchmark paths shown in tT space. Benchmark paths are tuned to produce a 40 Ma
- 142 cooling age using published legacy and modern kinetics models of the AHe, AFT, and ZHe

143 systems









Figure 3: Expanding the data predicted by benchmark paths to include crystals with a range of
eU (AHe, ZHe) and track length distributions (AFT) shows data trends that can be used to
distinguish among the predictions and interpretations of different kinetics models.





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147 4. Using benchmark paths to visualize the additional effects of compositional variations

148 in datasets with more than one analysis

We next use the tuned benchmark paths to predict age-[eU] trends and track-length
distributions (Fig. 3). Expanding the predicted results of a benchmark path in these ways

simulates the resolving power of a real dataset with multiple analyses and demonstrates how

the choice of kinetics model may impact the possible fits to the data.

153 For the AHe and ZHe systems, we used tuned benchmark paths to predict multiple He 154 ages from a range of crystal [eU] compositions and thereby quantify and visualize the potential 155 impact of choosing one kinetics model over another during data analysis (Fig. 3). Simple and 156 fast cooling, like Paths 1 and 6, or steady and monotonic cooling, like Path 2, produce minimal 157 differences in the data patterns predicted by different kinetics models (Fig. 3). For example, 158 Paths 1 and 6 predict AHe cooling ages with a difference of ~ 1 Myr using the three published 159 kinetics models that account for radiation damage accumulation and annealing effects (Flowers 160 et al. 2009; Gautheron et al., 2009, Willett et al 2017) for crystals with [eU] values ranging from 161 10 ppm to 300 ppm. For the same [eU] apatite crystals, Path 2 predicts cooling ages that differ 162 by between ~ 1 - 5 Myr. In contrast, paths 3, 4, and 5 spend more time at He partial-retention 163 temperatures and therefore produce age-[eU] patterns that are more variable among the 164 kinetics models (Fig. 3).

165 The versions of Path 5 tuned to three radiation damage accumulation and annealing 166 models in the AHe system (Gautheron et al., 2009; Flowers et al., 2009; Willet et al., 2017) 167 provide a particularly instructive result. The peak temperatures required by the Flowers- and 168 Willet-tuned tT paths are within 0.5°C of each other, meaning that they predict a 40 Ma age for a 169 60 μm and 60 ppm [eU] crystal with the effectively identical tT histories. Likewise, at [eU] < 40 170 ppm, the Willet- and Flowers-tuned paths predict very similar ages. However, these models 171 diverge by >20 Myr at [eU] > 90 ppm; in other words, just because the Flowers- and Willet-tuned 172 tT paths are identical does not mean they predict the same ages for all crystal compositions. In





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173 contrast, the version of Path 5 tuned to the Gautheron et al. (2009) kinetics model, which has a 174 slightly higher peak temperature (Fig. 2), produces an age-[eU] trend that is similar to the Willet-175 tuned trend at [eU] > 60 ppm, similar to the Flowers- and Willet-tuned models at [eU] = 10 ppm, 176 but different from both the Flowers- and Willet-tuned trends at [eU] = 30 ppm (Fig. 3). Thus, 177 these simple forward models reveal the non-systematic differences among these kinetics 178 models and in what types of thermal histories (i.e., paths 3, 4, and 5) these differences manifest 179 most. 180 In this approach, it is critical to recognize that the largest differences in predicted He 181 ages among kinetics models occurs for the [eU] values that are different from 60 ppm [eU] 182 composition used to tune the paths, i.e., sometimes, but not always, the highest and lowest [eU] 183 crystals in an age-[eU] pattern. This is a result inherent to the particular approach we have 184 taken here: the tuning of the path to a fixed parameter (e.g., [eU] and grain size). The relative 185 difference in cooling ages for each [eU] would be different for paths tuned to a 20 ppm crystal or 186 a 100 ppm crystal. We emphasize that the choice of exactly how to tune a benchmark path 187 depends on the application. Regardless of the details of how a path is tuned, it will always be 188 the case that different kinetics models predict different patterns of data that depend on these 189 parameters, and exploring the sensitivities of each parameter is important to understand in the 190 modeling process. 191 For the ZHe system, the versions of Path 5 tuned to radiation damage accumulation and

annealing models of Guenthner et al. (2013) and Ginster et al. (2019) have peak temperatures within 0.5°C of each other (Fig. 2), but the predicted age-[eU] distribution is also nearly identical. For these kinetics models, tuned Path 5 thermal histories predict cooling ages within ~ 1 Myr of each other for [eU] values ranging from 100 - 3000 ppm (Fig. 3). This is also true for the other benchmark paths tuned to the Guenthner et al. (2013) and Ginster et al., (2019) kinetics models. This suggests that for 100-Myr-long thermal histories, the Guenthner and Ginster models will predict similar results. A third kinetics model—which for demonstration purposes





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199	simulates only damage accumulation, and not annealing (Guenthner, 2021)—has peak
200	temperatures 1.5 - 2°C higher than models that incorporate annealing. This no-annealing model
201	predicts an age-eU trend that only diverges from the others at [eU] > 600 ppm (Fig. 3), at crystal
202	compositions where radiation damage accumulates more rapidly and thus the annealing of this
203	damage is more impactful.
204	Considering the track-length distributions for the AFT system is one way to explore how
205	different AFT kinetics models predict data distributions for crystals with the same chemistry (Fig.
206	3). Although benchmark paths for the Ketcham (1999) and Ketcham et al. (2007) kinetics
207	models predict the same modalities and mean track lengths that vary by a maximum of ~ 0.15
208	$\mu m,$ the uncertainties of mean track lengths can vary by as much as 0.25 $\mu m.$ Consequently, the
209	kinetics model of Ketcham et al. (2007) predicts a narrower peak(s) of track lengths for all Paths
210	(Fig. 3). Versions of Path 5 tuned to each kinetics model produce identical mean track lengths,
211	but uncertainty is 0.05 μ m lower for track lengths predicted by the Ketcham et al. (2007) kinetics
212	model. Interestingly, the uncertainty in mean track lengths, ~0.25 μm , is greatest for Paths 1
213	and 6 which have simple, fast cooling. This example uses track-length distributions, but
214	modifying other parameters—for example, grain chemistry or its proxy, Dpar—could also be
215	used to explore predictions from different AFT kinetics models.

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217 **5.** A vision for the application of benchmark paths

Here, we demonstrate how a suite of benchmark tT paths can be designed to leverage the temperature sensitivity of a particular low-temperature thermochronometer and then tuned to specific kinetics models. We propose that the six benchmark paths we use in this work can provide a practical tool for the thermochronology community to use in a variety of contexts, including comparing kinetics models and predicting data patterns that arise from variable mineral compositions or geometries. This 'design-then-tune' approach is not meant to identify a single 'best' kinetics model for a particular system but to quantify and visualize how kinetics





225	models predict different tT conditions and data patterns. Having a common framework can also
226	be used in the future to facilitate communicating how new kinetics models differ from existing
227	models. The design and tuning decisions we made here provide a common reference point for
228	interpreting AHe, AFT, and ZHe data, but a single suite of tuned paths cannot capture all
229	complexities of these systems. For example, our proposed benchmark paths span a 100 Myr
230	time frame (Fig. 1)—a time period that may be insufficient for capturing the accumulation of
231	radiation damage and/or annealing that is a hallmark of the AHe and ZHe systems and is
232	captured in those kinetics models. Despite these limitations, we envision that benchmark paths
233	can serve as an entry point to thinking critically about the relationship between the style of a tT
234	history and the kinetic behaviors of chronometric systems that are sensitive to both temperature
235	and time.
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237	Competing Interests
238	All authors are Coordinators for the GChron Special Issue "Technical notes on modelling
239	thermochronologic data" to which this technical note is submitted.
240	
241	Author Contributions
242	ALSG, KEM, ALA, and MW all contributed to the project design and modeling. ALSG and KEM
243	prepared the manuscript with contributions from all authors.
244	
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